

Total square-Root Electron Content (TREC): Sounding the Ionosphere with ELF Whistlers Detected by the Swarm Mission

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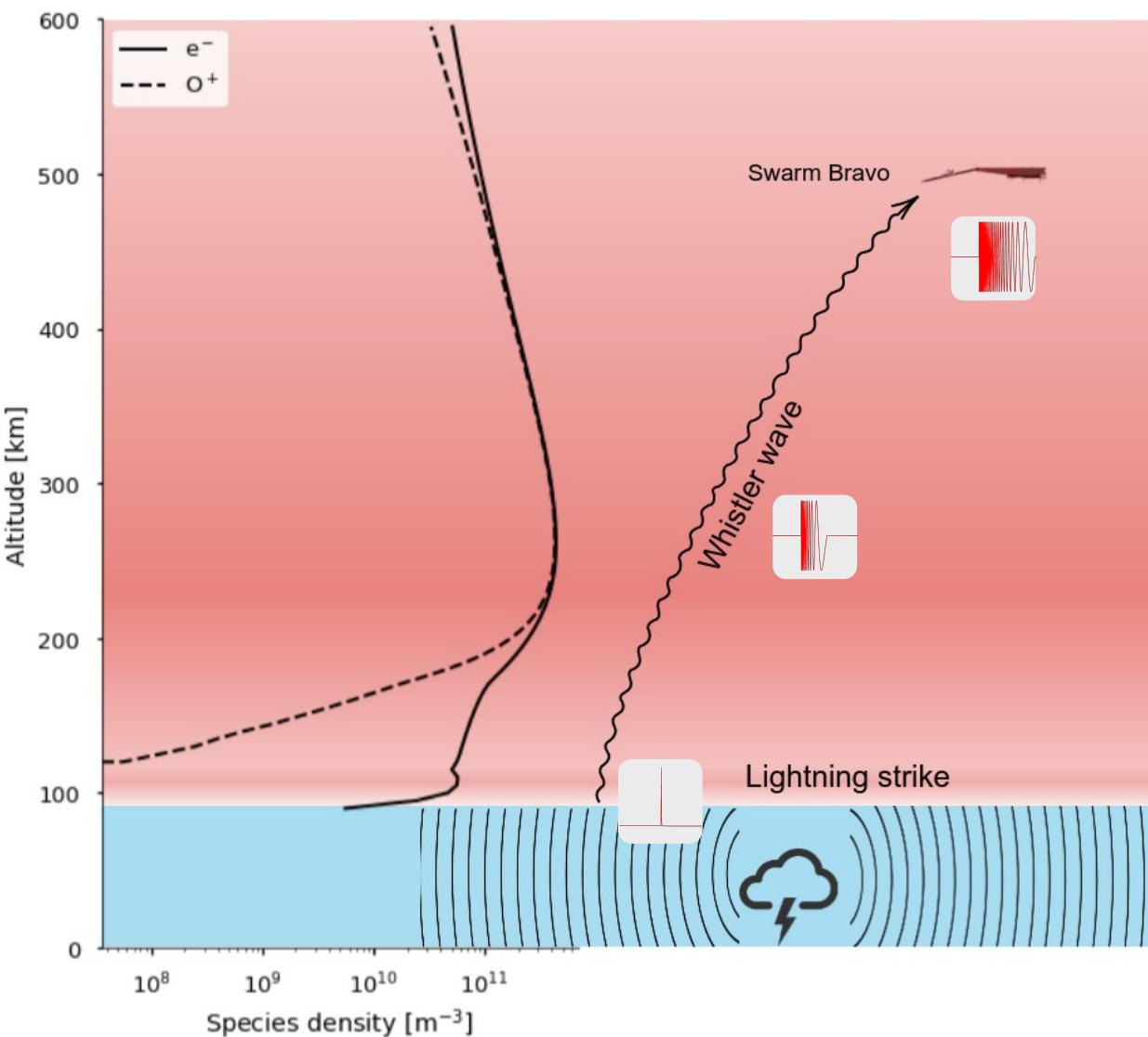
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Whistler in Extremely Low Frequency: what is this ?



- Whistlers in Extremely Low Frequency (ELF): **Electromagnetic** signals propagating through the **ionosphere**
- Originate from **lightning** generated impulsion **leaking** into the ionosphere
- Detected by Swarm **Absolute Scalar Magnetometers** (ASM) during **burst sessions**
- Whistlers are **dispersed** during their propagation depending on the **ionospheric condition**
- The propagation “**follows**” the magnetic field, i.e. ψ is mostly constant

