

# IMPACT EFFECTS CALCULATOR

<http://AsteroidHazard.pro>

SHOCK WAVE EFFECTS FROM IMPACTS OF  
COSMIC OBJECTS WITH DIAMETER FROM A  
FEW METERS TO 3KM

IAA PLANETARY DEFENSE  
CONFERENCE 2021  
26-30 APRIL 2021

## IDG RAS

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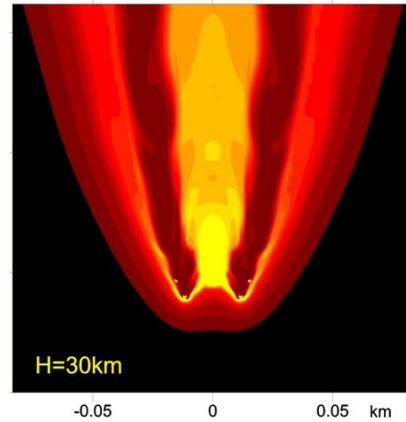
# Motivation

*Physical process*



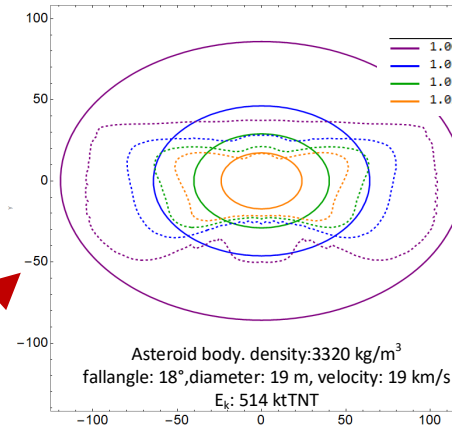
*impossible for a full – scale laboratory experiment*

*Modeling*



*slow calc*

*Scaling relations*



*quick calc*

*online calculator*

Projectile Parameters  
Diameter: 19 m  
Density: 3320 kg/m<sup>3</sup>

Impact Parameters  
Velocity: 19.2 km/s  
Entry Angle: 18.3°

<http://www.AsteroidHazard.pro>

BASIC

Projectile Parameters

Diameter, m: 19

Density, kg/m<sup>3</sup>: 3320

Impact Parameters

Velocity, km/s: 19.2

Entry Angle, °: 18.3

Point of Effect

Distance to the point of intersection of the trajectory with the Earth's surface, km: 100.05

Angle to Trajectory, °: 89.95

*easy to use*



\*\*\*

The main motivation is to create a quick and accurate tool for assessing the consequences of the impact of a cosmic body.

# Quasi-liquid meteoroid model

## Basis:

large meteoroid deformation begins at  $h$ , where aerodynamical loading  $\gg$  strength

## Main assumptions

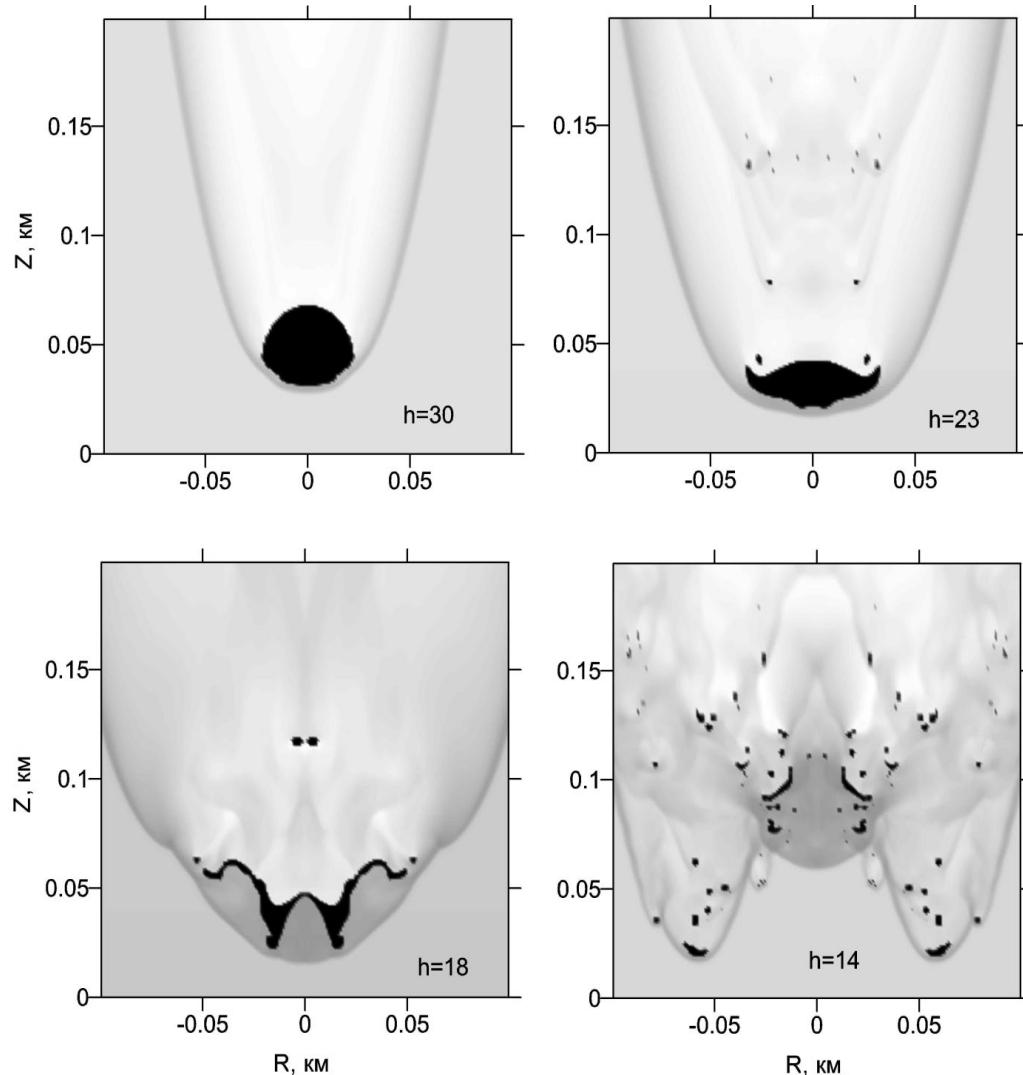
- ❖ Zero strength
- ❖ Ablation as evaporation
- ❖ Radiation transfer in thermal conductivity approximation

## Formal range

$D > 30-50$  m;  $h < 40$  km (Svetsov et al. 1993)

## Restrictions:

quasi-liquid assumption



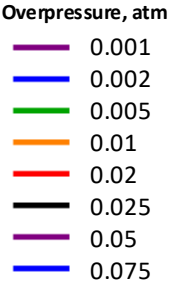
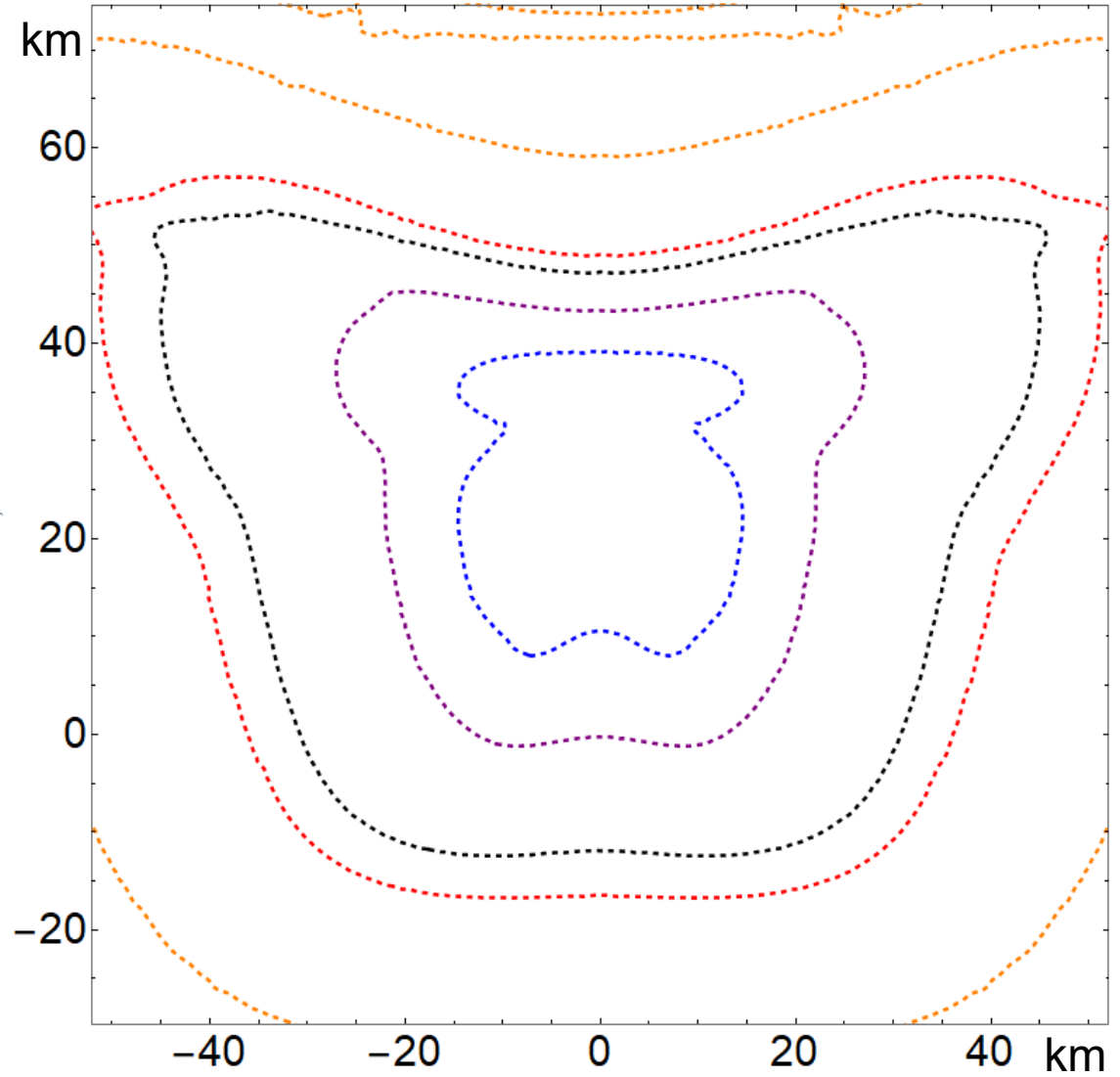
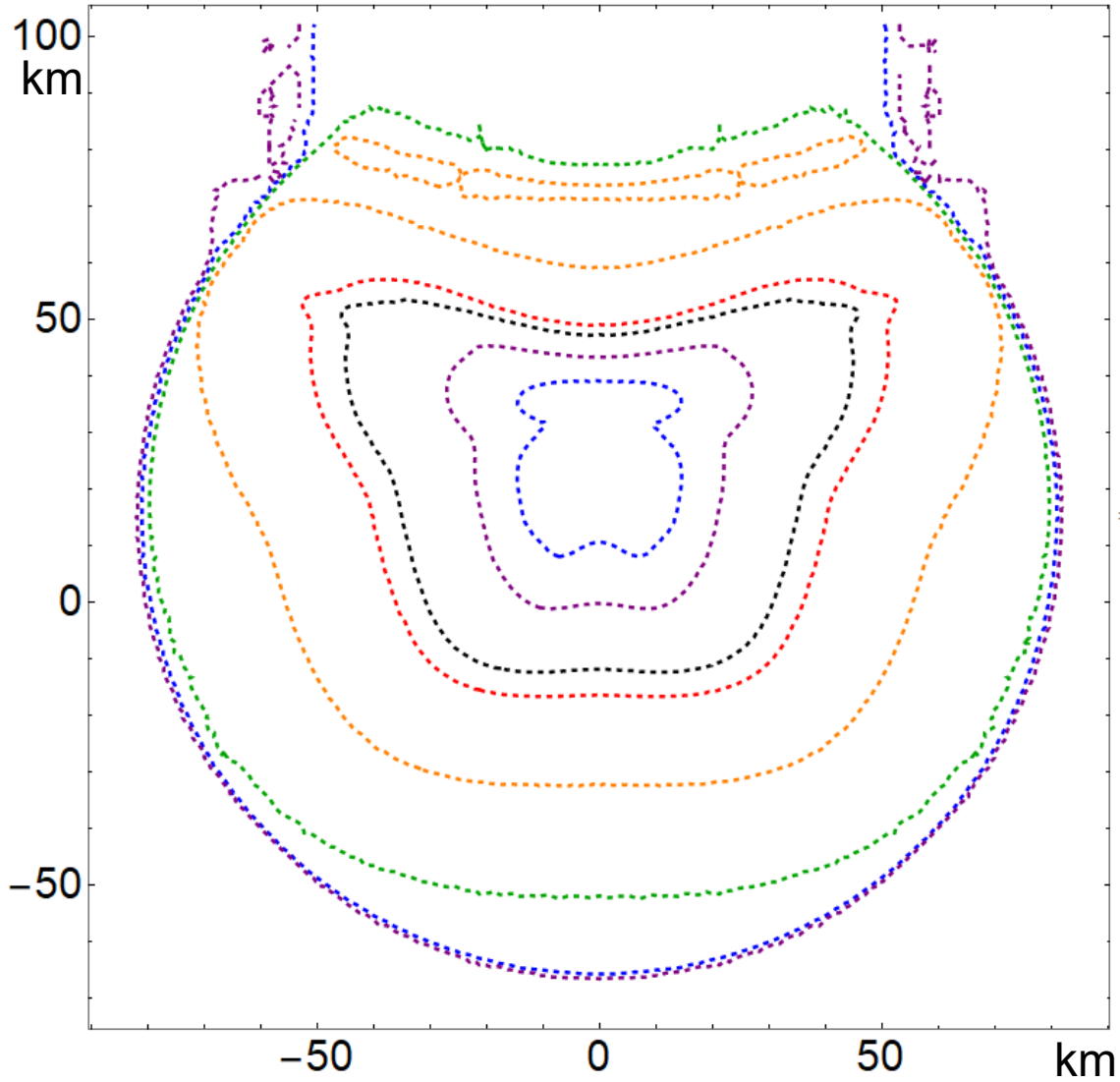
Relative density distribution along trajectory at different altitudes  $h$   
 $D=40$  m,  $V=18$  km/s; chondritic material ( $2650$  kg/m<sup>3</sup>),  $\alpha=90^\circ$   
Black – solid meteoroid material

