



# Comparing Coincident Elevation and Freeboard of IceBridge ATM, Cryosat-2, and Sentinel-3 over Arctic Sea Ice

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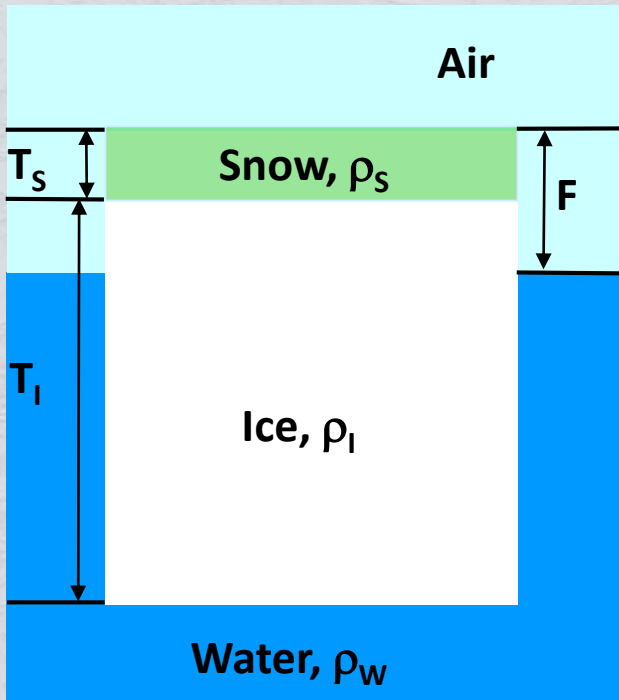
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ESA: The DUAL-CRYO online Workshop on "Dual-Band Altimetry of the Cryosphere"

13/14 January 2021.

# Sea Ice Elevation, Freeboard, and Thickness



How good are the assumptions?

ATM/ICESat-2: Air/Snow boundary and Air/Water boundary

Cryosat-2/Sentinel-3: Snow/Ice boundary and Air/Water boundary

Snow Thickness:  $H_{\text{laser}} - H_{\text{radar}}$   
OIB Snow radar, AMSR-E, Climatology, Models

Archimedes' principle

Sea Ice Thickness  $T_i$  is a function of Freeboard  $F$  and Snow Thickness  $T_s$ :

$$T_i = \rho_w / (\rho_w - \rho_i) \times F - (\rho_w - \rho_s) / (\rho_w - \rho_i) \times T_s$$

