



THE UNIVERSITY  
of EDINBURGH

# Detecting Waves in Core Surface Flow Acceleration Derived from 26 Years of Secular Variation

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# Background

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- Since 1999: (Almost) continuous satellite monitoring of the magnetic field
- Satellites provide much improved spatio-temporal coverage
- Allows us to see rapid field changes world wide
- Allowed seeing signatures of **hydromagnetic waves**

**Aim: See signatures of such waves in the core flow acceleration**

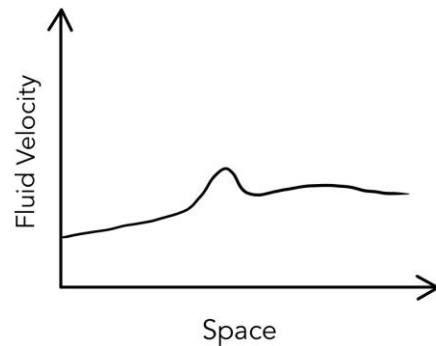
# Determining a flow from secular variation data

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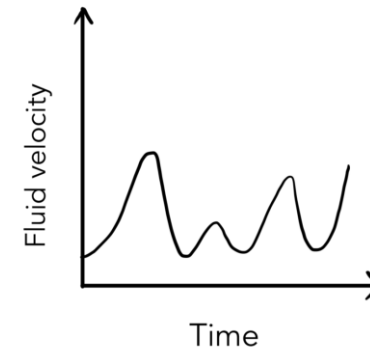
- Invert the radial magnetic induction equation, assuming frozen flux (negligible diffusion)

$$\dot{B}_r = -\nabla_H \cdot (\mathbf{u}B_r)$$

- Regularization in time and space: assume flow large scale, only little change in time