Quasi-liquid model= QL model

# D-30-45-20

density: 3320 kg/m<sup>3</sup>  
diameter: 30 m

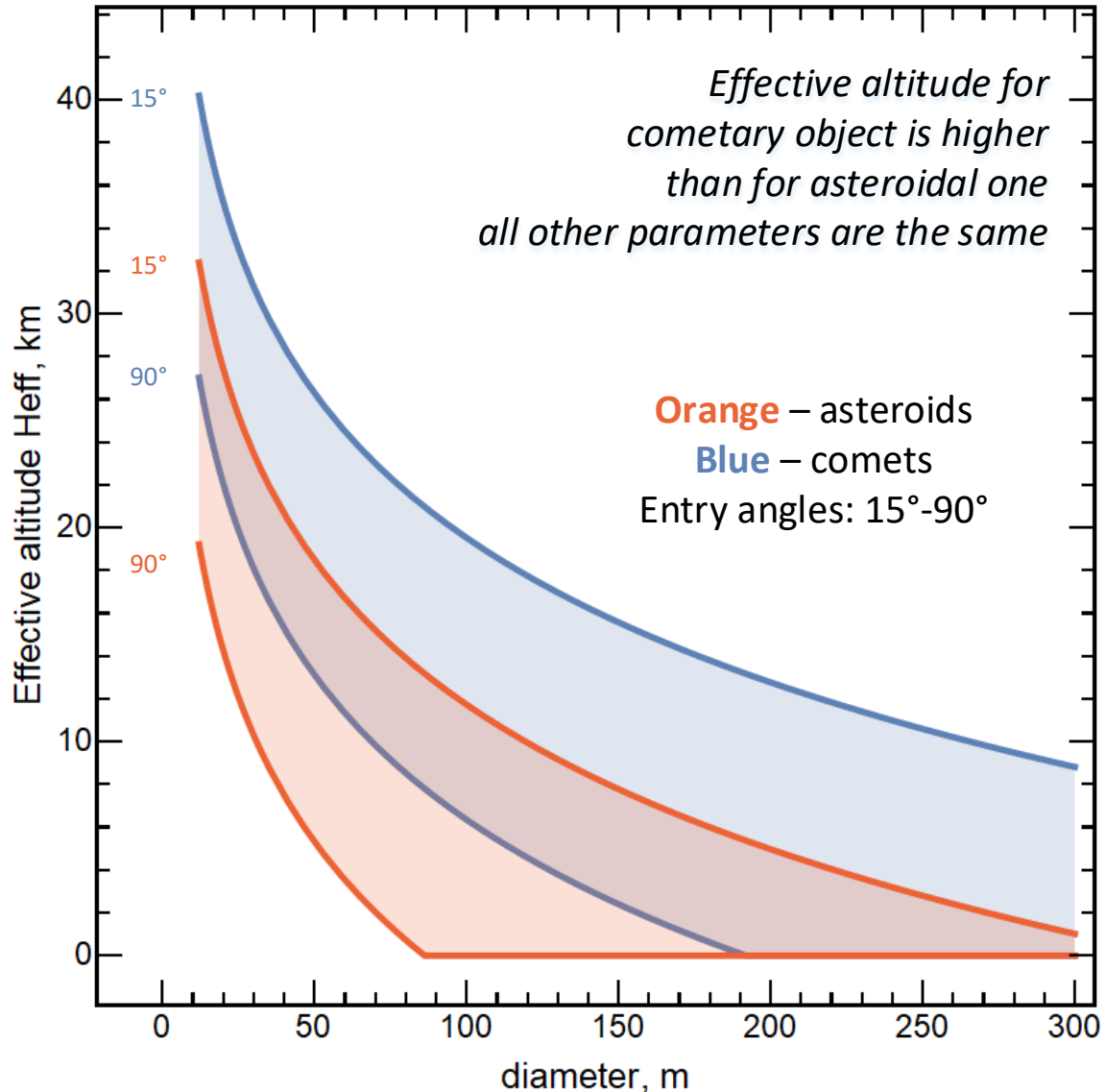
entry angle: 45°  
velocity: 20 km/s



Overpressure distribution obtained for one variant



# Effective airburst altitude



Effective altitude dependence on meteoroid size

$$H_{eff} = (-1.3 * H * \ln(D * (\sin[\alpha]/H) * (\rho/\rho_0)^{2/3}) + H) / 1000$$

For quick rough evaluation of the impact consequences (levels of damage, area of the damage, etc) at large distances from the ground zero spherical source - reasonable SW evaluation if the altitude  $H_{eff}$  of E-equivalent point explosion is correctly determined