$$\psi = \angle(\vec{k}, \vec{B})$$

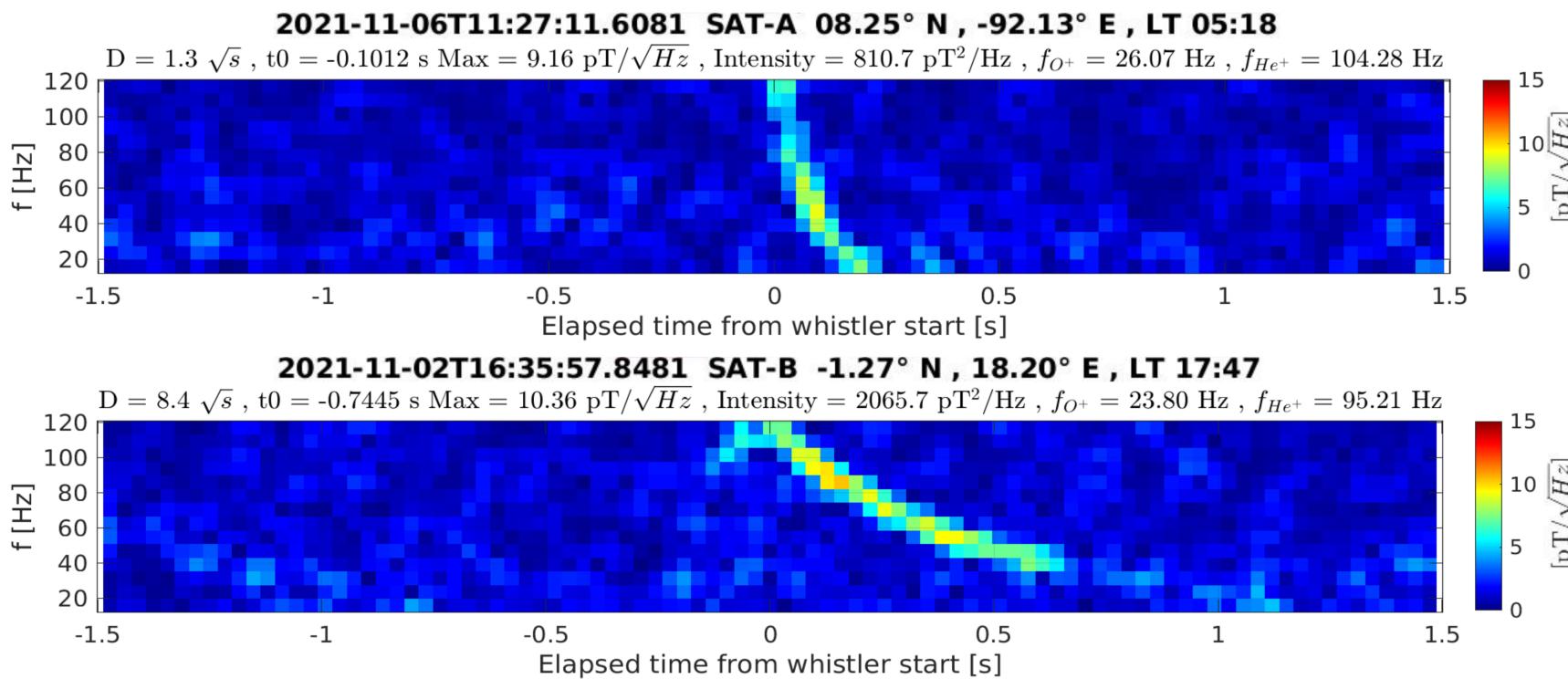


Lightning Generated Whistlers detected by Swarm

The whistlers data come from the **burst mode sessions** of the **ASM** (one week every month for Alpha and Bravo):

- **WHLxEVT_2_product**: 100000+ detections, up to several hundreds a day
- Whistlers detection between **10 Hz** and **120 Hz**: ELF range

[See poster of Pierdavide Coïsson]



Objective:
**Retrieve ionospheric
parameters from
Swarm's whistler data**



ELF ionospheric propagation theory

- Neutral, cold, collisionless, 1D plasma containing only e^- and O^+
- For ELF propagation above the gyrofrequency f_{gi} of the plasma

Stix [1966] equation for the refractive index:

$$n^2 = \frac{RL \sin^2 \psi + PS(1+\cos^2 \psi) \pm \sqrt{(RL-PS)^2 \sin^4 \psi + 4P^2 D^2 \cos^2 \psi}}{2S \sin^2 \psi + 2P \cos^2 \psi}$$

R, L, P, S, D depend on the plasma and the magnetic field

In **ELF**, within the **ionosphere**, we have the following: $f_{pe} \gg f$; $f_{ge} \gg f$; $f_{pi} \gg f$; $m_i \gg m_e$

$$n^2 \simeq \frac{f_{pi}^2}{f_{gi}^2 - f^2} \left(1 + \frac{1}{2} \tan^2 \psi - \sqrt{\frac{1}{4} \tan^4 \psi + \frac{f^2}{f_{gi}^2 \cos^2 \psi}} \right)$$



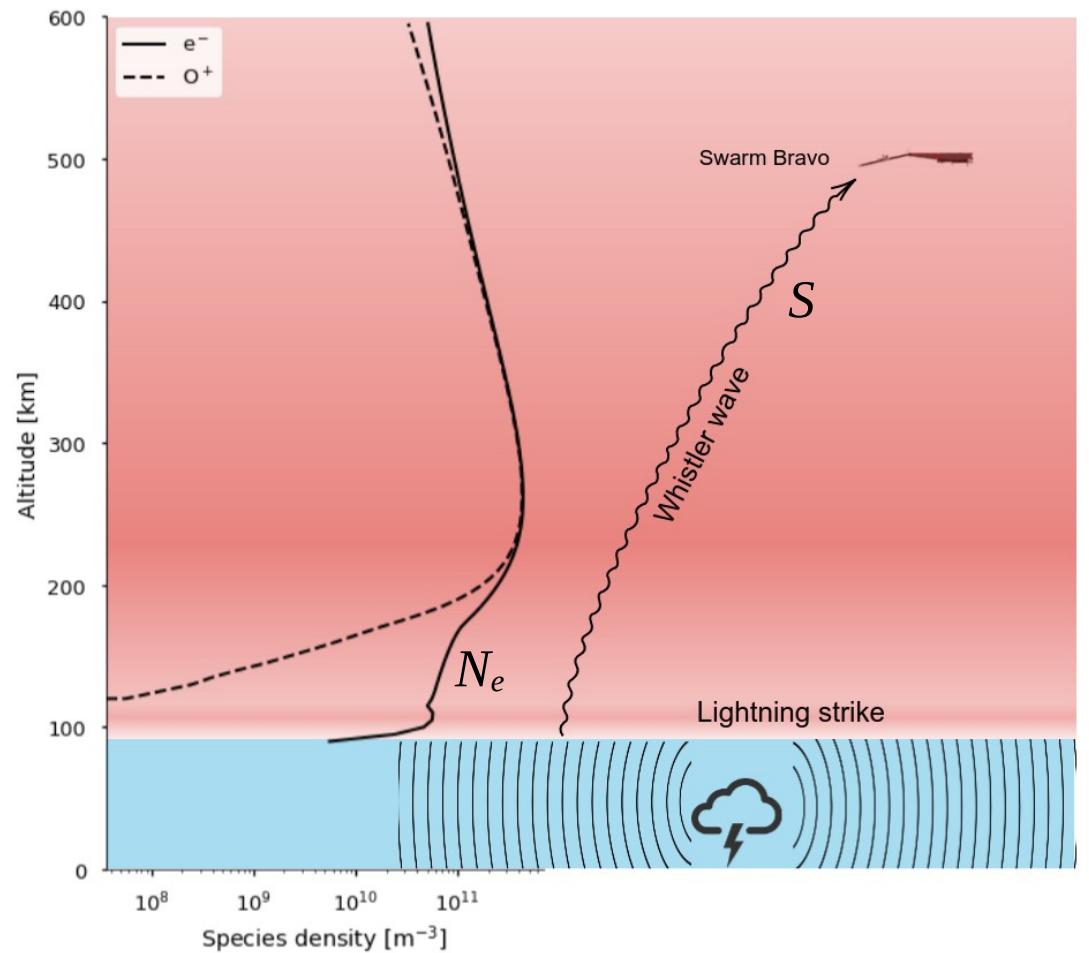
Link between the group delay and the electron density

$$T(f) \simeq K(f, B, \psi) \int_S \sqrt{N_e(s)} ds$$

- T is the **group delay** for the signal to propagate through the ionosphere to our instrument.
- N_e is the **electron density**
- S is the **ray path length**
- K is a coefficient that depends on the **frequency** f , the strength of the **magnetic field** B , and ψ

We call this integral **Total Root Electron Content** (TREC)

$$TREC(S) = \int_S \sqrt{N_e(s)} ds$$





Dual frequency method

How do we derive the TREC from Swarm's whistler signal ?