Minimise second spatial derivative of the flow



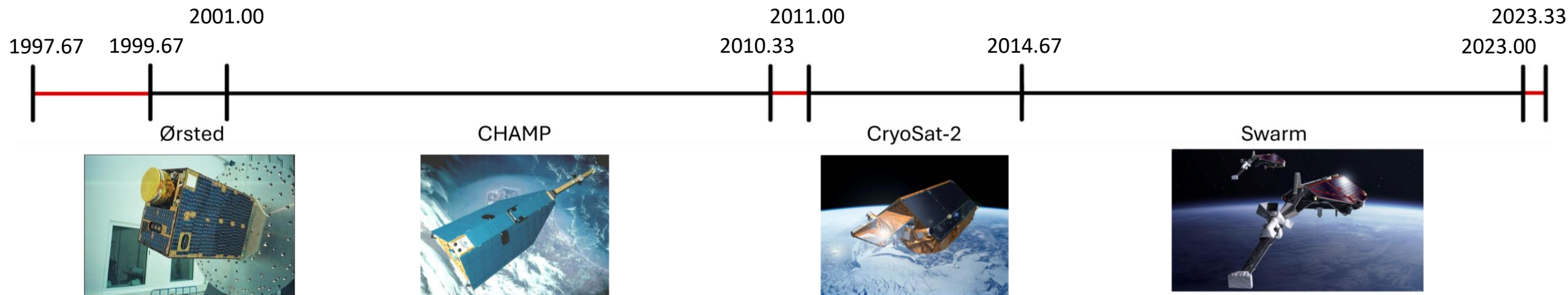
Minimise flow acceleration

- Main field treated as known, specified by the CHAOS-7 model

# The Secular Variation Data

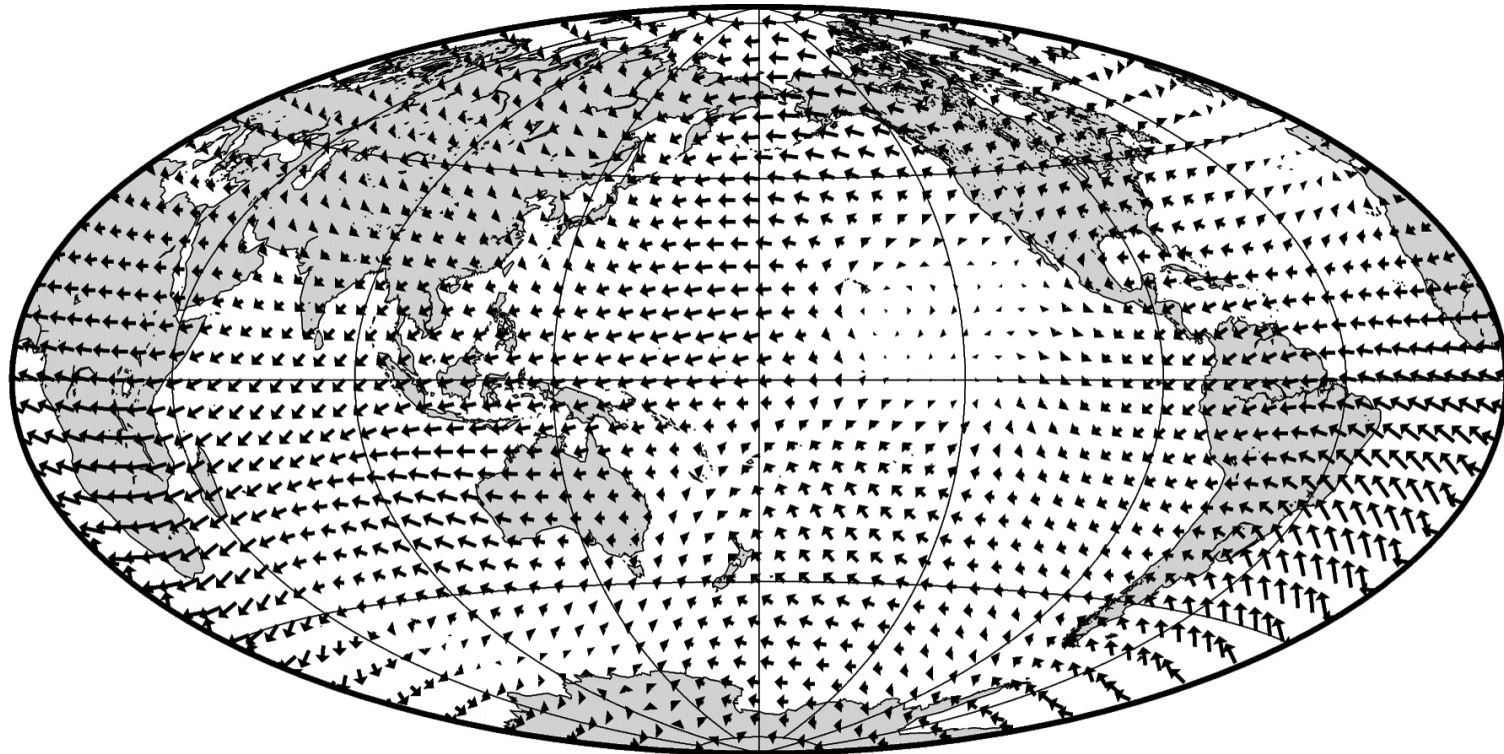
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- Combination of Swarm data with other satellite and ground observatory data
- Satellite data is represented by geomagnetic virtual observatories
- Higher quality data chosen when overlapping



# The resultant flow

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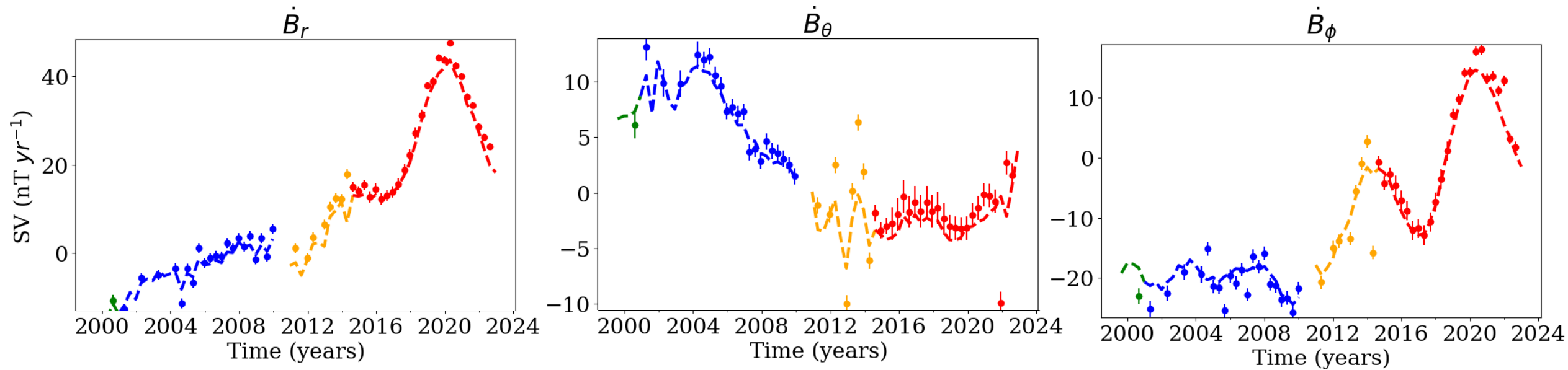