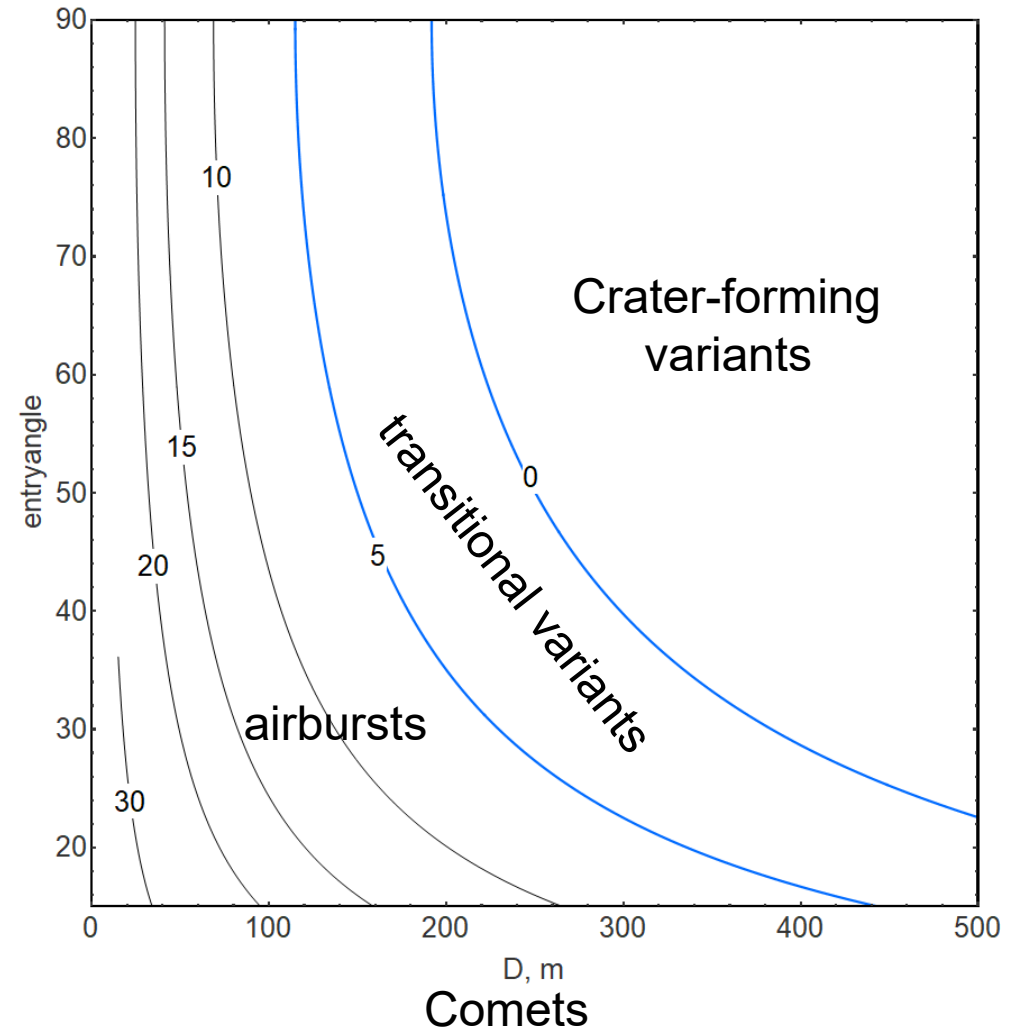
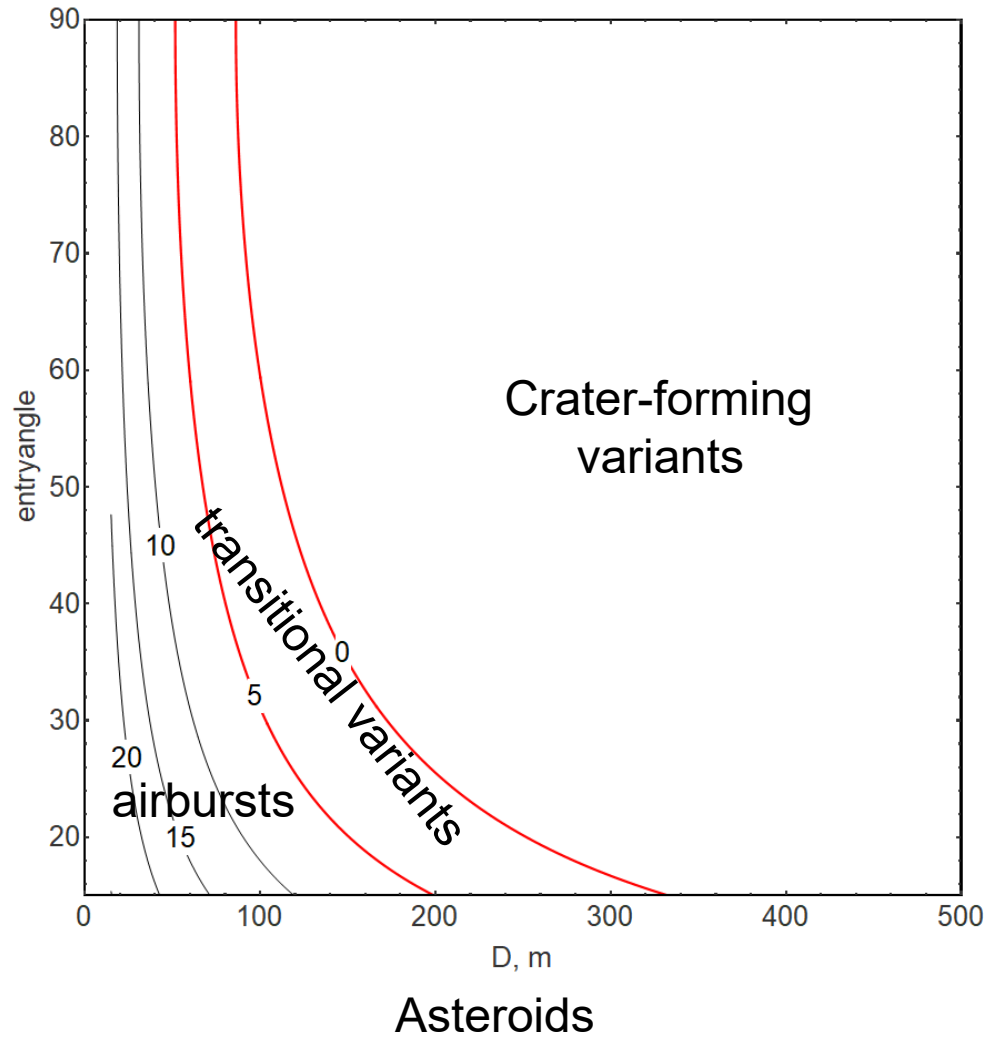
QL model was used to determine  $H_{eff} = f(D, \text{density}, \alpha)$  (Shuvalov et al. 2016)

This approach:

- Precision of estimates - 2-3 km (random character of disruption)
- Is applicable for  $D > 10-30$  m
- for  $D \sim 10-30$  m the uncertainty in effective altitude may reach 10-15 km (Chelyabinsk, TC<sub>3</sub>2008 and other cases)
- (strength, fragmentation features etc)

*Determination of the height of the "meteoric explosion"*  
 Shuvalov et al. Solar System Research 2016, V.50, I.1, pp 1-12

# Effective airburst altitude – uncertainty area



$$H_{eff} = (-1.3 * H * \text{Ln}(D * (\text{Sin}[\alpha]/H) * (\rho/\rho_0)^{2/3}) + H)/1000$$

# Scaling relation for overpressure

$$\Delta p = el * m * \left( \frac{E_k^{1/3}}{H_{eff}^2 + x^2 + y^2} \right)^{pow}$$

$x, y$  – spatial coordinates

$el$  – ellipticity parameter,

$E_k$  – kinetic energy of the impactor in kt TNT,

$H_{eff}$  – effective height of point source,

$\phi$  –  $\arctan(y/x)$ .

## Airburst

$$pow = 1.5$$

$$m = const$$

$$H_{eff} = function(\rho, D, \alpha)$$

$$el = el(\phi, n_{ab}, b_{ab}, f_{ab})$$

$$n_{ab} = fuction(\rho, D, \alpha, V)$$

$$b_{ab} = fuction(\rho, D, \alpha, V)$$

$$f_{ab} = fuction(\rho, D, \alpha, V)$$

## Crater-forming

$$pow = 1.4$$

$$m = function(E_k)$$

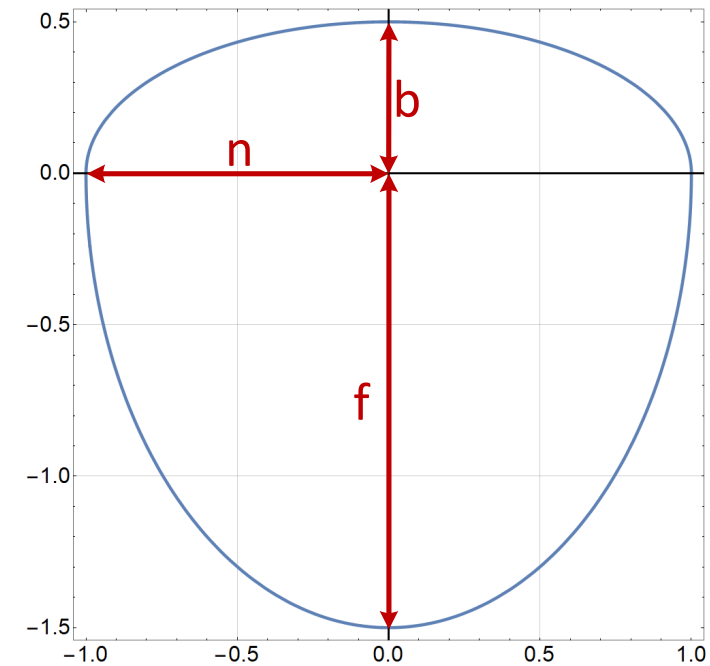
$$H_{eff} = 0$$

$$el = el(\phi, n_{cf}, b_{cf}, f_{cf})$$

$$n_{cf} = fuction(\rho, D, \alpha, V)$$

$$b_{cf} = fuction(\rho, D, \alpha, V)$$

$$f_{cf} = fuction(\rho, D, \alpha, V)$$



the spatial heterogeneity

$$el(\phi, \dots) = \begin{cases} \frac{n * b}{\sqrt{n^2 \sin^2[\phi] + b^2 \cos^2[\phi]}}, & 0 \leq \phi < \pi \\ \frac{n * f}{\sqrt{n^2 \sin^2[\phi] + f^2 \cos^2[\phi]}}, & -\pi \leq \phi < 0 \end{cases}$$

Wind speed:

$$V_{max} = \frac{330}{\gamma} * (p/p_0 - 1) * \left( 1 + \frac{\gamma + 1}{2 * \gamma} * (p/p_0 - 1) \right)^{-1/2}$$

$\gamma$  - adiabatic index

$$v_{max} = \begin{cases} \frac{67.1 * E_k^{0.38}}{H_{eff}^{1.53}}, & \rho = 1000 \text{ kg/m}^3 \\ \frac{40.51 * E_k^{0.39}}{H_{eff}^{1.45}}, & \rho = 3320 \text{ kg/m}^3 \end{cases}$$