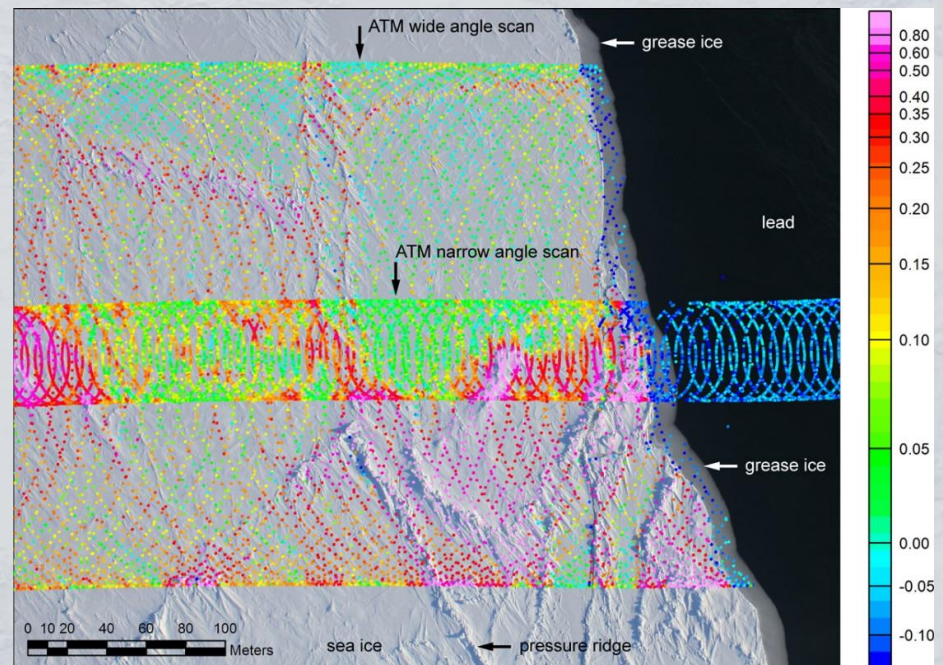
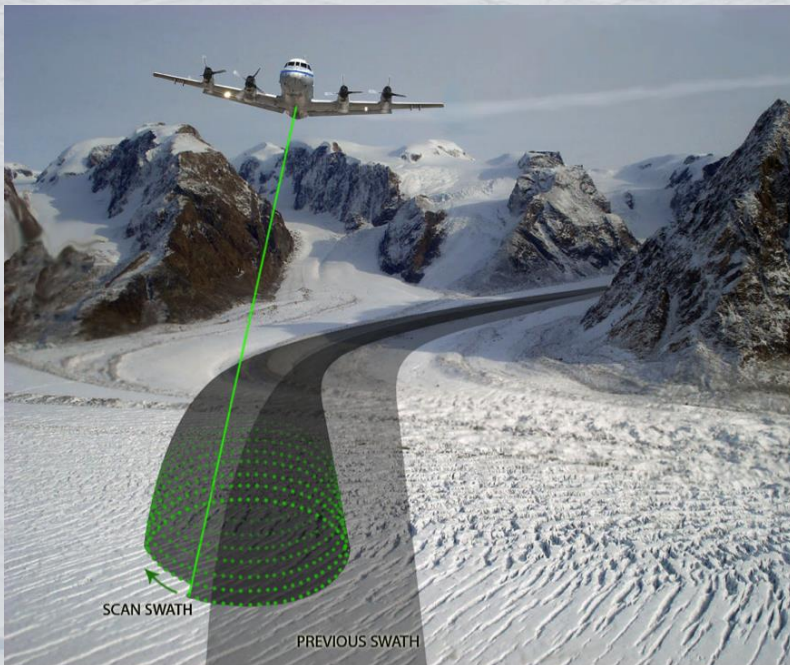
$$T_i = 9.411 \times F - 6.653 \times T_s$$



# Airborne Topographic Mapper (ATM)

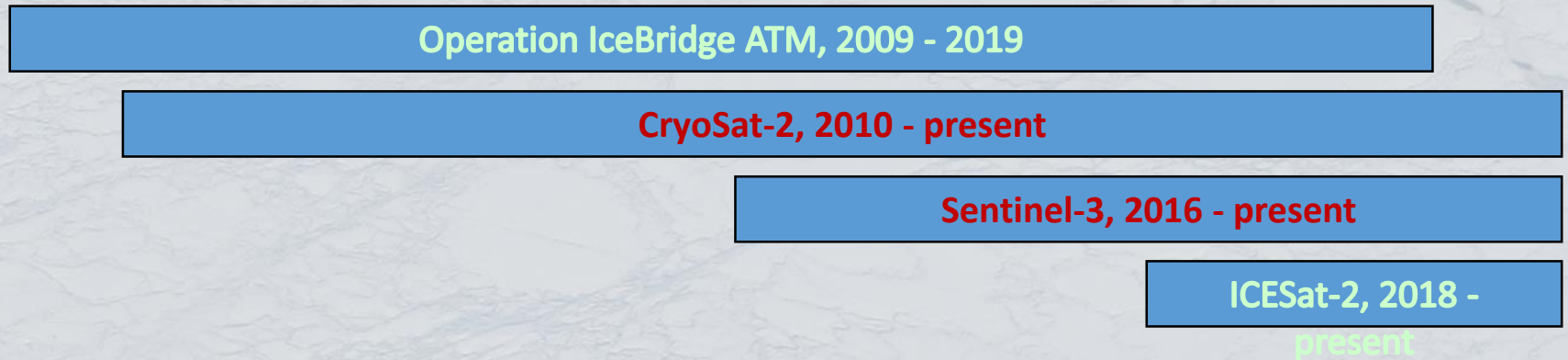
Two conical scanning laser altimeters:

Off-nadir Scan Angle	Swath Width at 1500 ft AGL	Wavelength	Footprint at 1500 ft AGL	Elevation Accuracy/Precision
15° - wide	250 m	532 nm	1 m	< 7 cm / 8 cm Brunt et al., 2017
2.5° - narrow	40 m	532 nm	1 m	< 7 cm / 3 cm





# ATM, Cryosat-2, Sentinel-3, and ICESat-2



## Data to be compared:

- Coincident ATM elevations, freeboard, IceBridge Snow depth  
VS  
Cryosat-2/Sentinel-3 elevations and freeboards  
(Standard Cryosa-2/Sentinel-3 data products and **Fully Focused SAR results**)
- Coincident Cryosat-2 and ICESat-2 elevations and freeboards
- CRISTAL data in the future

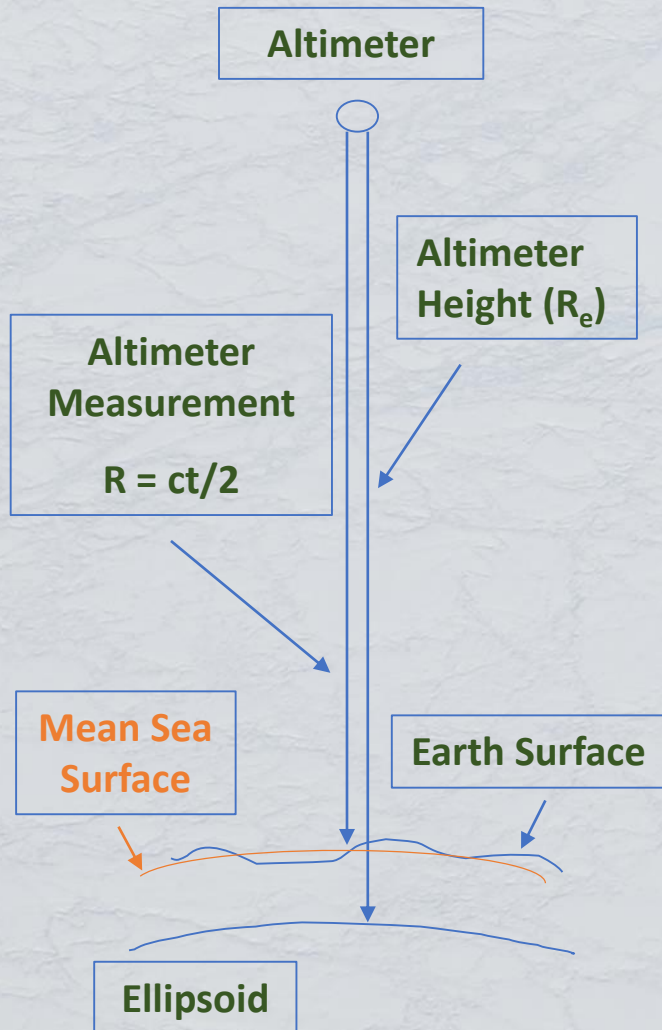


# ATM data coverage (2009-2019)



**Will use the  
coincident data of  
ATM and Cryosat-2  
and Sentinel-3**

# Surface Elevation



## Sea Surface Elevation

$$H = h_e - h_{mss} - h_{st} - h_{ot} - h_{lt} - h_{pt} - h_{dac}$$

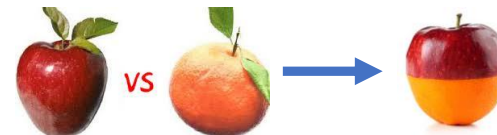
$h_e$ : elevation reference to ellipsoid (WGS84)