1997.67

→  
10.0km/yr

(Note: Continents  
for reference only)

# Flow-predicted secular variation



Scatter dots: Observations, Dashed line: Flow predictions  
Green: Ørsted, Blue: CHAMP, Orange: CryoSat-2, Red: Swarm

# Calculating flow acceleration

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$$a_t = u_t - u_{t-1}$$

Acceleration at time  $t$    Velocity at time  $t$    Velocity at time  $t - 1$

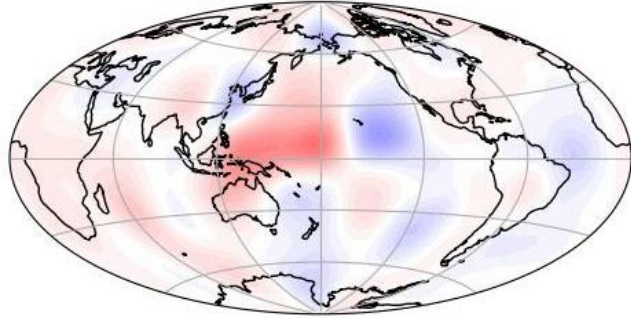
- No smoothing involved
- Temporal damping minimised the acceleration
  - Any acceleration seen must be included to fit the flows to the data



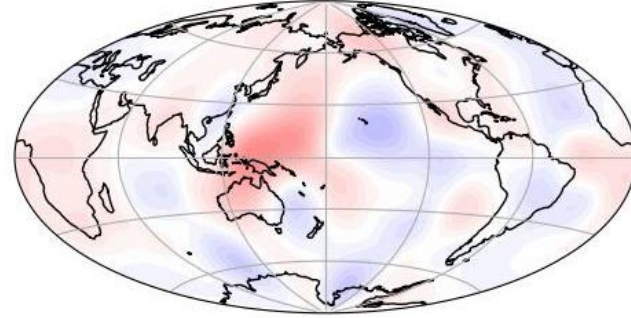
# Azimuthal Acceleration Profile

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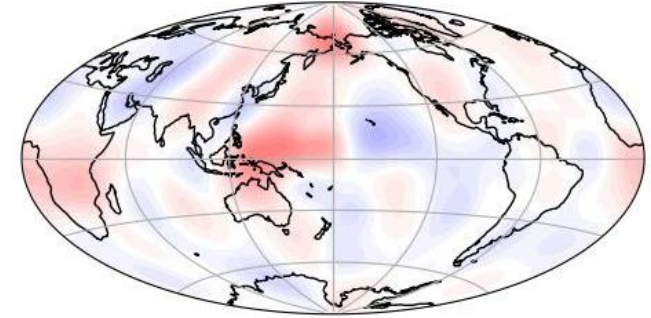
2019.33