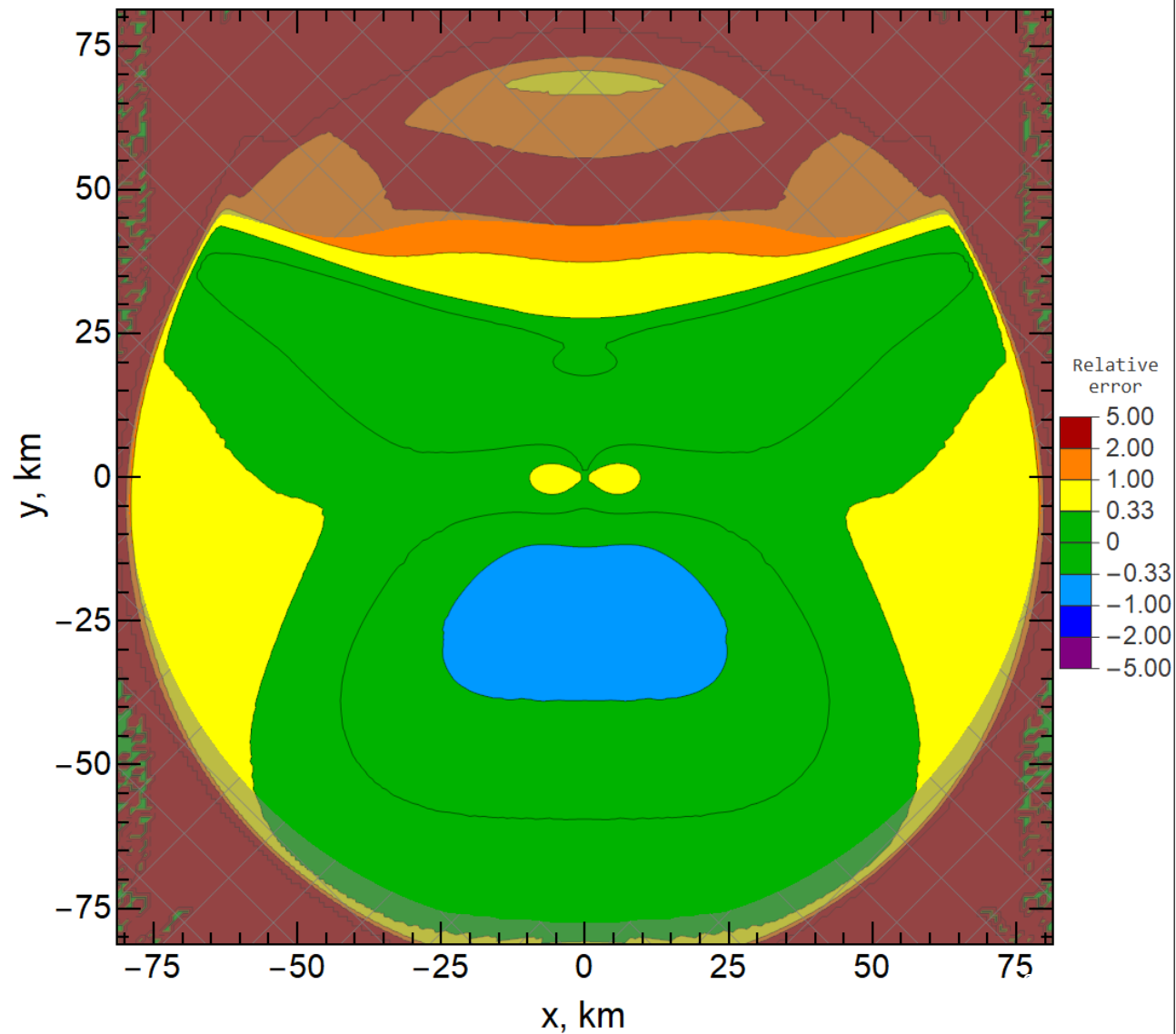
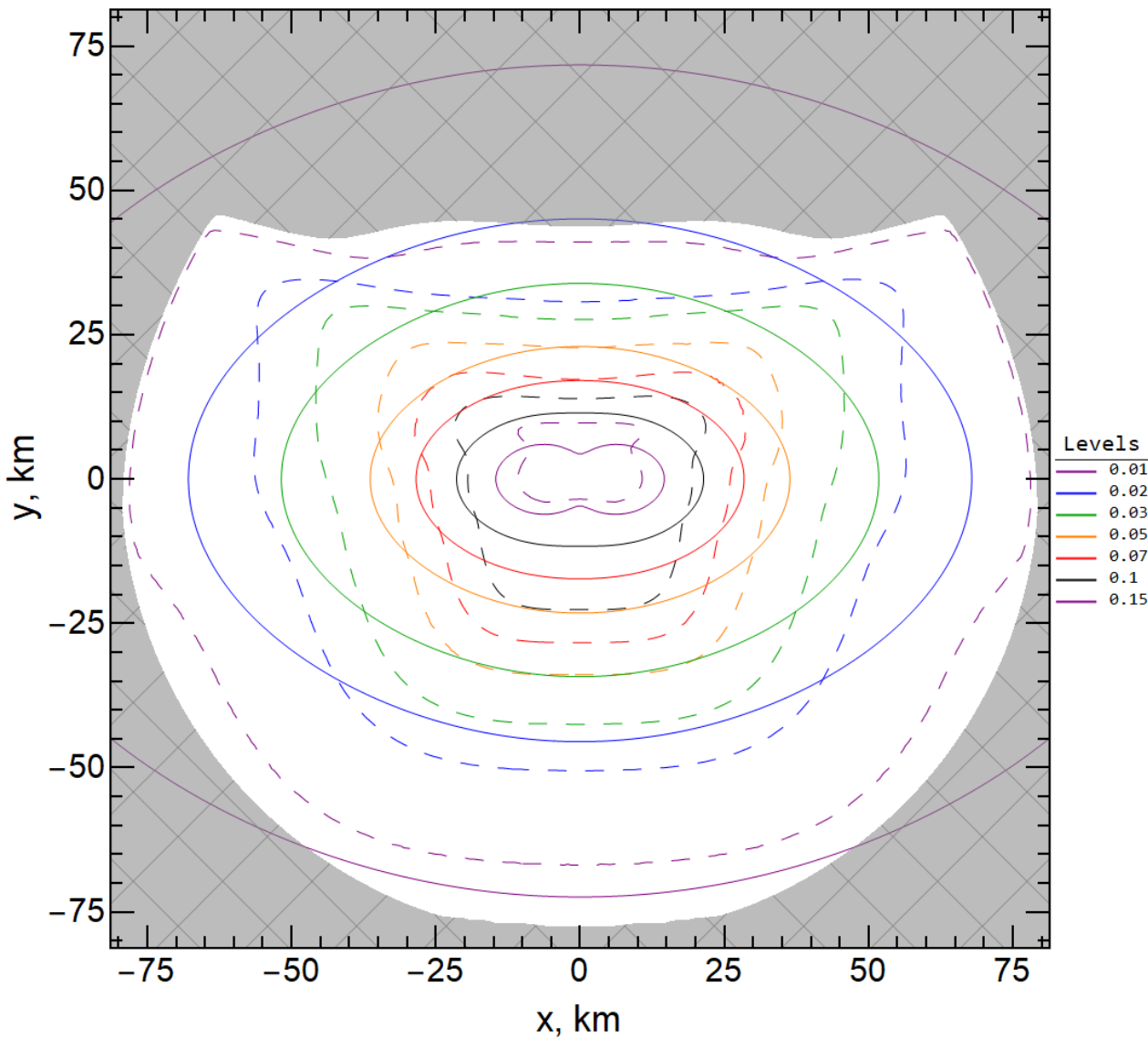


# Overpressure field with model and errors

Plot №17, D:50 m,  $\alpha:30^\circ$ , V:15 km/s,  $\rho:3320$  kg/m<sup>3</sup>, E:5.8 Mt TNT

a 5.8  
hetl 1.2  
hetp 0.66  
hetn 0.67

	ErrorValue	Mean	Median	StandardDeviation
Relative squared error	0.39	0.15	0.061	0.26
Abs squared log error	0.14	0.019	0.011	0.024



# Results comparison

Our scaling relations  
<http://AsteroidHazard.pro>

## D-50-30-15

density: 3320 kg/m<sup>3</sup>

diameter: 50 m

fall angle: 30°

velocity: 15 km/s

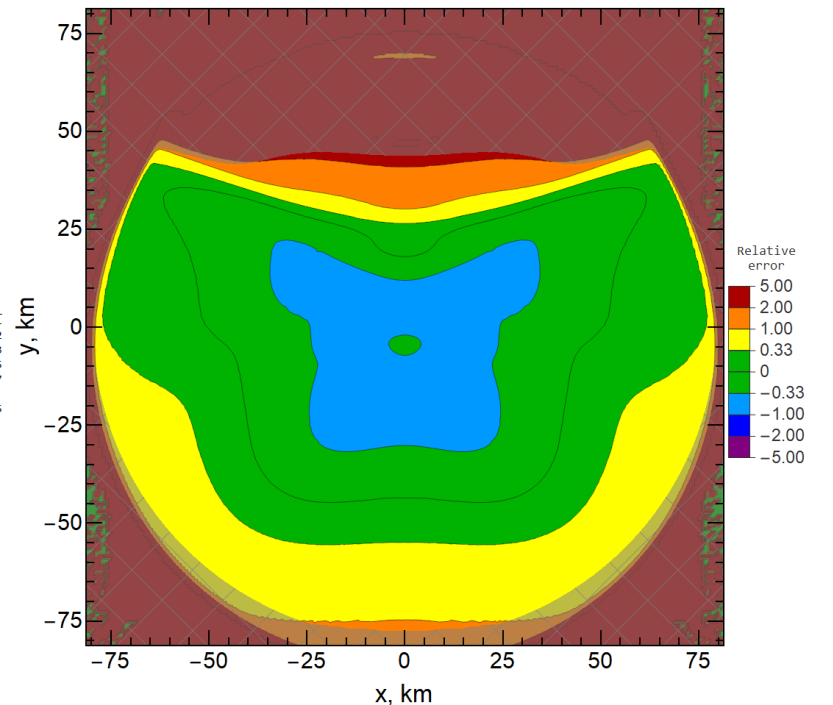
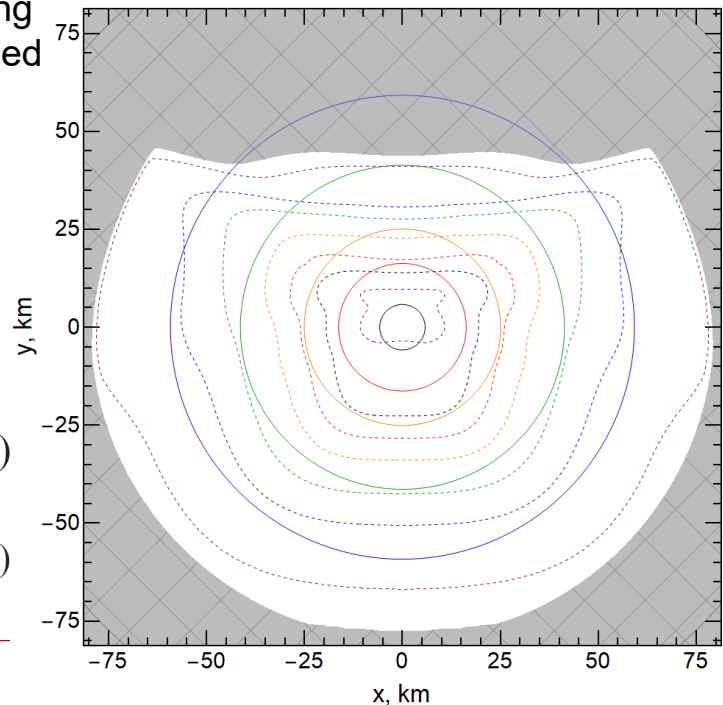
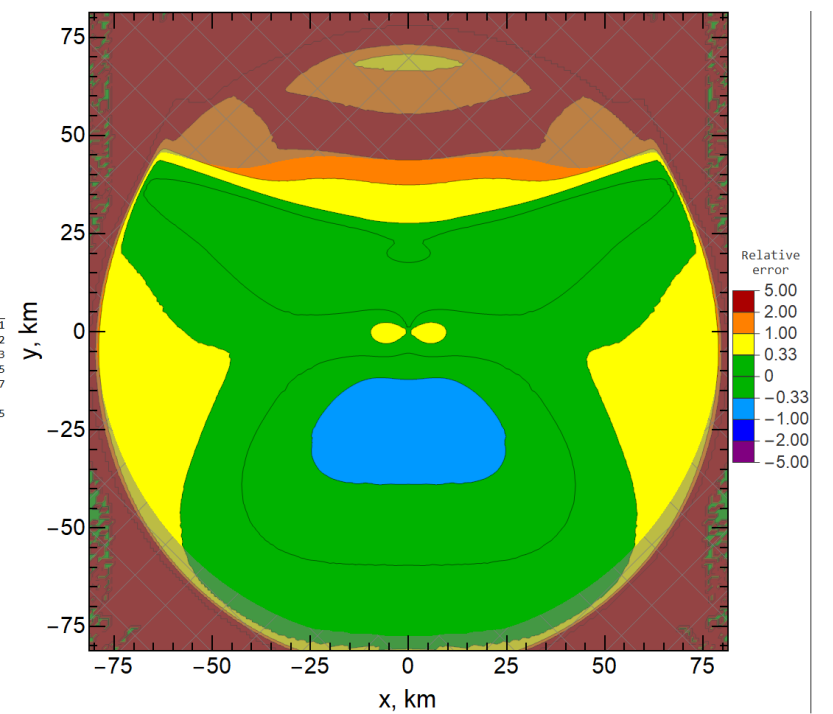
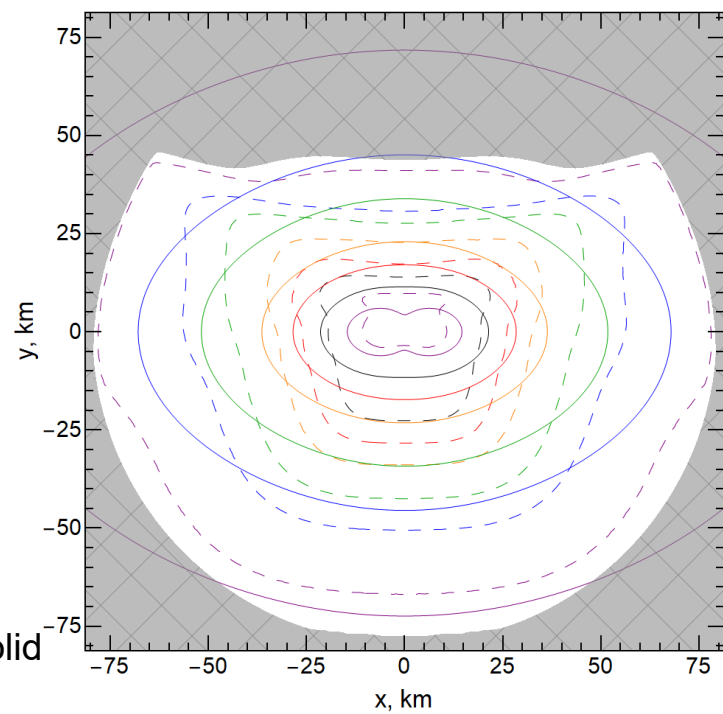
Collins et al. 2017