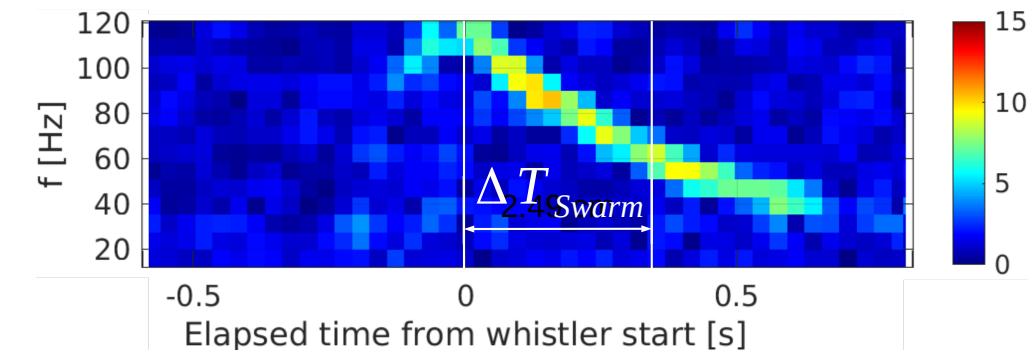
$$T(f_i) \simeq K_i \text{ TREC}(S_i)$$

We define the mean path S and σ :

$$S(r) = \frac{S_2(r) + S_1(r)}{2} \quad \sigma(r) = \frac{S_2(r) - S_1(r)}{2}$$

At frequencies f_1 and f_2 for the **mean ray path S** :

$$\underbrace{T(f_2) - T(f_1)}_{\Delta T} = \Delta T(f_1, f_2) = \gamma_{12} \text{ TREC}(S) + b_{12}$$



where γ_{12} and b_{12} are functions of K_1 and K_2 and σ

If we know the **parameters γ_{12} and b_{12}** we can estimate the **TREC** from the **observed ΔT** .

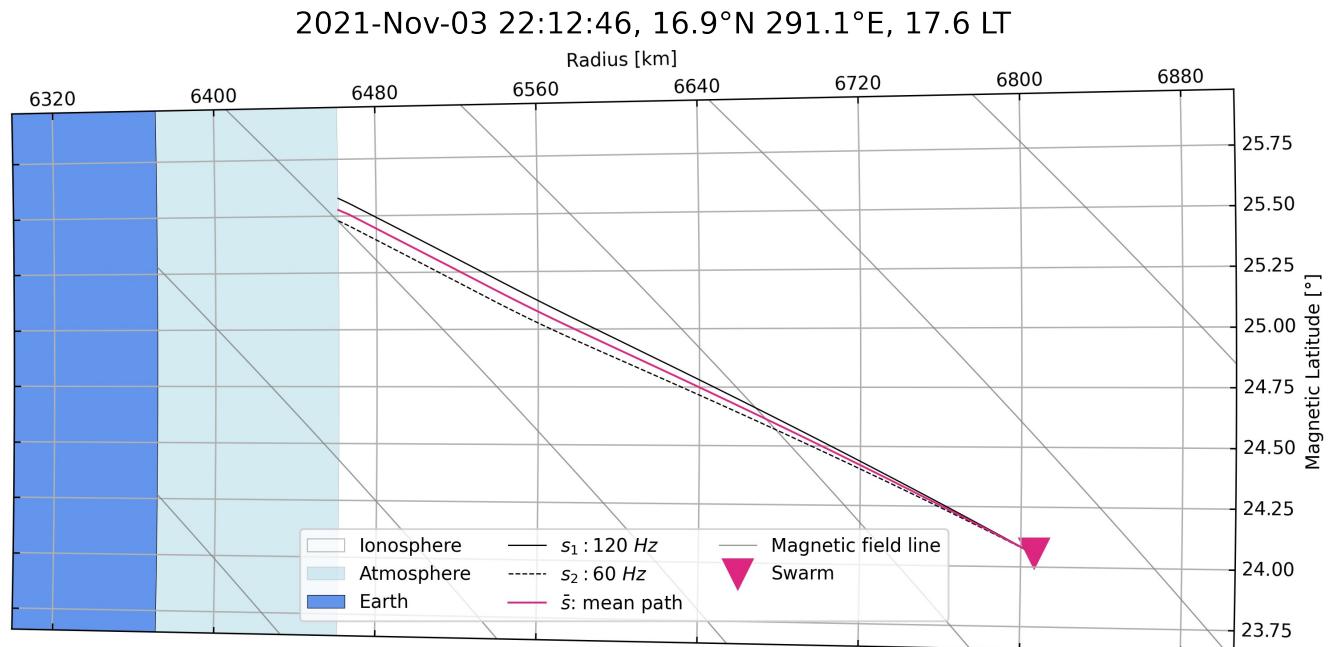
$$\text{TREC}(S) = \frac{\Delta T(f_1, f_2) - b_{12}}{\gamma_{12}}$$



Propagation modelisation with ray-tracing

Initial wave-vector is vertical at the base of the ionosphere (90 km)

- **Climatological IRI** (2016 or 2020) [Bilitza et al. 2017 and 2022]
- Magnetic field: **IGRF-13** [Alken et al. 2021]
- Outputs for each frequency:
 - **group delay T_1 and T_2**
 - **ray path S_1 and S_2**