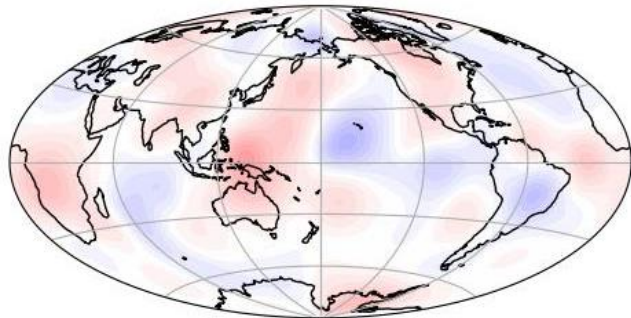
2019.67



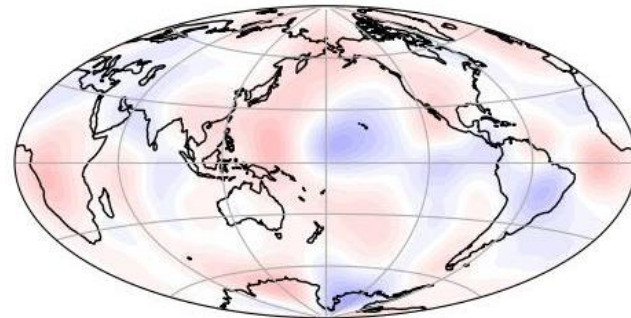
2020.00



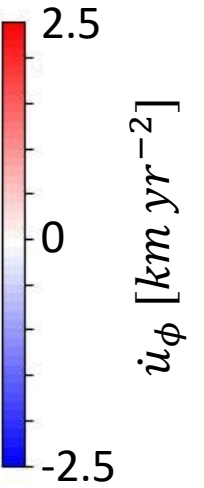
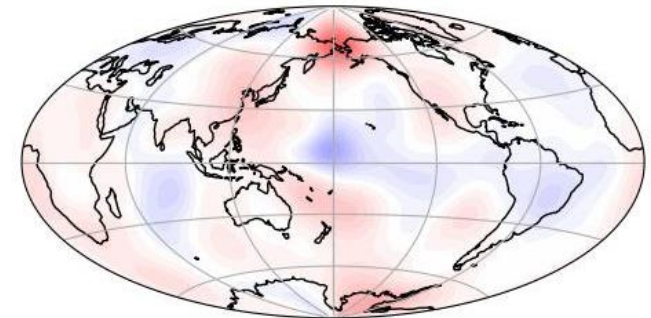
2020.33



