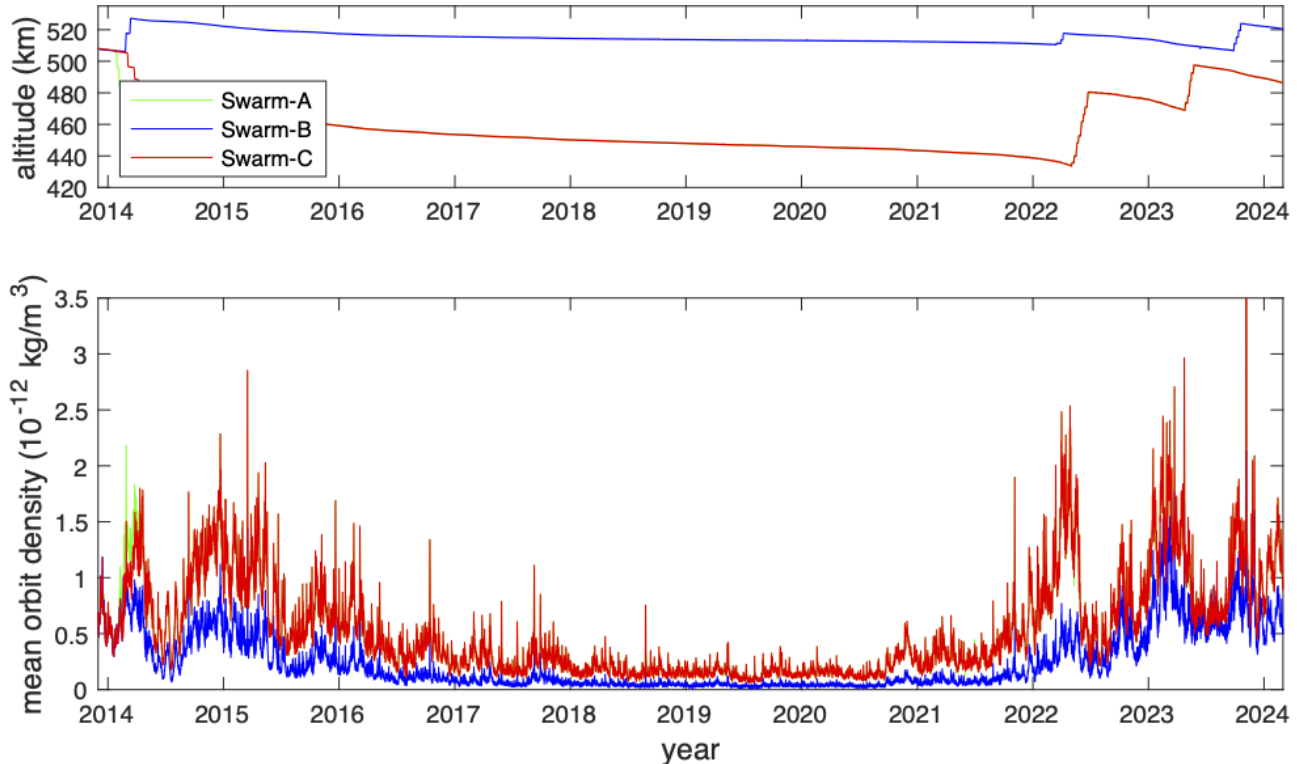


# Assessment of GPS-based accelerometry performance with adaptive filter settings

Jose van den IJssel, Christian Siemes, Pieter Visser  
Delft University of Technology

Swarm 10 Year Anniversary and Science Conference, 8-12 April 2024

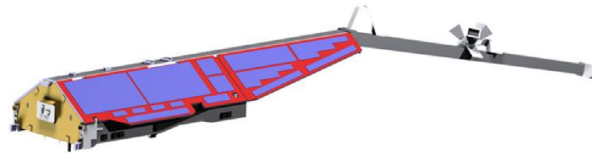
# Swarm GPS-derived densities



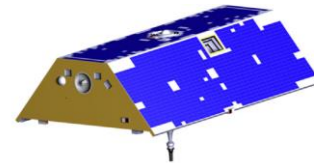
Density signal varies over the mission with clear impact of solar cycle and altitude. GPS-based accelerometry settings are fixed and optimized for early mission.