Estimation of the **coefficients y_{12} and b_{12}** with ray tracing through IRI:

$$y_{12} = K_2 - K_1 = \frac{T_2}{TREC(S_2)} - \frac{T_1}{TREC(S_1)}$$

$$b_{12} = (K_2 + K_1) \int_{r_0}^{r_{sw}} \sqrt{N_e(r)} \frac{d\sigma}{dr} dr$$



Dual frequency method

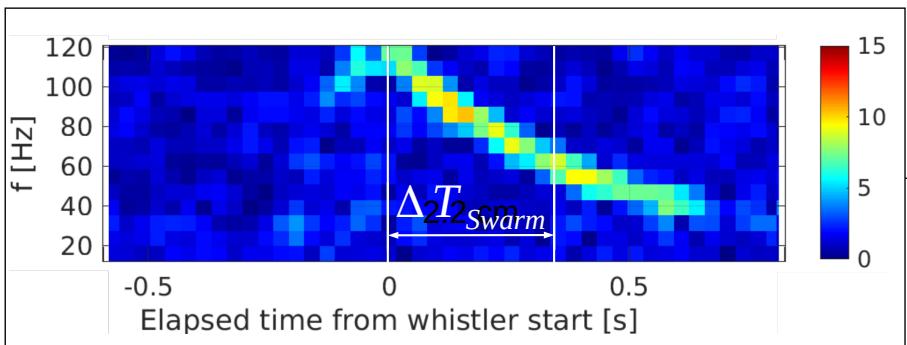
Models

Climatological IRI

- TREC from direct integration
- T_1 and T_2 from ray-tracing

γ_{12} b_{12} S_{IRI}

ASM detections

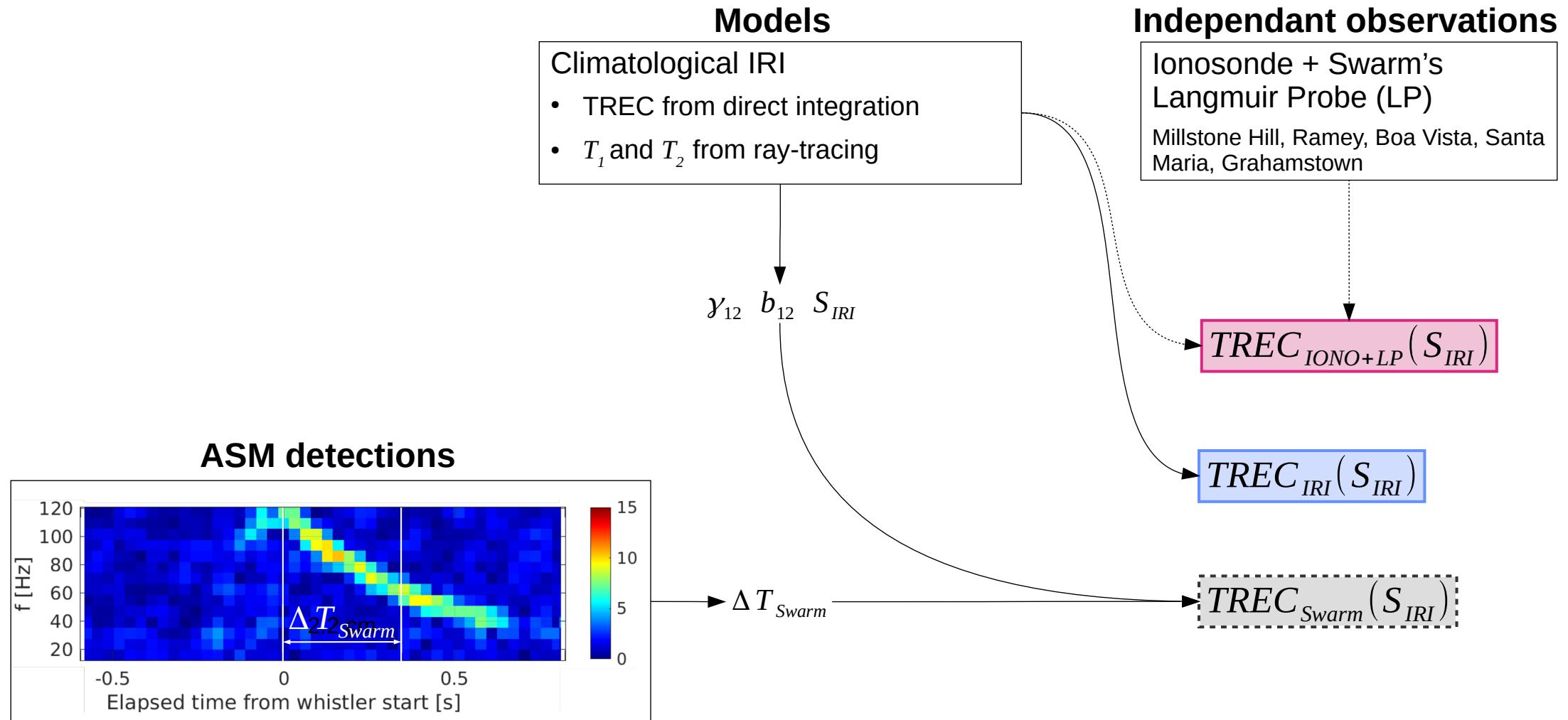


ΔT_{Swarm}

$TREC_{Swarm}(S_{IRI})$



Validation method





Verification data: Ionosonde and Langmuir probes



- Chosen stations: Millstone Hill, Ramey, Boa-Vista and Santa Maria, Grahamstown
- Selection of whistlers occurring **within 500 km** of an active ionosonde station
- Keep whistlers **within 7.5 minutes of the closest profiles**

Topside (above hmF2) of ionograms are usually modelled. We replace it with a better informed topside:

- Modeled with the **NeQuick2 topside function**
- Anchored on Swarm **Langmuir Probe (LP)** plasma density