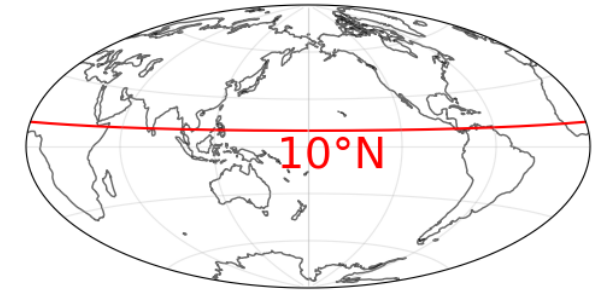
2020.67



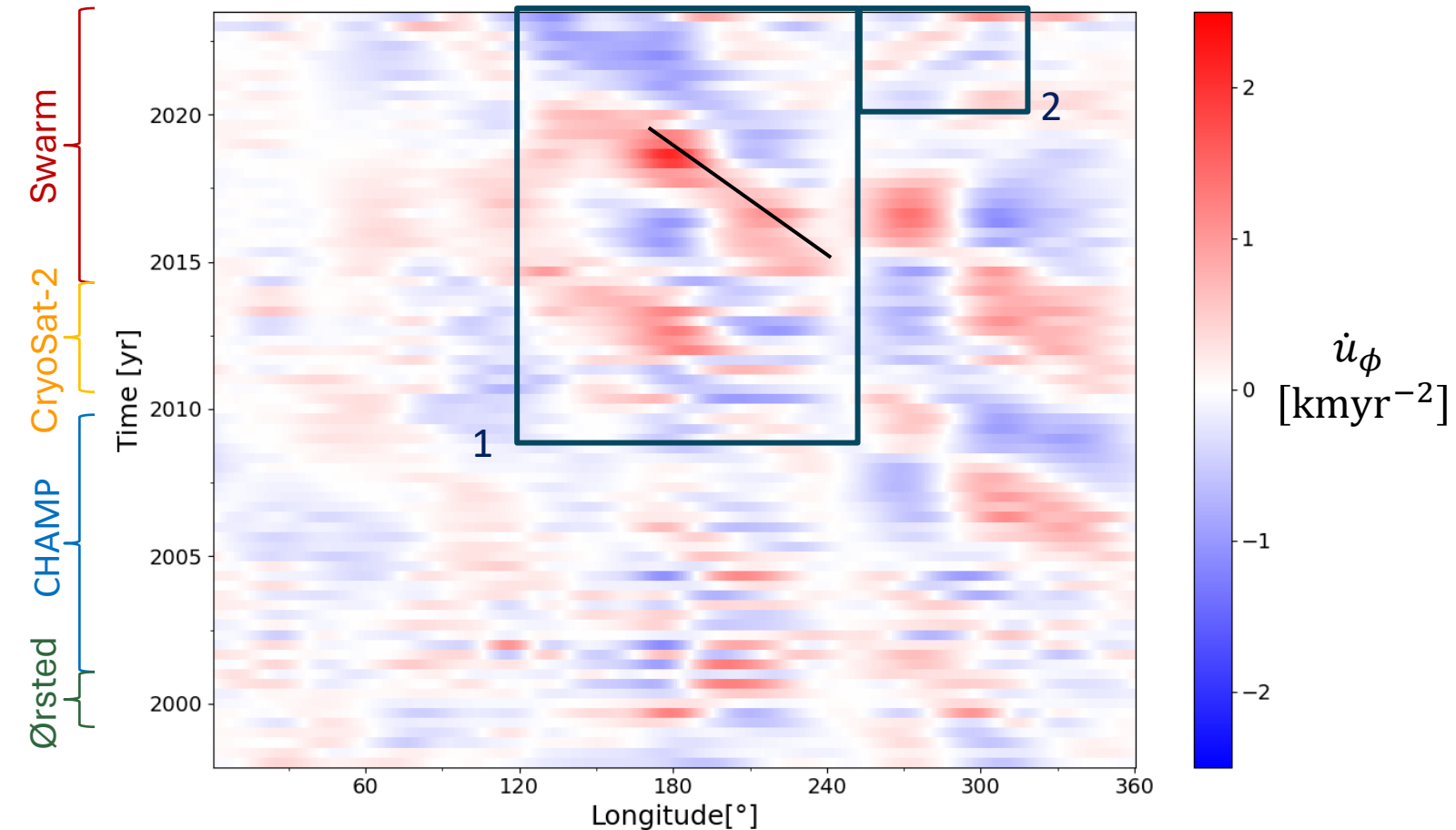
2021.00







# Time-longitude section

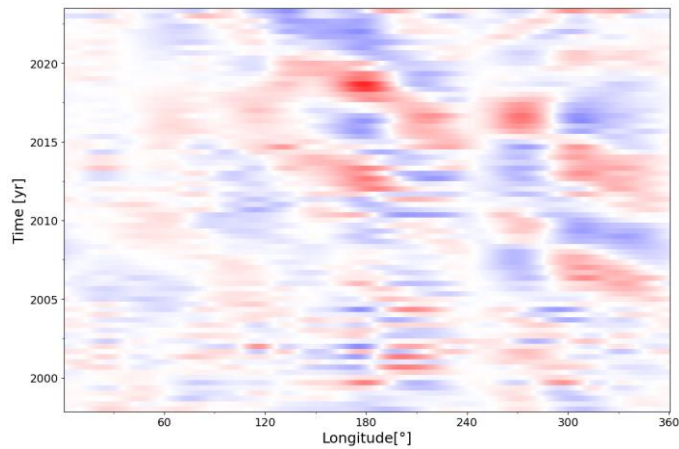
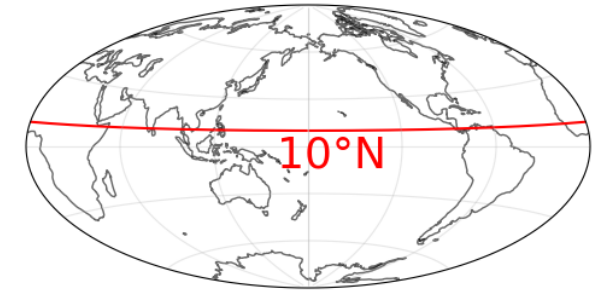