$$p(r) = 3.14 \times 10^{11} (r^2 + z_b^2)^{-2.6/2} + 1.8 \times 10^7 (r^2 + z_b^2)^{-1.13/2} \quad (7)$$

$$z_{b,50\%} = 25.7 - 7.83 \log_{10} E_{Mt} - 0.31 (\log_{10} E_{Mt})^2 \quad (6b)$$

Scalings-solid

Numerical modeling data - dashed



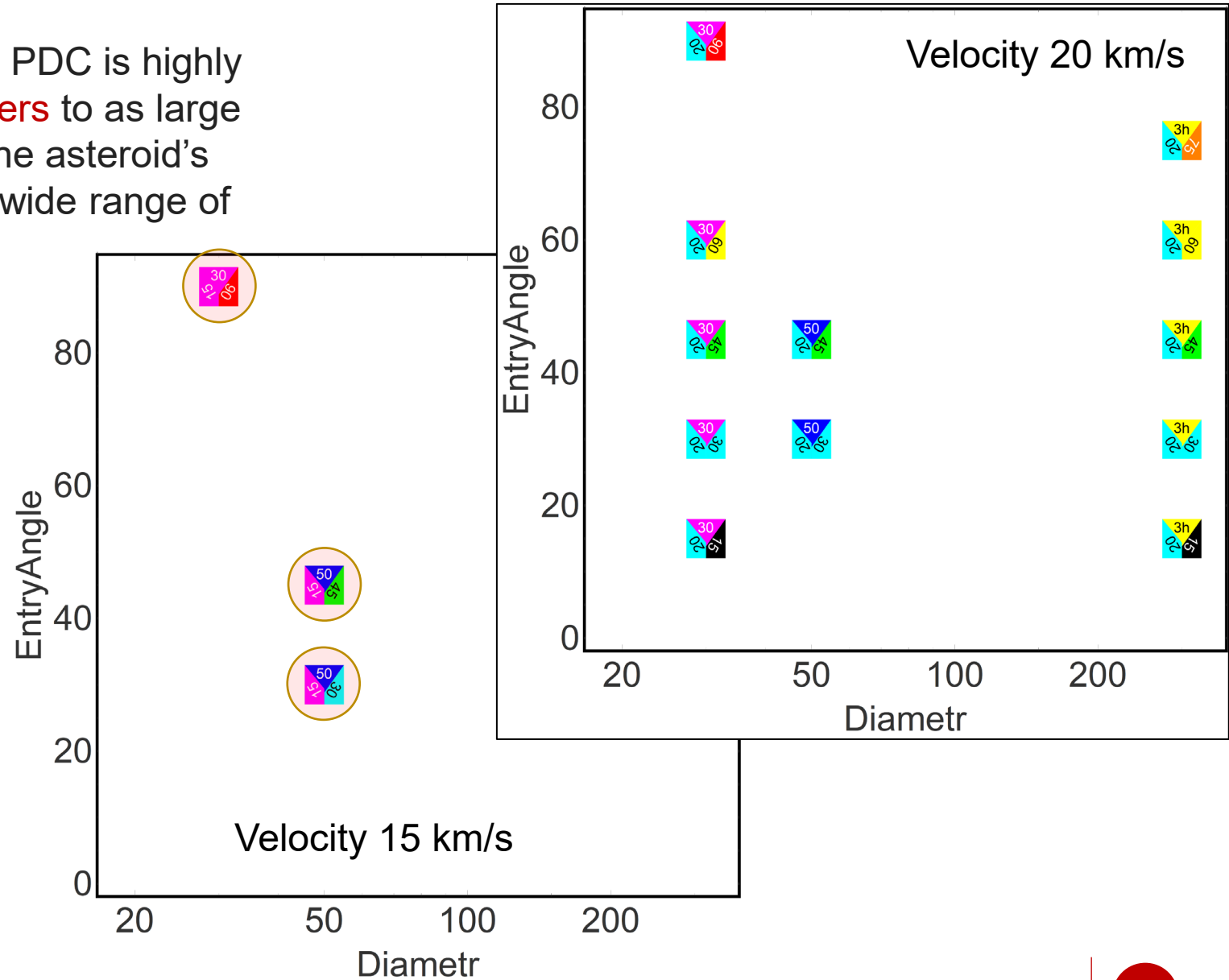
# Modeled variants in 2021 PDC exercise

«As mentioned previously, the size of 2021 PDC is highly uncertain, ranging from as small as **35 meters** to as large as **700 meters**. This estimate is based on the asteroid's brightness, its estimated distance, and the wide range of possible albedos (reflectivities).

Little is known about other properties of the object, such as composition and density. As a result, the potential impact damage and population risk is also highly uncertain. Based on these estimates, the possible **energy released** on impact could range from **1.2 Mt** to **13 Gt (TNT equivalent)**.

Velocity from 15.12 to 15.87 km/s

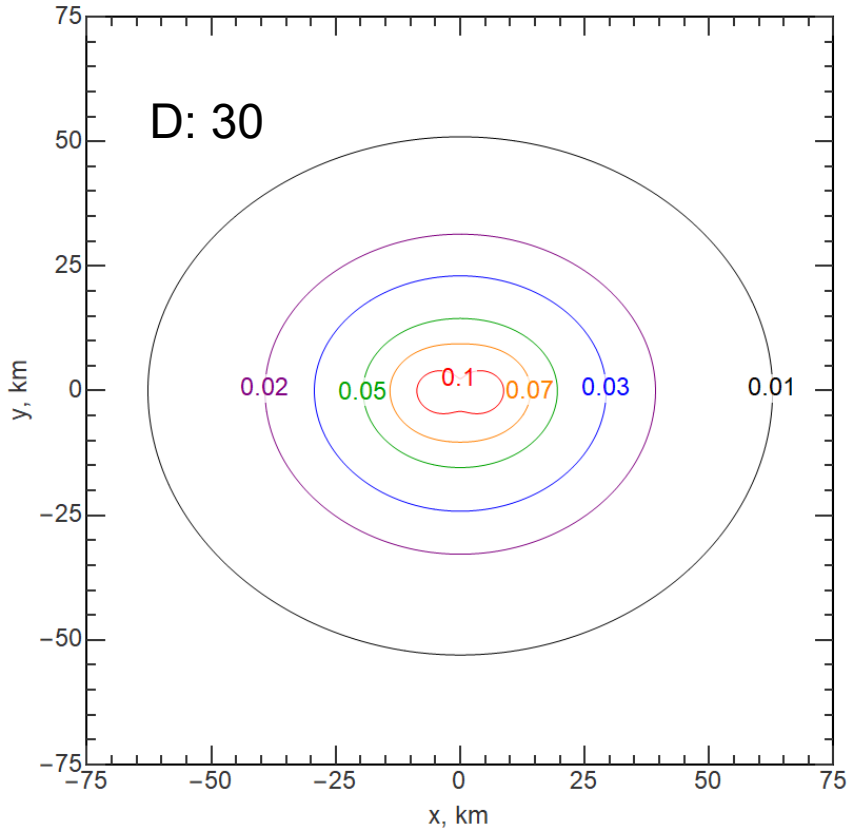
Entry angle from 0 to 90°



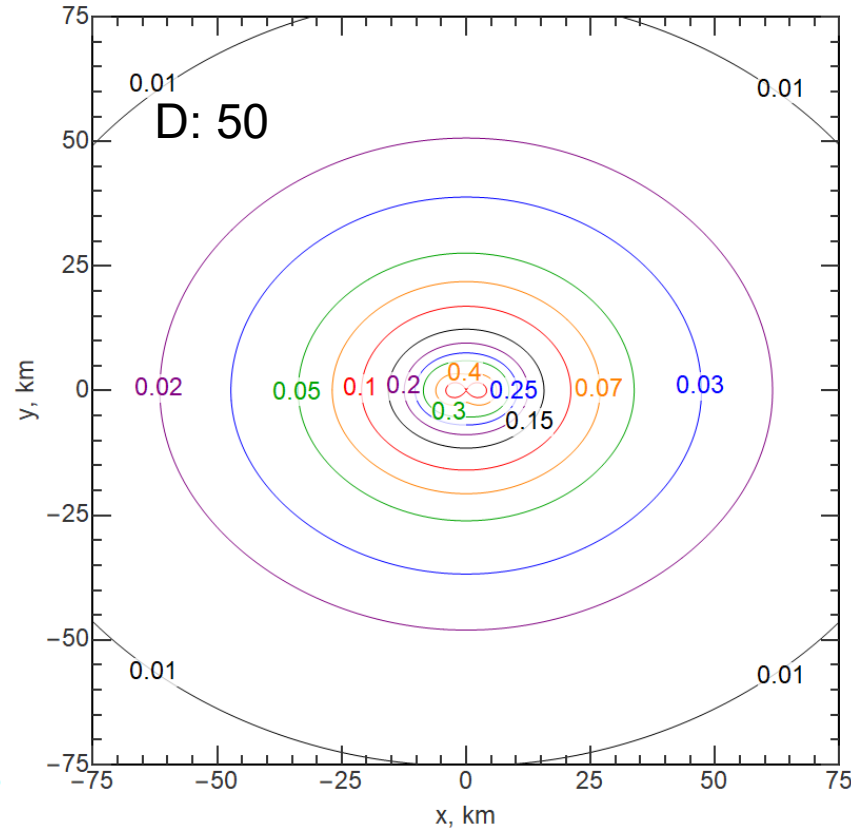
# Scaling relation for different diameters

density: 3320 kg/m<sup>3</sup>  
diameter: various  
fall angle: 60°  
velocity: 15 km/s