# GPS-accelerometry performance assessment using GRACE data

- The GRACE satellites deliver high-accuracy accelerometer data → allows accurate comparison with GPS-derived results
- The GRACE satellites have experienced a large range of density signals from  $10^{-13}$  kg/m<sup>3</sup> to  $10^{-11}$  kg/m<sup>3</sup> → allows tuning of filter settings for various conditions



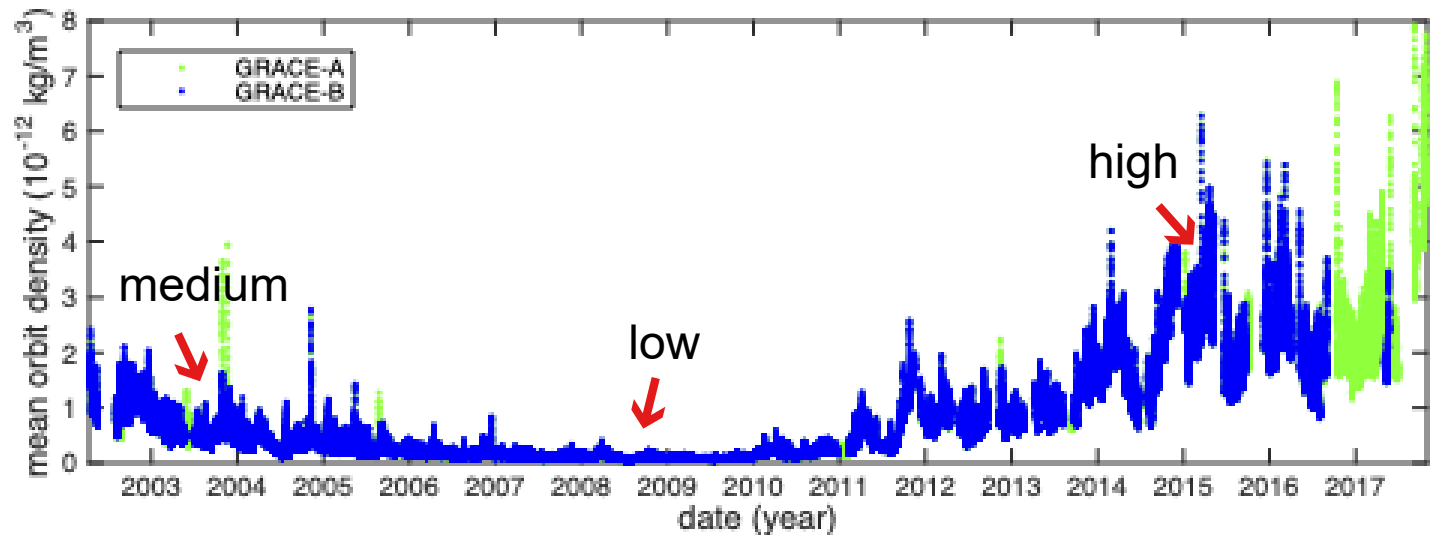
Swarm



Grace

# Test periods

case	satellite	period	mean density
low	Grace-B	November 2008	$1.01 \cdot 10^{-13} \text{ kg/m}^3$
medium	Grace-B	November 2003	$7.77 \cdot 10^{-13} \text{ kg/m}^3$
high	Grace-B	April 2015	$21.79 \cdot 10^{-13} \text{ kg/m}^3$



Selection taking into account: temperature control / data gaps / maneuvers

# Implementation GRACE GPS-based accelerometry chain

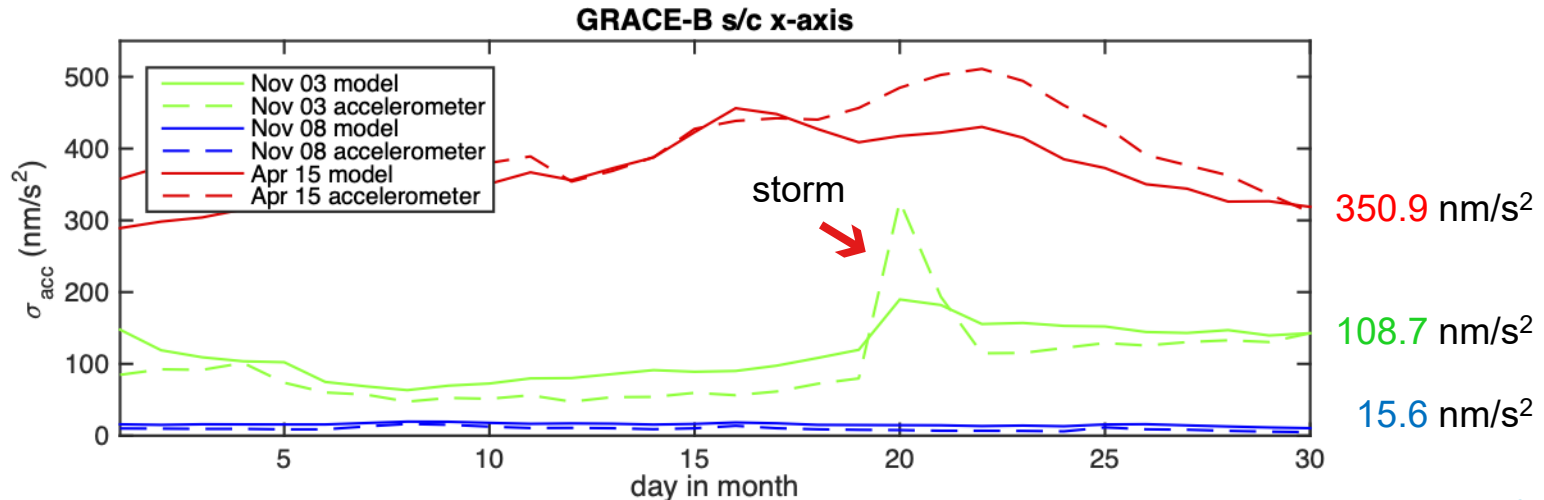
Implementation based on Swarm L2 GPS-based accelerometry chain