**1** – Left sloping features of alternating sign

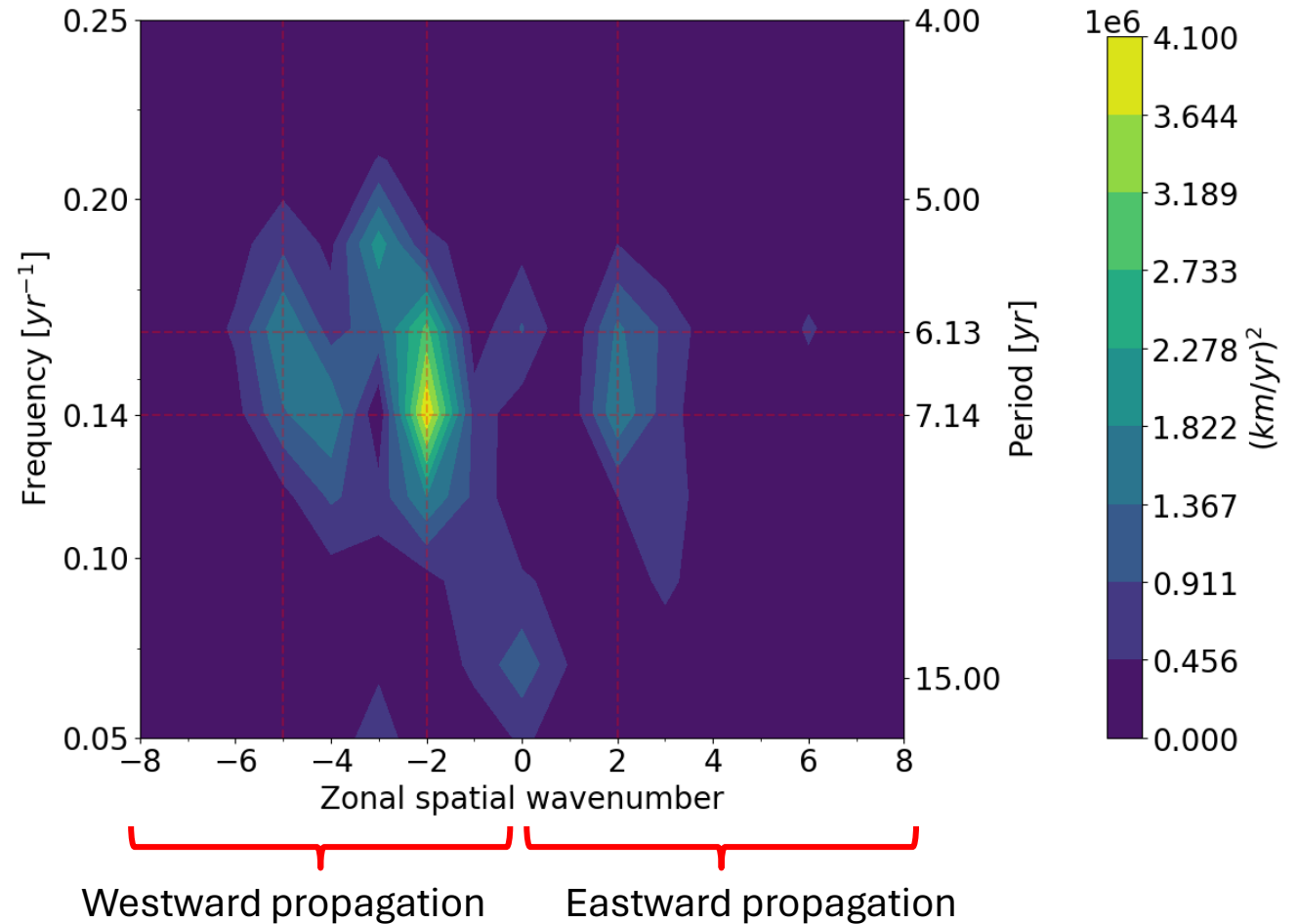
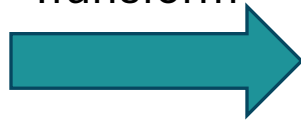
**2** – Weaker, right sloping features