Results (Boa-Vista, near equator) and discussion

$TREC_{Swarm}(S_{IRI})$

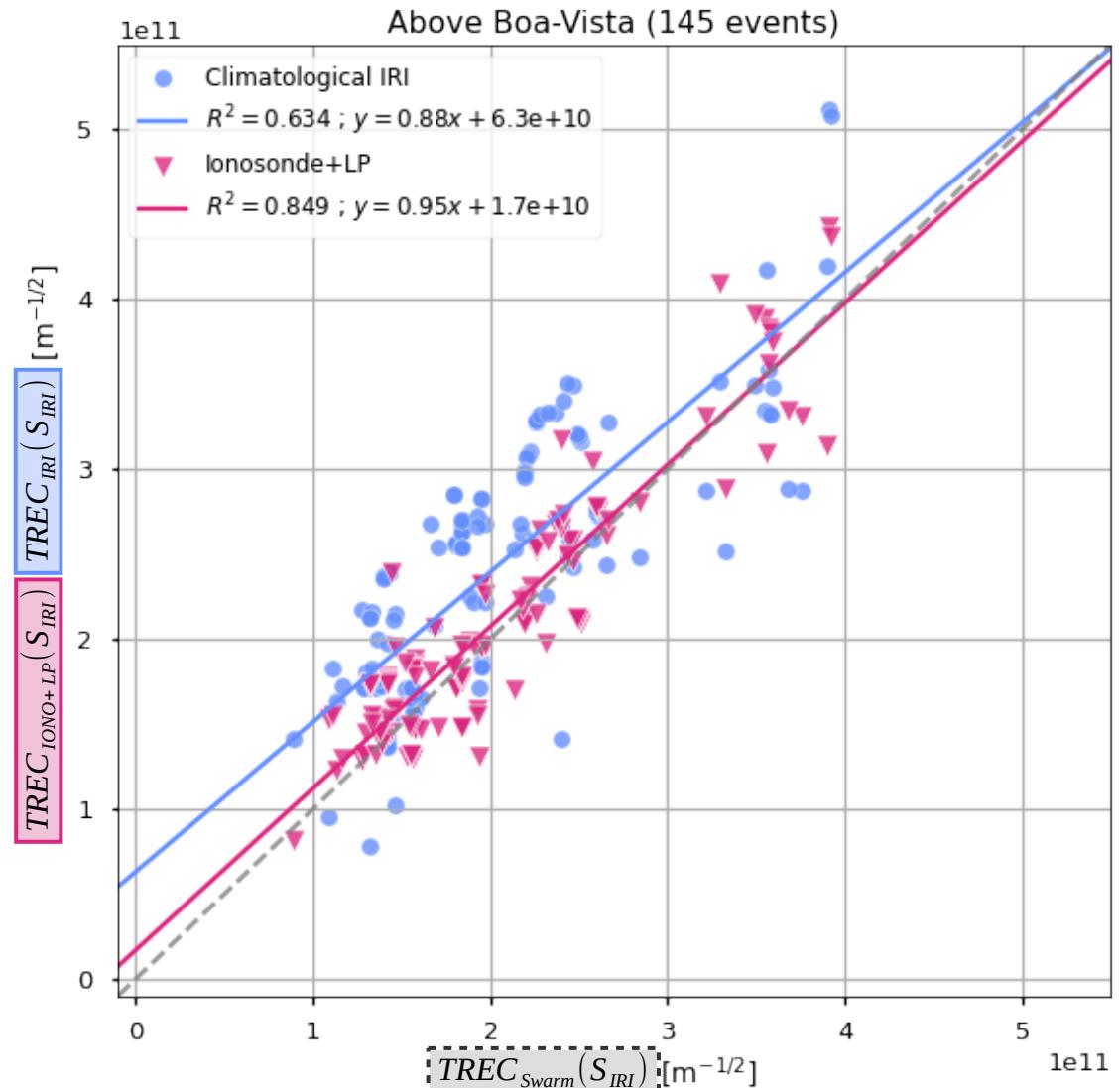
- Horizontal axis:** Calculation of the TREC using
- ΔT from Swarm's data
 - **γ and b coefficient** from the ray-tracing

$TREC_{IRI}(S_{IRI})$

- Vertical axis:** Direct integration of the **climatological IRI profile** along the climatological IRI ray-path
 → **climatological value**