- **Extended Kalman filter approach** with DLR GHOST s/w using 26hr arcs
- Undifferenced ionosphere-free GPS observations
- Final CODE ephemeris and 5s clock product
- Attitude information from star tracker data
- GRACE **PCV map** provided by Astronomical Institute of University of Bern
- Estimation of float carrier phase ambiguities
- State-of-the-art gravitational modelling
- SRP, Earth albedo and infrared modeling based on **8-plate macro model** with surface properties for absorbed, diffusely or specular reflected radiation
- Instantaneous reemission thermal modeling for non-solar panel surfaces
- **Smooth empirical accelerations recover the aerodynamic signal**

# Tuning of empirical accelerations $\rightarrow$ adaptive $\sigma_P$

Empirical accelerations that absorb the aerodynamic signal are defined by a steady-state variance  $\sigma_a$ , process noise  $\sigma_P$  and correlation time  $\tau$ .

In radial and cross-track direction small aerodynamic signal  $\rightarrow \sigma_P = 5 \text{ nm/s}^2$ .  
In along-track direction large variation in aerodynamic signal  $\rightarrow$  adaptive  $\sigma_P$ .  
Adaptive  $\sigma_P$  is based on variance of NRLMSISE-00 model accelerations.



# Quality measures

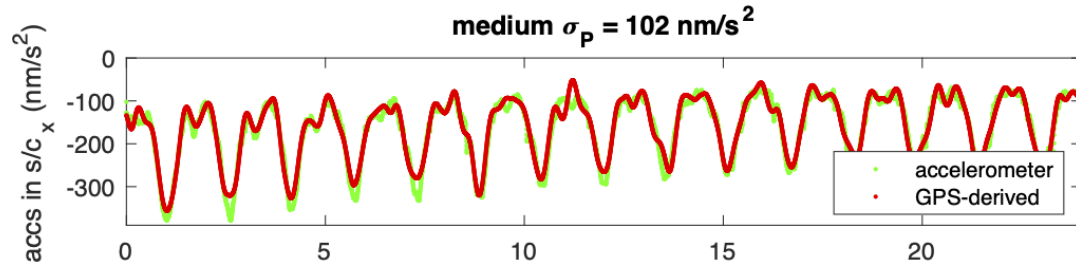
Comparison GPS-derived aerodynamic accelerations with accelerometer data

- Remove RP signal from accelerometer data using the same panel model
- Rotate GPS-derived accelerations from orbit to satellite body frame

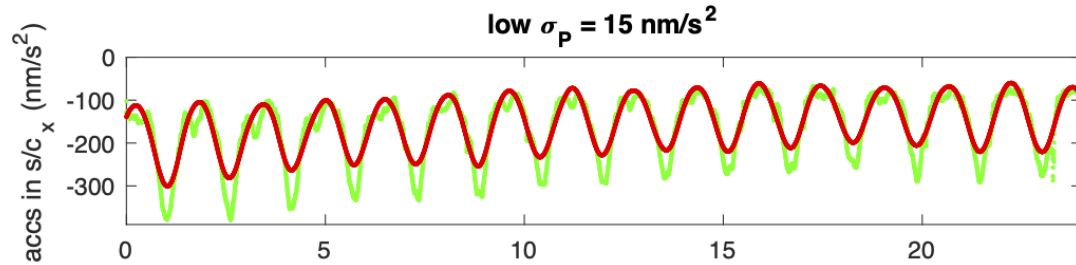
## Quality measures

- RMS differences (accelerometer – GPS)
- Relative recovery error ( $\text{RMS}_{\text{diffs}}/\text{RMS}_{\text{acc}}$ )
- Correlation
- PSD