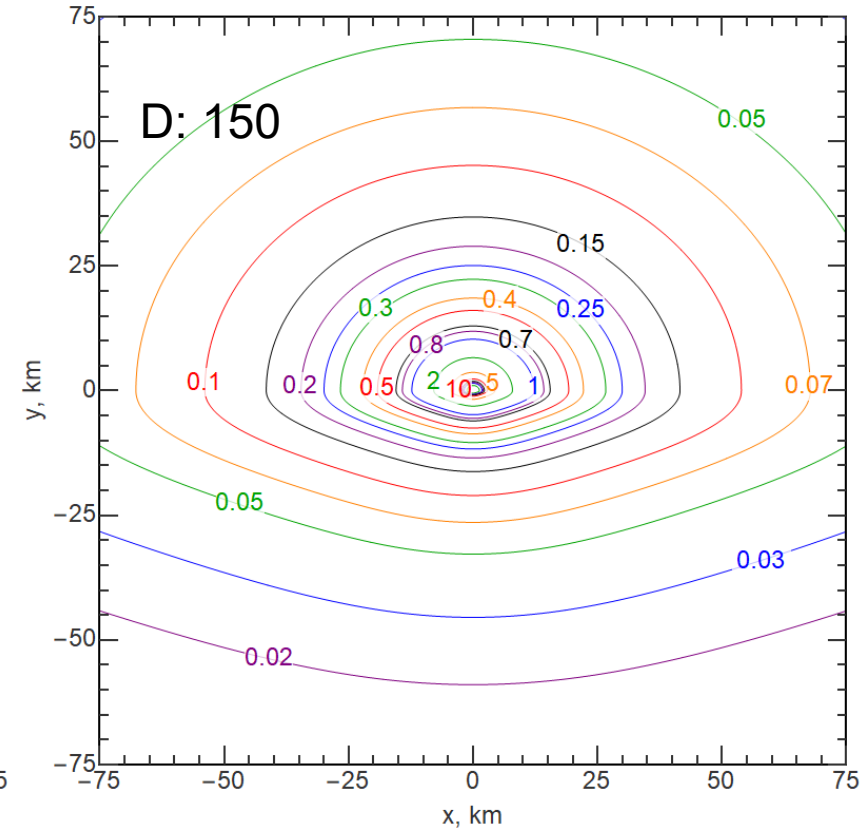
D:30 m,  $\alpha:60^\circ$ , V:15 km/s,  $\rho:3320 \text{ kg/m}^3$ , E:1.3 Mt TNT



D:50 m,  $\alpha:60^\circ$ , V:15 km/s,  $\rho:3320 \text{ kg/m}^3$ , E:5.8 Mt TNT



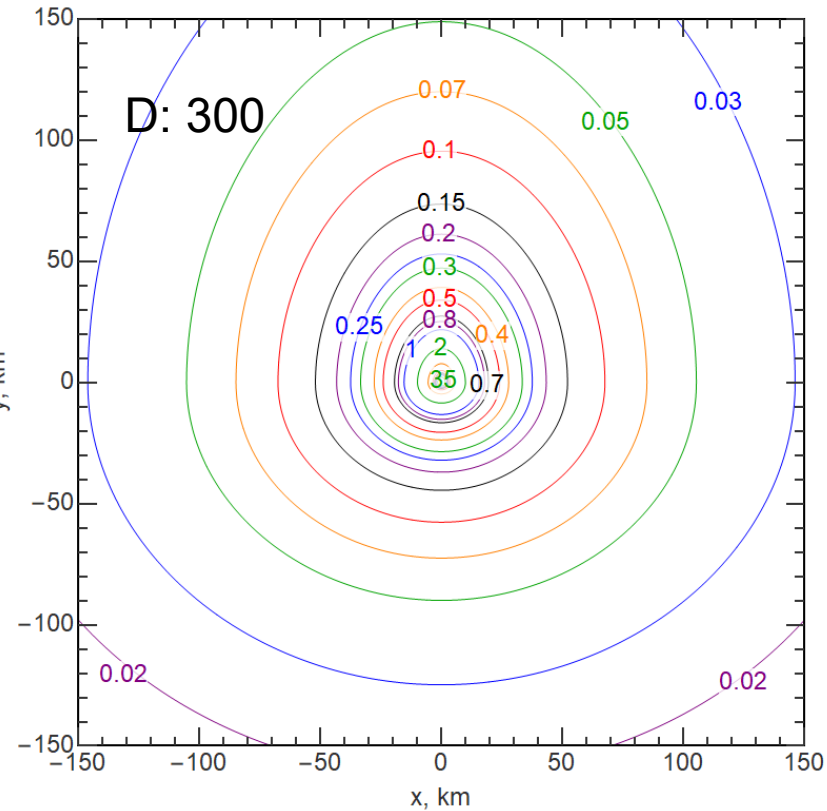
D:150 m,  $\alpha:60^\circ$ , V:15 km/s,  $\rho:3320 \text{ kg/m}^3$ , E:160 Mt TNT



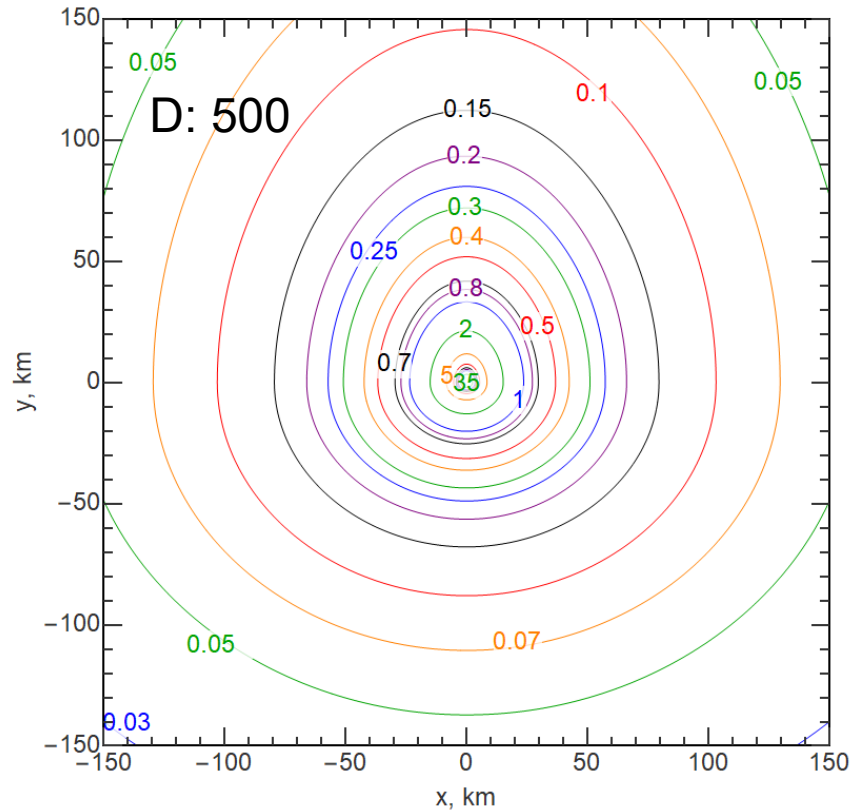
# Scaling relation for different diameters

density: 3320 kg/m<sup>3</sup>  
diameter: various  
fall angle: 60°  
velocity: 15 km/s

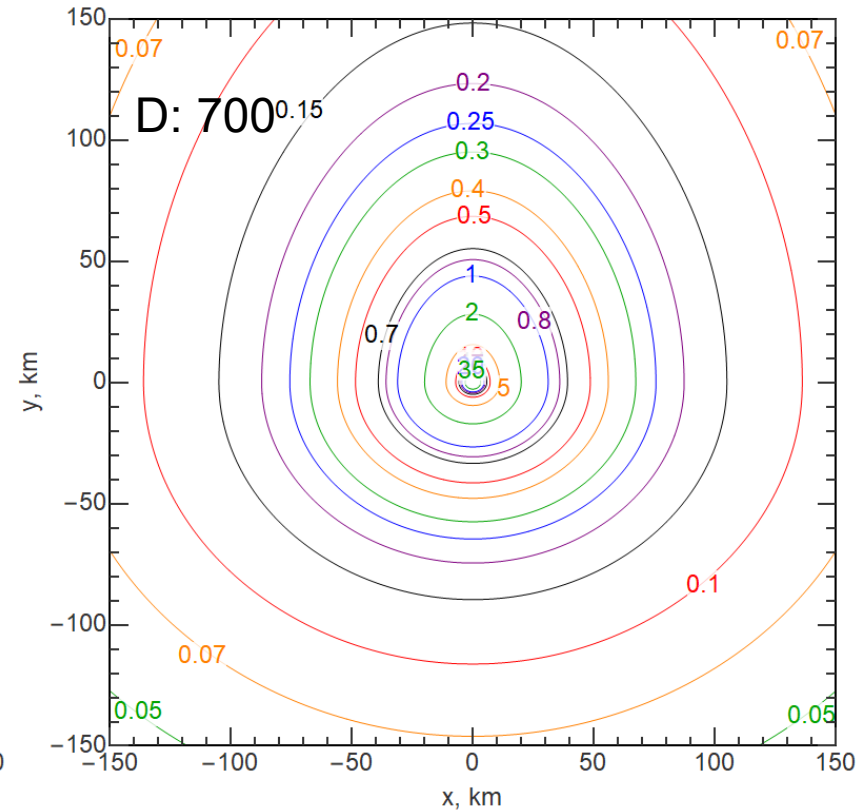
D:300 m,  $\alpha:60^\circ$ , V:15 km/s,  $\rho:3320 \text{ kg/m}^3$ , E:1.3 Gt TNT