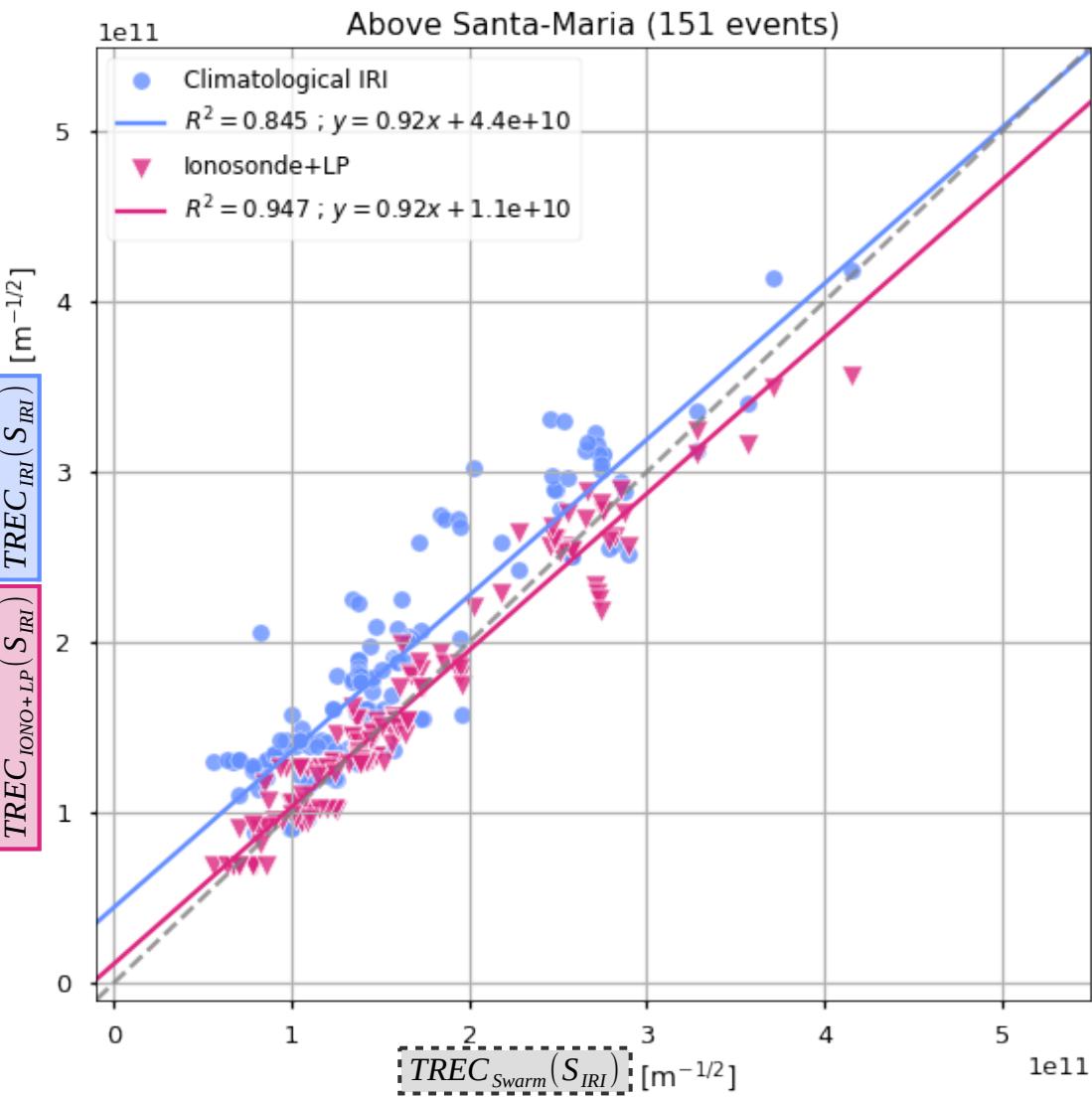
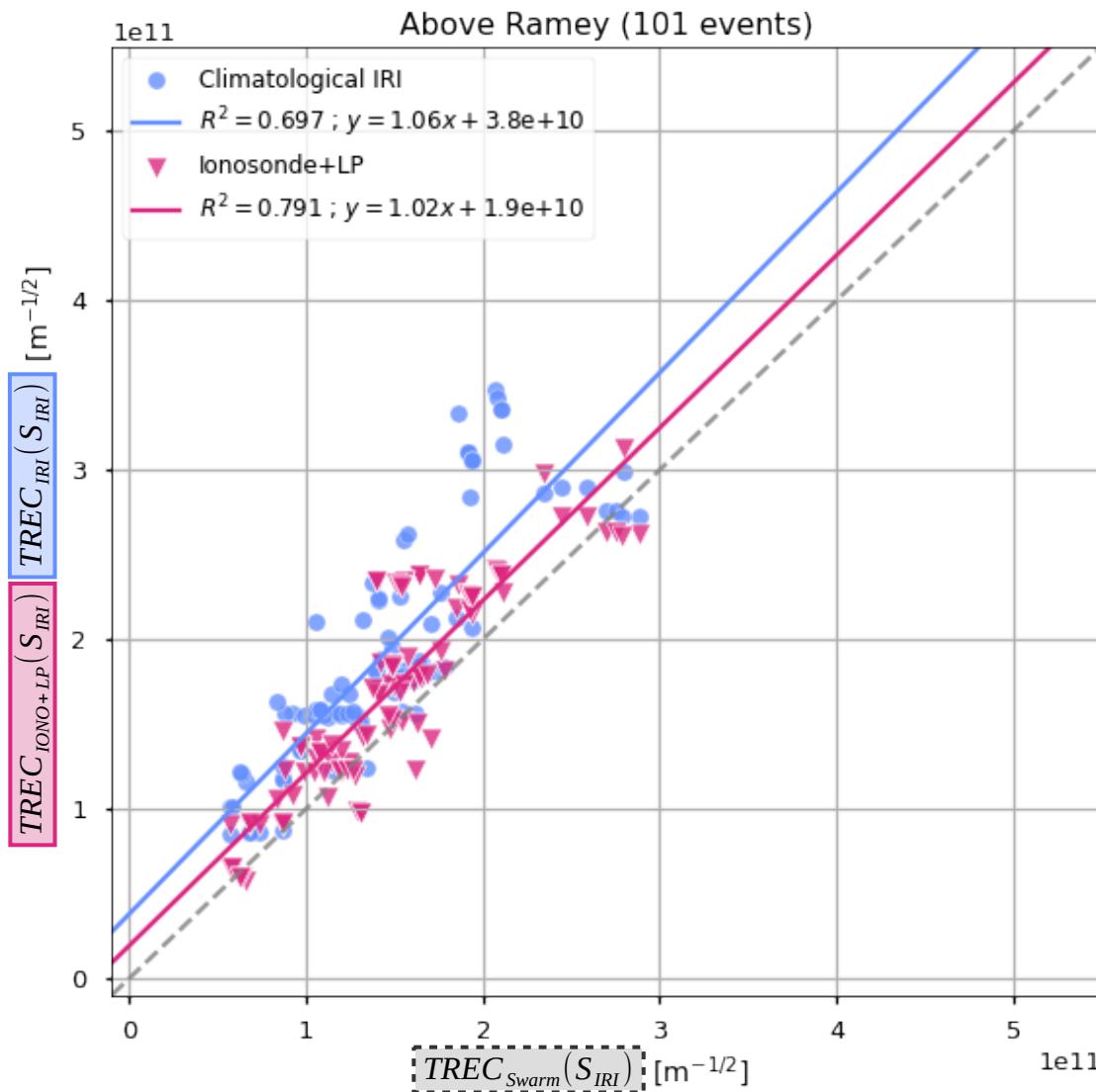
$TREC_{IONO+LP}(S_{IRI})$

- Vertical axis:** Direct integration of the **ionosonde profile corrected by the LP value** along the same climatological IRI ray-path
 → **ionosonde and LP observations**