# Impact of different process noise settings

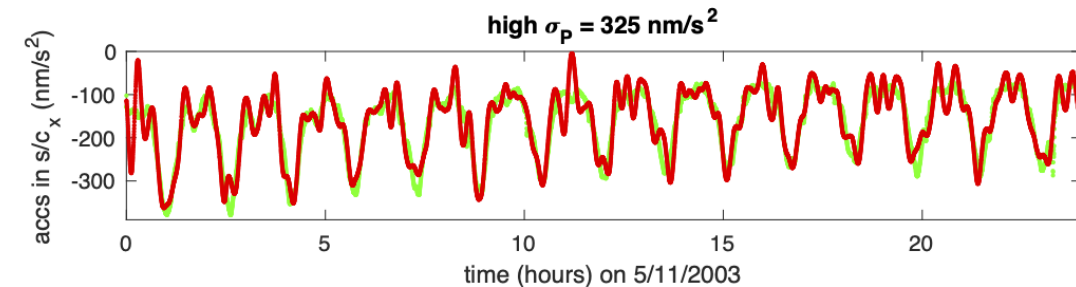


RMS	18.0 nm/s <sup>2</sup>
rel error	10.1 %
correl.	0.973



RMS	30.3 nm/s <sup>2</sup>
rel error	16.9 %
correl.	0.931

→ Accelerations are too smooth

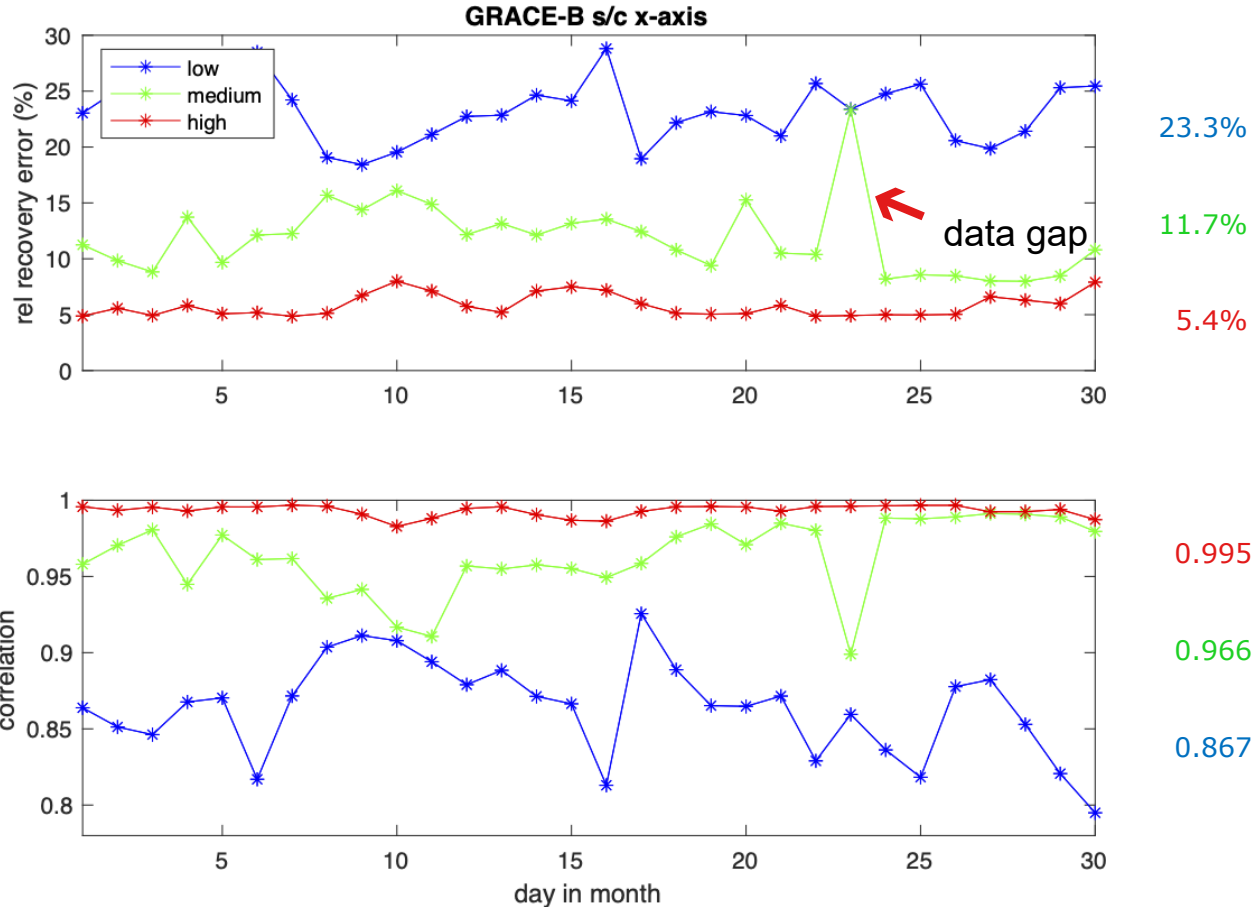


RMS	32.7 nm/s <sup>2</sup>
rel error	18.3 %
correl.	0.908