Features travel westward at velocities on the order of 1700km/yr

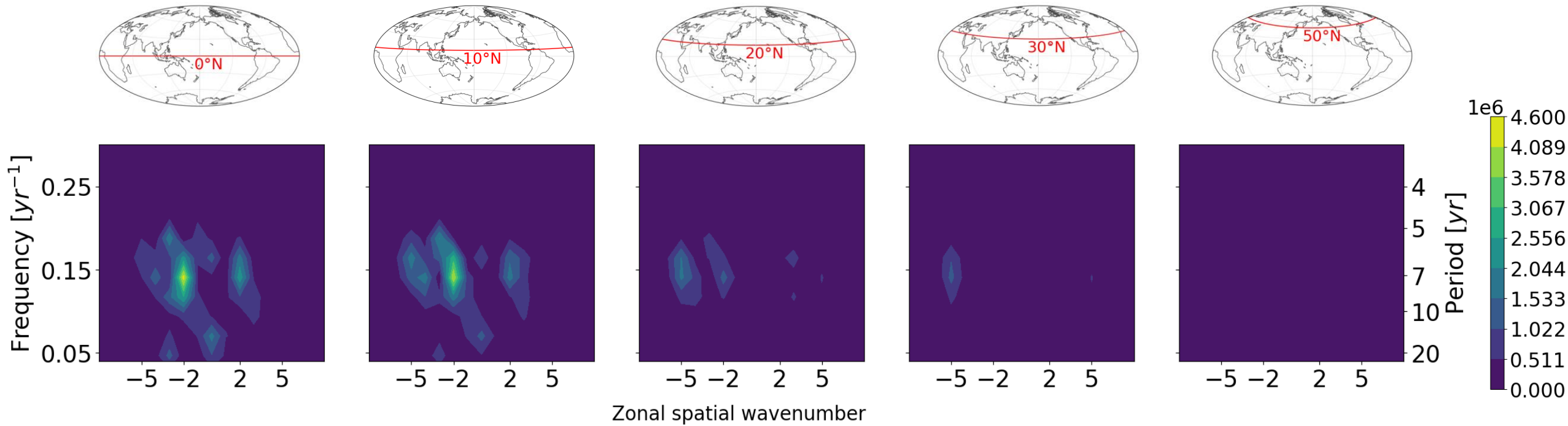
# Power spectral density



2D Fourier Transform

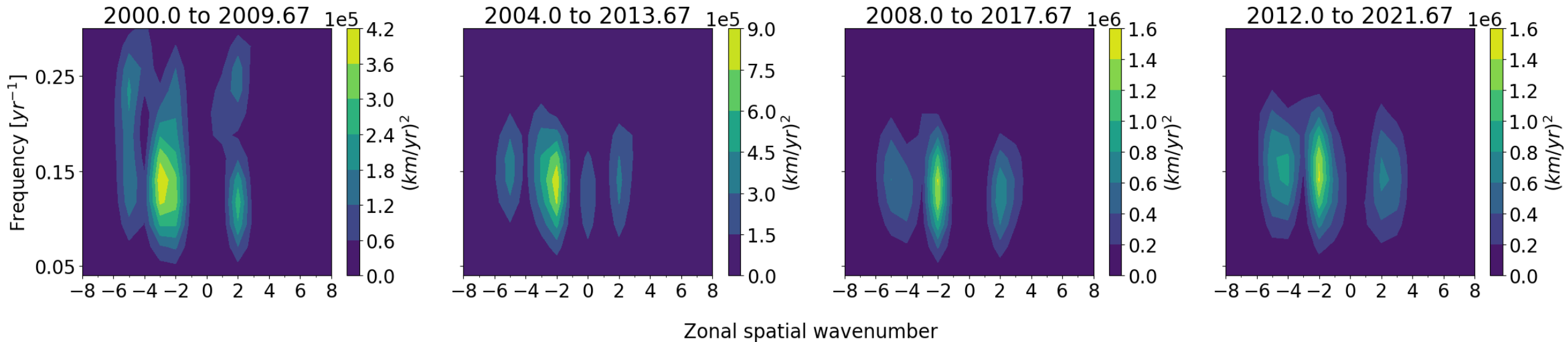
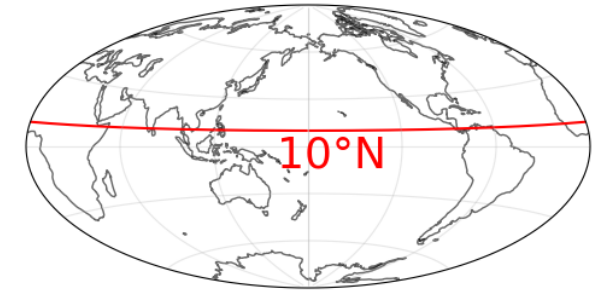


# Spatial variations



- Focusing at low latitudes
- One order of magnitude smaller at 20°N

# Time variations



- Repeat analysis on overlapping intervals of length 10 years
- Noisier start, but afterwards the signal persists through time

# Summary

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- Inverted a 26-year SV dataset of GVO satellite and ground observations for core surface flows.
- Flow acceleration shows systematic periodic features travelling at velocities on the order of 1700km/yr
- PSD shows both eastward and westward travelling modes at spatial wavenumbers -5, -2, and 2, with periods of ~6 and ~7 years.
- Features are focussed on low latitudes.
- Features appear robust in time.