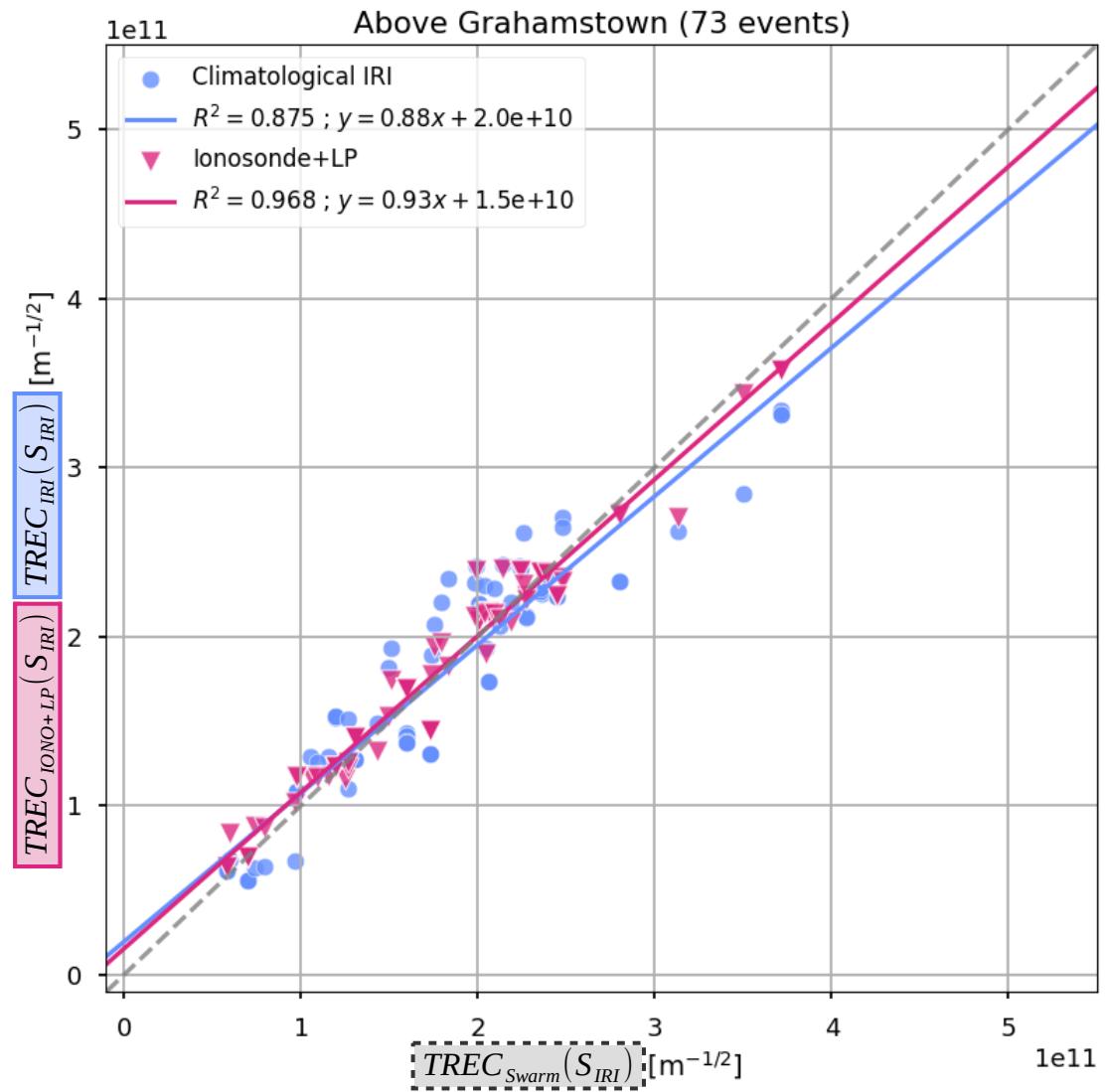
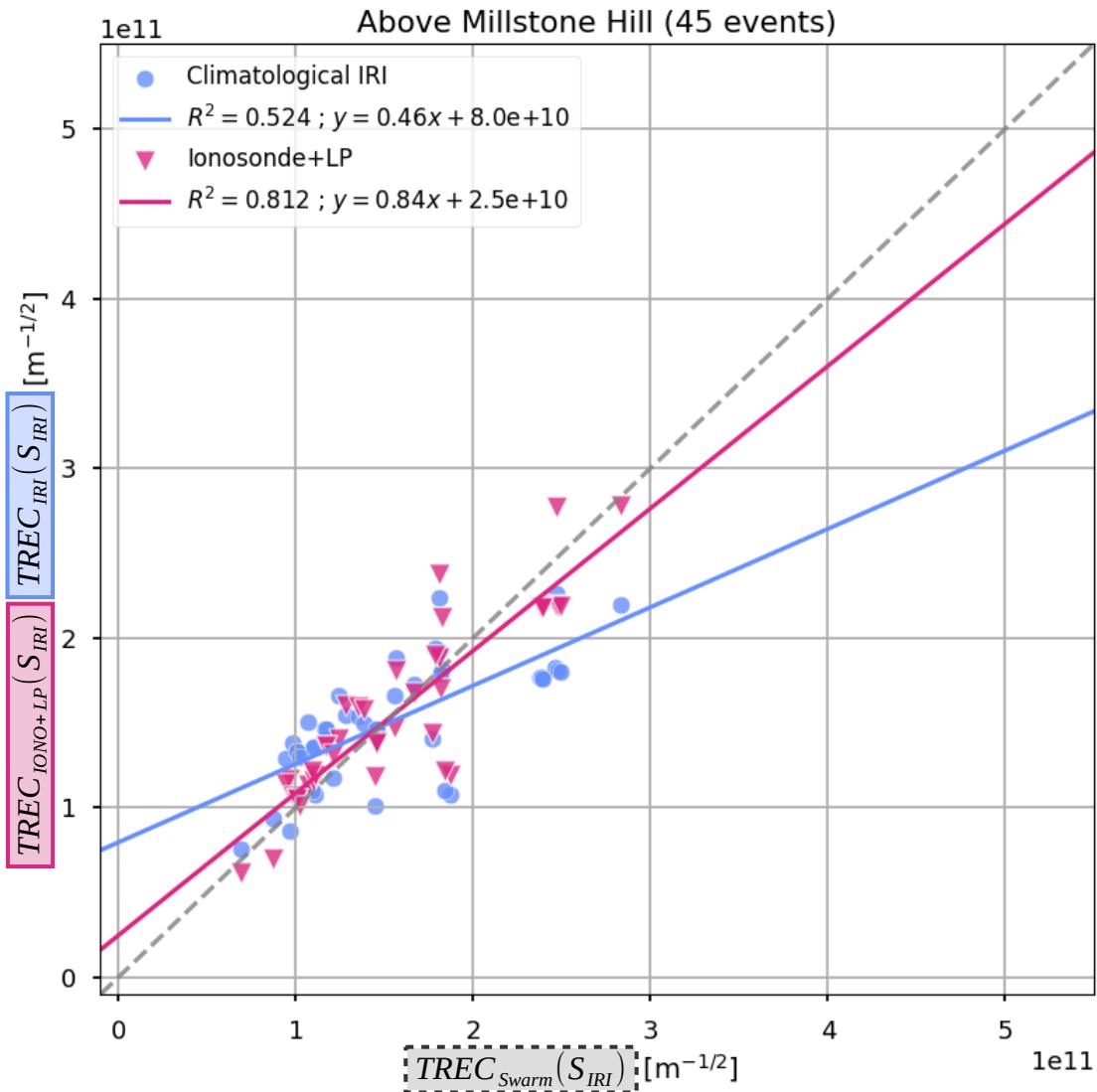


Ramey and Santa-Maria (low-latitude)