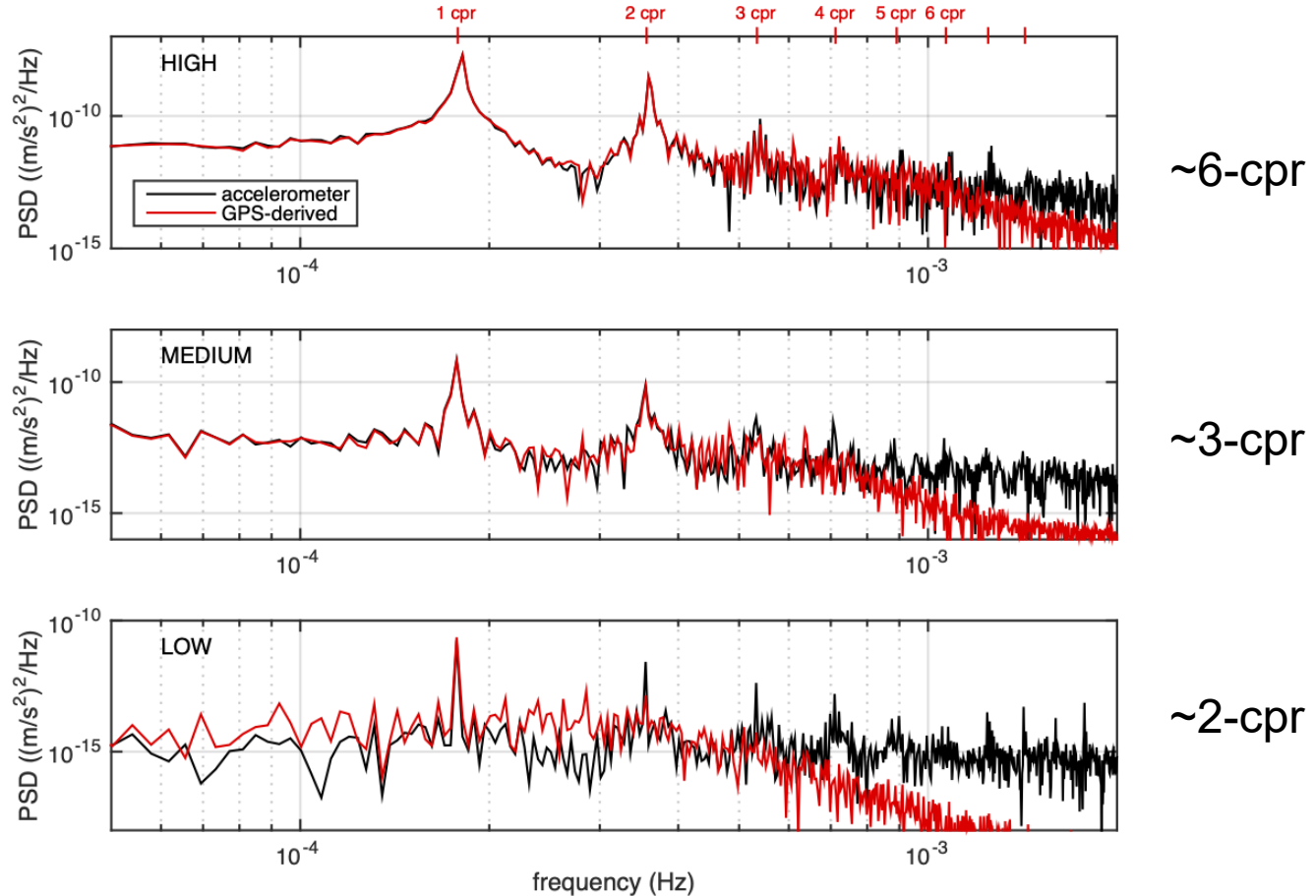
→ Accelerations are too wobbly



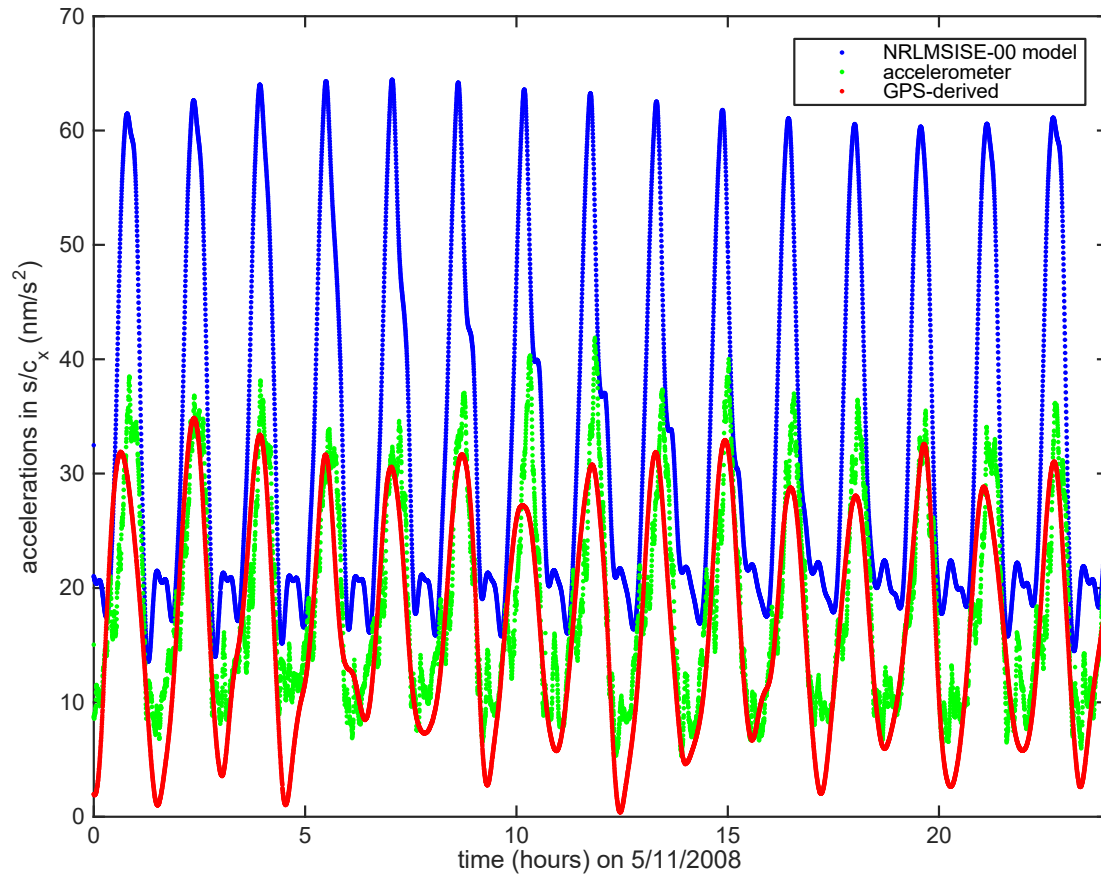
# Performance of low/medium/high signal cases