D:500 m,  $\alpha:60^\circ$ , V:15 km/s,  $\rho:3320 \text{ kg/m}^3$ , E:5.8 Gt TNT

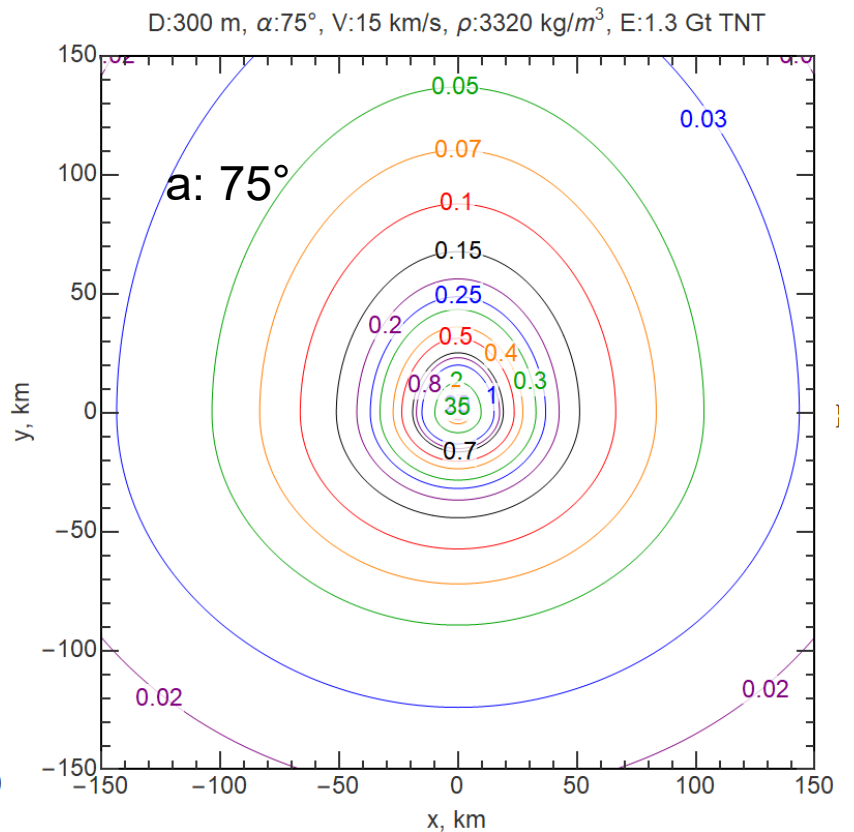
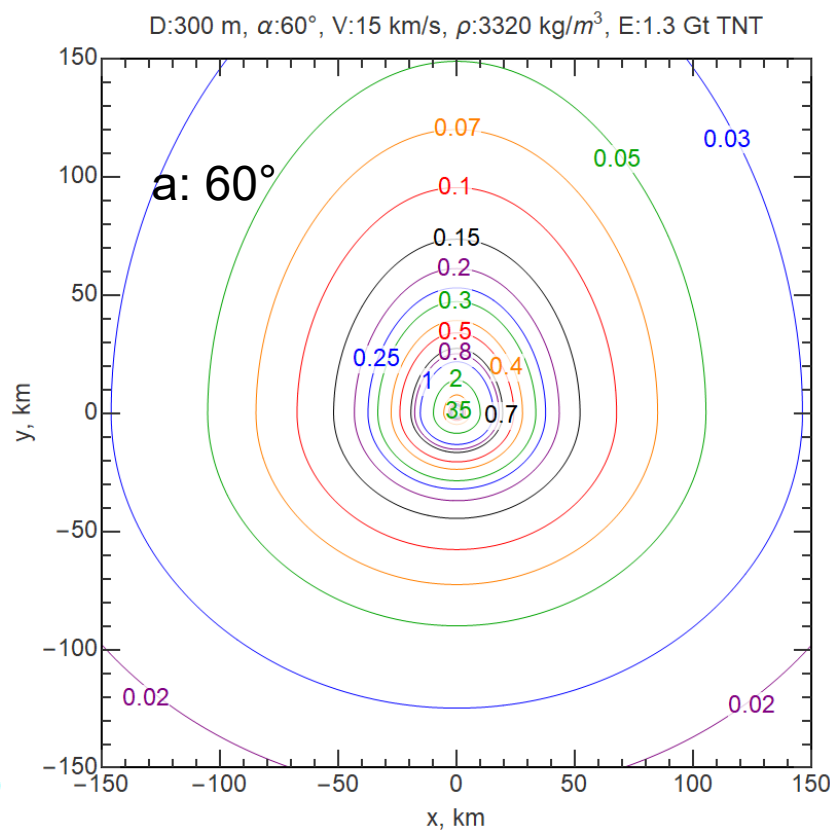
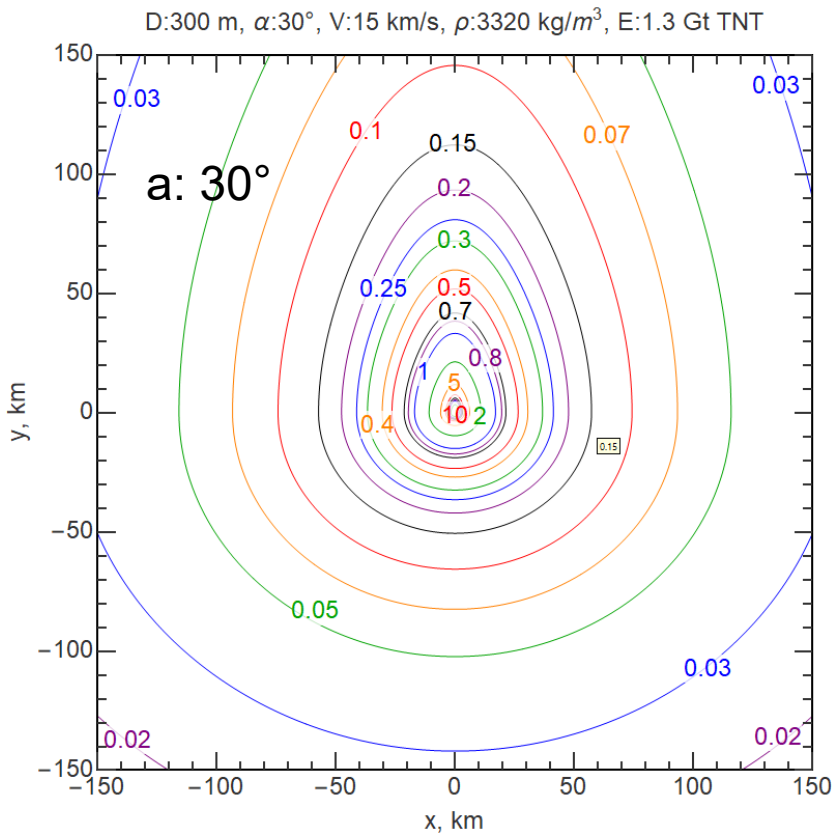


D:700 m,  $\alpha:60^\circ$ , V:15 km/s,  $\rho:3320 \text{ kg/m}^3$ , E:16 Gt TNT

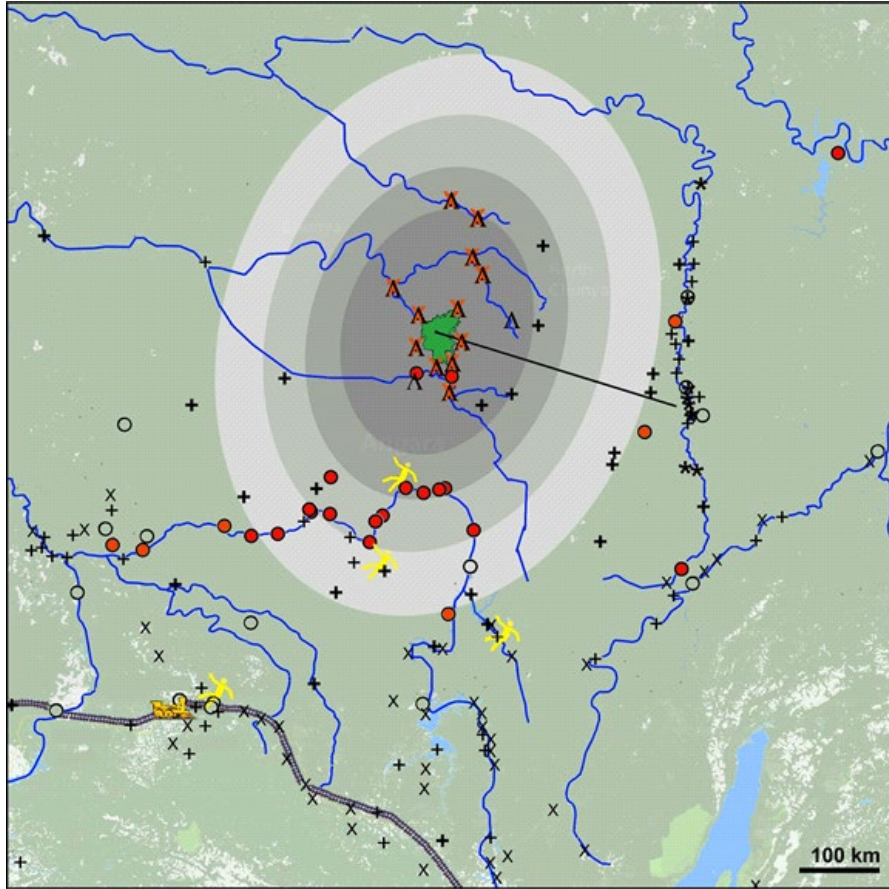


# Scaling relation for different entry angles

density: 3320 kg/m<sup>3</sup>  
diameter: 300 m  
fall angle: various  
velocity: 15 km/s