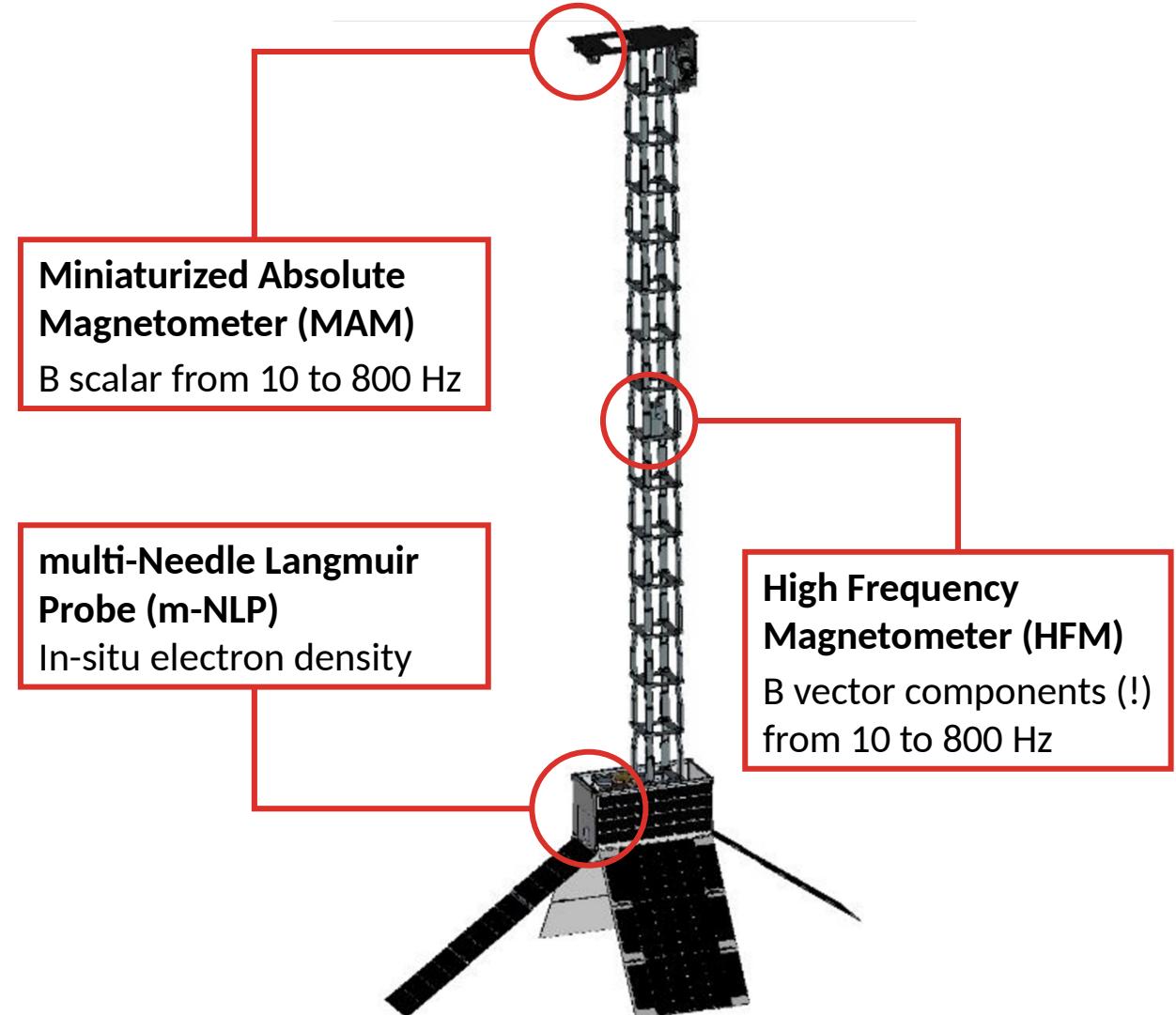
Millstone Hill and Grahamstown (mid-latitude)





Conclusions and perspectives

- The TREC is a new, valuable, measurement of the **ionization** state of the ionosphere
- Can be recovered from **ELF whistler** detection by Swarm
- Can be replicated on other missions e.g.:
 - **CSES** [poster of Qiao Wang],
 - **DEMETER**,
 - **NanoMagSat** (up to 800 Hz)



More informations: jenner@ipgp.fr

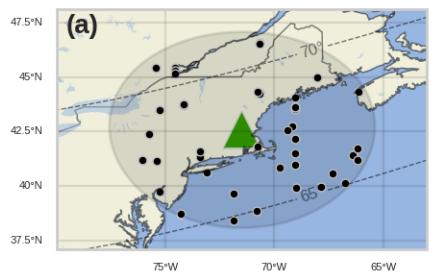
Thank you



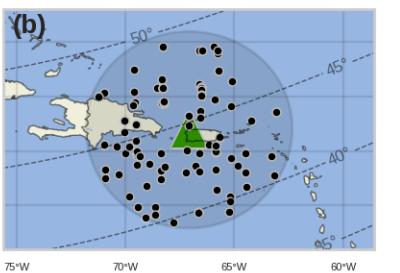
swarm



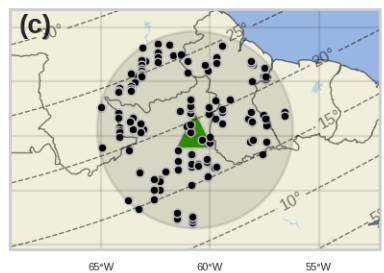
Millstone Hill
45 whistlers



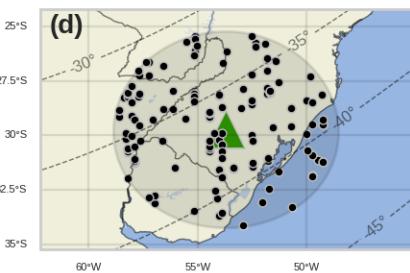
Ramey
101 whistlers



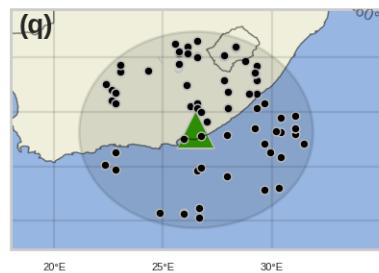
Boa Vista
145 whistlers



Santa Maria
151 whistlers



Grahamstown
73 whistlers



▲ Ionosonde station • Whistler location ■ Whistler selection area ----- Magnetic iso-inclination