# Performance of low/medium/high signal cases

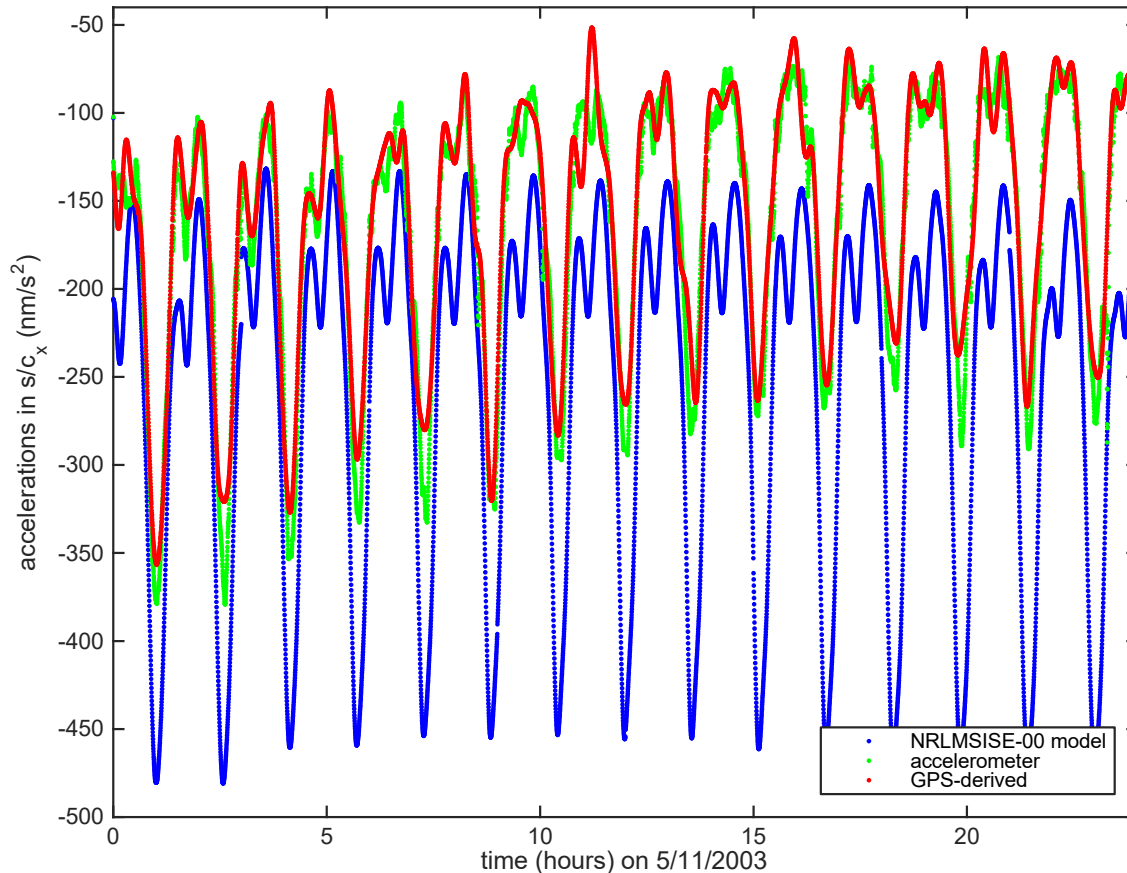


# Low signal example day



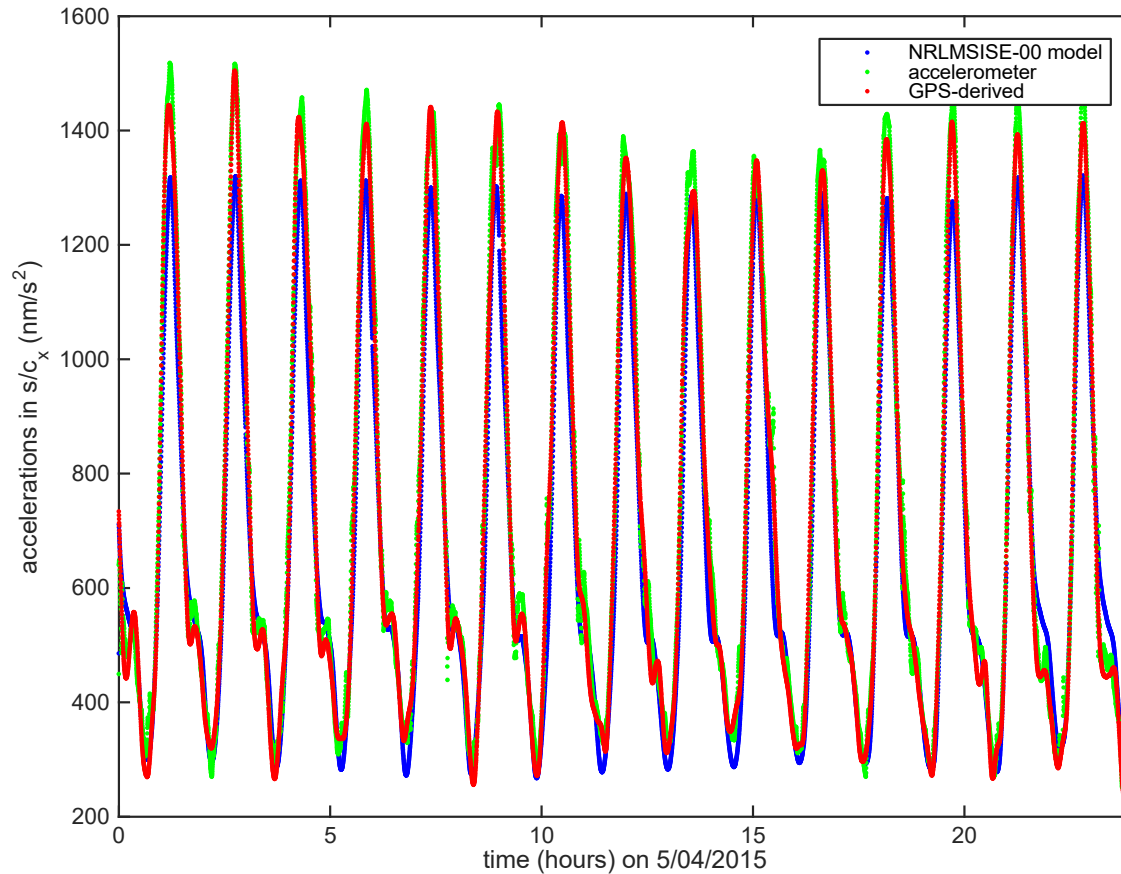
	GPS	model
RMS ( $\text{nm/s}^2$ )	4.9	17.1
rel error (%)	24.2	84.2
correl.	0.870	0.867