# Tunguska and Chelyabinsk events



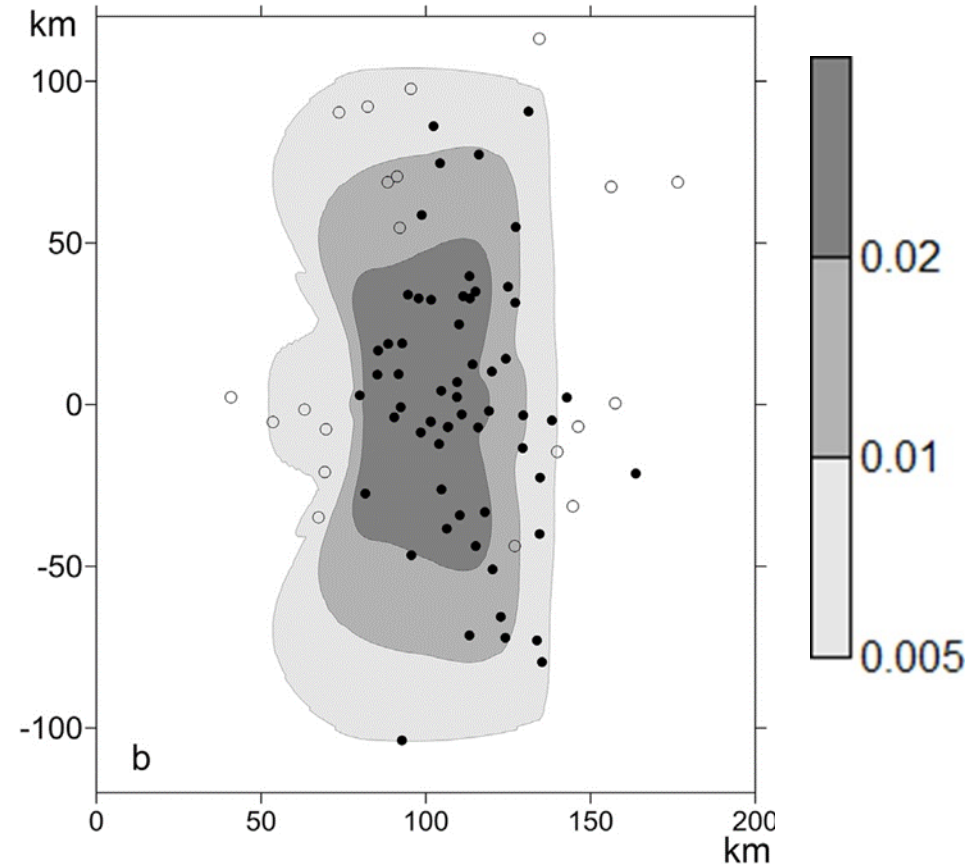
Location map of eyewitness reports. .

Glass damage (filled red circle); glass rattled, not broken (o); chum destruction ( $\Delta$ ); heat and unconsciousness (orange X); people falling (person symbol).

Gray areas -  $\Delta P$  based on scaling relations (12 Mt, 2000 kg/m<sup>3</sup>, 25°, 27 km/s).

Contours (from dark to light):  $\Delta P \sim 1500, 1000, 700$  and 500 Pa

(*Jenniskens et al. 2019*)



$\Delta P$  obtained in the frame of QL model (*Shuvalov et al. 2017*), black circles - reported damage, open circles – no damage.

Main characteristics of  $\Delta P$  zones ( $>1$  kPa) - satisfactory agreement  
Scaling relations (not given) are also in agreement.

## Projectile Parameters

Diameter: *19 m*  
Density: *3320 kg/m<sup>3</sup>*

## Impact Parameters

Velocity: *19.2 km/s*  
Entry Angle: *18.3 °*

## Point of Effect

Distance to the point of intersection of the trajectory with the Earth's surface: *100.05 km*

## BASIC

## ADVANCED

## Projectile Parameters

Diameter, m

19

Density, kg/m<sup>3</sup>

3320



## Point of Effect

Distance to the point of intersection of the trajectory with the Earth's surface, km

100.05



## Impact Parameters

Velocity, km/s

19.2



Entry Angle, °

18.3



Angle to Trajectory Projection, °

89.95


[RUN CALCULATIONS](#)

## Impact Effects

Comprehensive assessment of hazardous effects caused by impacts of cosmic bodies

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## Projectile Parameters

Diameter: 19 m  
 Density: 3320 kg/m<sup>3</sup>  
 Energy:  $2.19 \cdot 10^{15}$  J  
 Energy (kt TNT):  $5.23 \cdot 10^2$  kt TNT

## Entry Parameters







Velocity: 19.16 km/s  
 Entry Angle: 18°  
 Latitude: 54.45°  
 Longitude: 64.56°  
 Azimuth: 103°

## Observation Point

Zero Point: *The point of intersection of the trajectory with the Earth's surface*  
 Angle to Trajectory Projection,  $\psi$ : 92°  
 Distance to the Zero Point, L: 107 km  
 Distance Across the Trajectory Projection, L<sub>y</sub>: 107 km  
 Distance Along the Trajectory Projection, L<sub>x</sub>: 3 km  
 Latitude,  $\phi$ : 54.04°  
 Longitude,  $\lambda$ : 59.62°

[ALTER PARAMETERS](#)

## RESULTS

	Airblast Wave	Overpressure: 0.0016 atm (0.16 kPa)	<a href="#">more...</a>
	Irradiation	Thermal exposure: 0.14 J/cm <sup>2</sup>	<a href="#">more...</a>
	Crater	No crater	<a href="#">more...</a>
	Ejecta	No ejecta	<a href="#">more...</a>
	Seismic effect	Magnitude: 3.4	<a href="#">more...</a>
	Atmospheric disturbances	Peak amplitude of relative density oscillations at an altitude of 300 km: 0.52	<a href="#">more...</a>

## Impact Effects

Comprehensive assessment of hazardous effects caused by impacts of cosmic bodies

## Navigation

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## Projectile Parameters

Diameter: 30 m  
 Density: 3320 kg/m<sup>3</sup>  
 Energy:  $5.28 \cdot 10^{15}$  J  
 Energy (kt TNT):  $1.26 \cdot 10^3$  kt TNT

## Entry Parameters

Velocity: 15.00 km/s  
 Entry Angle: 60°  
 Latitude: 54.45°  
 Longitude: 64.56°  
 Azimuth: 103°

## Observation Point

Zero Point: The point of intersection of the trajectory with the Earth's surface  
 Angle to Trajectory Projection,  $\psi$ : 180°  
 Distance to the Zero Point, L: 50 km  
 Distance Across the Trajectory Projection, L<sub>y</sub>: 0 km  
 Distance Along the Trajectory Projection, L<sub>x</sub>: -50 km  
 Latitude,  $\phi$ : 54.46°  
 Longitude,  $\lambda$ : 64.45°

ALTER PARAMETERS

## RESULTS



## Airblast Wave

Overpressure: 0.013 atm (1.3 kPa)

...less

*Numerical simulations of a shock wave from the cosmic object impact provide possibility to suggest scaling relations for a value of maximal overpressure and its distribution on the surface, for maximal wind velocity behind the front and for a squares, where overpressure is larger than a fixed level all values are determined based only on the properties of the impactor*

Effective Altitude: 12 km

Maximal overpressure: 0.12 atm (12 kPa)

Distance to the center of a overpressure field from the point of intersection of the trajectory with the Earth's surface: 5.6 km

Areas, at which chosen levels of overpressure exceed:

at 0.02 atm: 0.42 km<sup>2</sup>at 0.05 atm: 0.07 km<sup>2</sup>at 0.1 atm: 0.04 km<sup>2</sup>at 0.2 atm: 0.04 km<sup>2</sup>

The value of the overpressure in the point of observation: 0.013 atm (1.3 kPa)

Maximum wind speed behind the shock front in the point of observation: 3 m/s



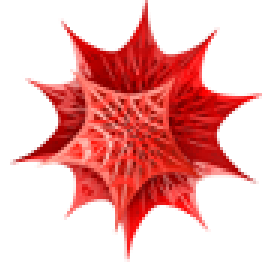
## Irradiation

Thermal exposure: 1.0 J/cm<sup>2</sup>

more...

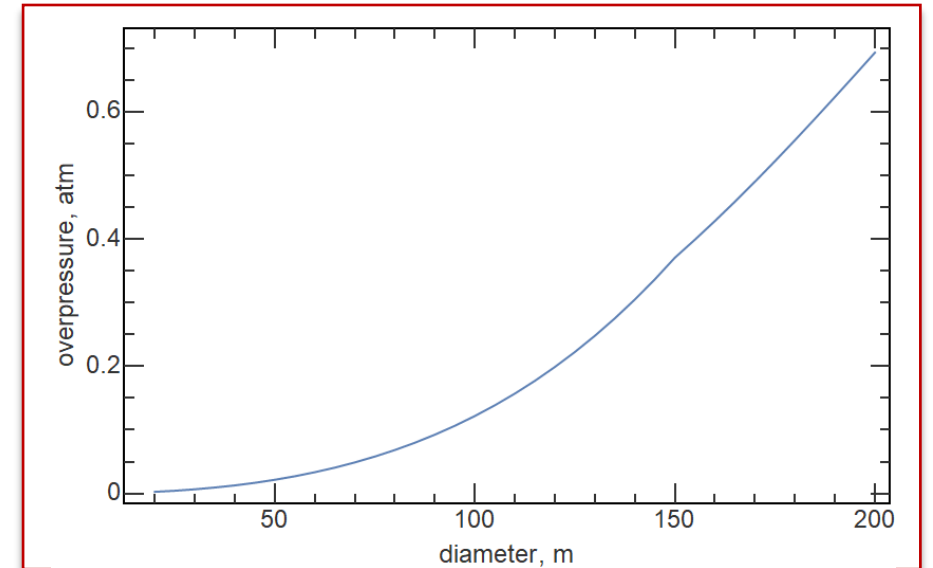
# API (application programming interface)

# Wolfram *Mathematica*<sup>®</sup>



## HTTP post request

```
retrievedF[d_] := Import[URLRead[HTTPRequest["http://asteroidhazard.pro/en/api", <|"Method" → "POST", "ContentType" → "application/json", "Body" → ExportString[  
  <|  
    "effects" → {"shockwave"},  
    "impactor" → <|"diameter" → d, "density" → 3320|>,  
    "entry" → <|"angle" → 18.3, "velocity" → 19|>,  
    "point_of_effect" → <|  
      "distance_across_trajectory" → 20,  
      "distance_along_trajectory" → 5|>  
    |>  
  , "RawJSON", "Compact" → True] |>]],  
  "RawJSON"] ["shockwave"] ["overpressure"] ["value"];  
In[ ]:= data = Table[{d, retrievedF[d]}, {d, 20, 200, 5}];
```



# Summary

- The scaling relations for shock wave effects for 20 – 3000 m objects impact are presented. Scaling relations for overpressure, wind and some other characteristics are constructed.
- For the first time this scaling relations take into account spatial asymmetry induced by impact angle.
- Suggested scaling relations were compared with modelling results and existing observational data and demonstrated reasonable agreement
- Described scaling relations are implemented into web-based calculator
- PDC probable impactor parameters are very uncertain and its impact may result in consequences of different scale.

The background features a series of concentric, overlapping circles and arcs. Some are solid lines, while others are dashed. The lines are light gray and create a sense of depth and movement, resembling a stylized orbital path or a ripple effect.

**Thank you for attention**

**follow the updates on the site**  
**[AsteroidHazard.pro](http://AsteroidHazard.pro)**