# Medium signal example day



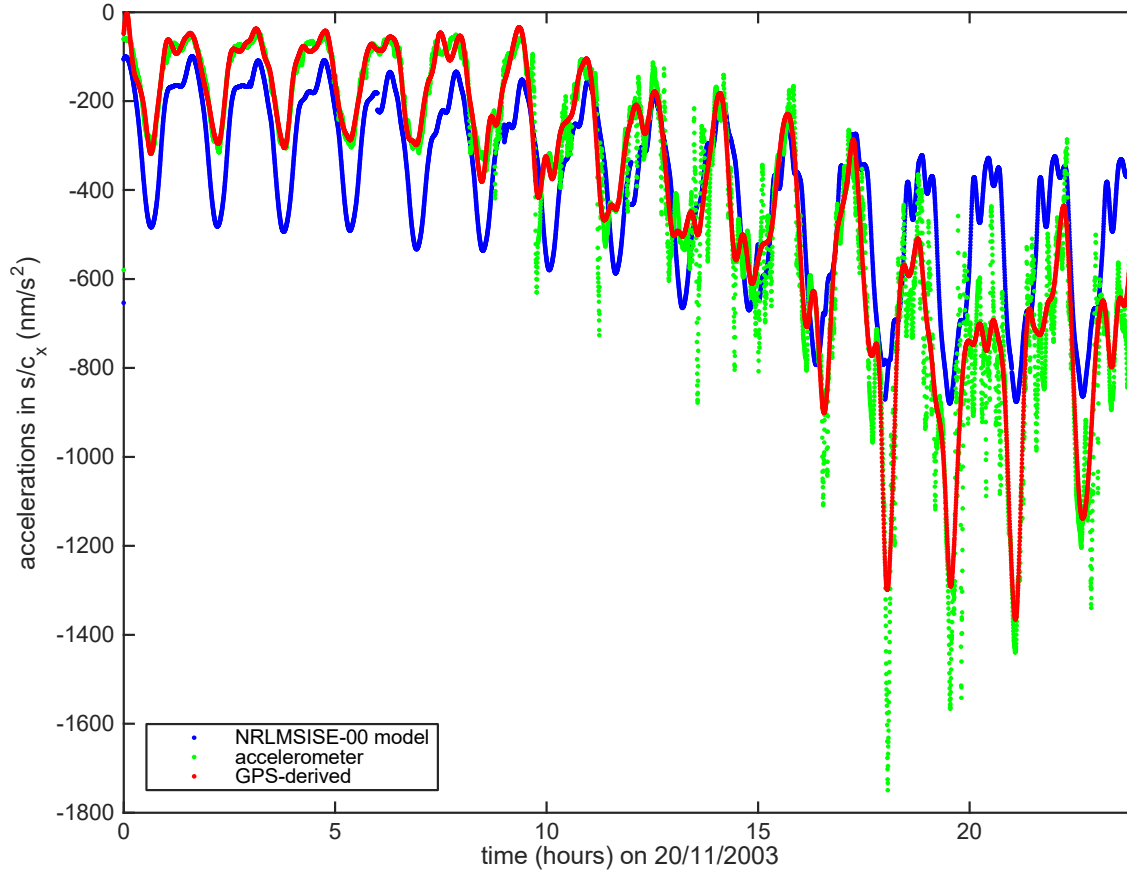
	GPS	model
RMS ( $\text{nm/s}^2$ )	17.3	103.5
rel error (%)	9.7	57.8
correl.	0.977	0.923

# High signal example day



	GPS	model
RMS ( $\text{nm/s}^2$ )	41.4	96.8
rel error (%)	5.1	11.9
correl.	0.996	0.987

# Geomagnetic storm example day



	GPS	model
RMS ( $\text{nm/s}^2$ )	81.1	203.5
rel error (%)	15.3	38.3
correl.	0.971	0.822

# Conclusions and outlook

## Conclusions

- Adaptive process noise improves the recovery of aerodynamic accelerations
- GPS-based accelerations show better agreement with accelerometer data than NRLMSISE-00 model accelerations
- Best performance with strong signal (0.995 correlation, 5.4% recovery error)
- Limited performance with low signal (0.867 correlation, 23.3% recovery error)

## Outlook

- Apply adaptive process noise to Swarm GPS-based density retrieval
- Further improve SRP modelling (Poster 56 Natalia Hladczuk)
- Further improve GSI modelling (Poster 54 Sabin Anton)
- Add uncertainty information to our densities (Siemes et al., Uncertainty of thermosphere mass density observations derived from accelerometer and GNSS tracking data, ASR, 2023)
- Apply GPS-accelerometry to other missions: NanoMagSat, GDC...