$h_{mss}$ : mean sea surface reference to  $h_e$  (DTU18MSS: including  $h_{geoid}$  and  $h_{dynamic\_topography}$ )

$h_{st}$ ,  $h_{ot}$ , and  $h_{lt}$  are solid earth tide, ocean tide, and load tide

$h_{pt}$ : permanent tide

$h_{dac}$ : dynamic atmospheric correction



Identical ellipsoid, geoid model, tide model, and dynamic atmospheric corrections for CryoSat-2, Sentinel-3, ICESat-2, and IceBridge data to eliminate elevation biases due to their differences.

# Methods

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To derive Cryosat-2/Sentinel-3 elevation and freeboard:

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IEEE TRANSACTIONS ON GEOSCIENCE AND REMOTE SENSING, VOL. 55, NO. 1, JANUARY 2017

## Fully Focused SAR Altimetry: Theory and Applications


Alejandro Egido, *Member, IEEE*, and Walter H. F. Smith

To compare elevation and freeboard:

IEEE TRANSACTIONS ON GEOSCIENCE AND REMOTE SENSING, VOL. 57, NO. 2, FEBRUARY 2019

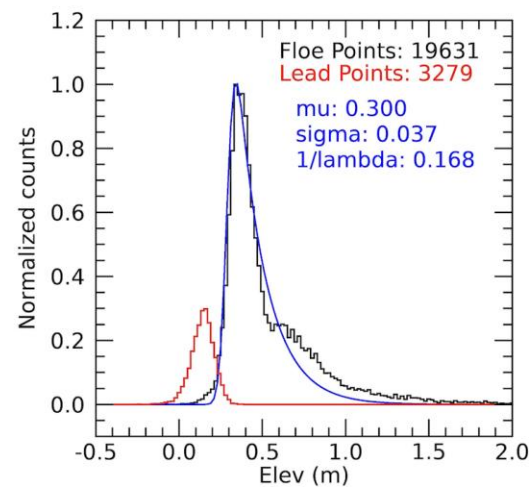
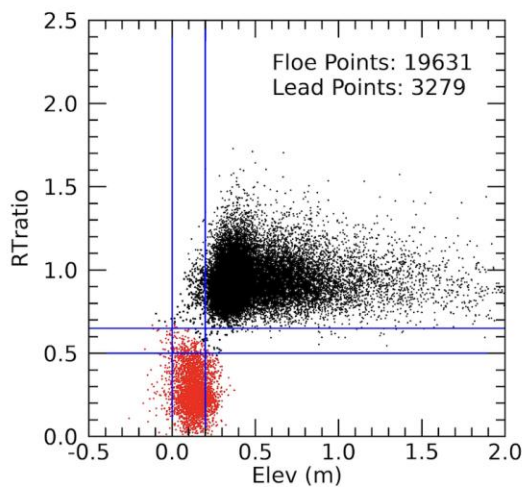
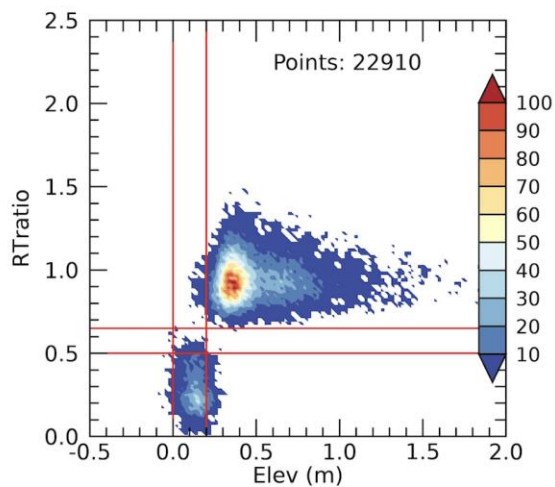
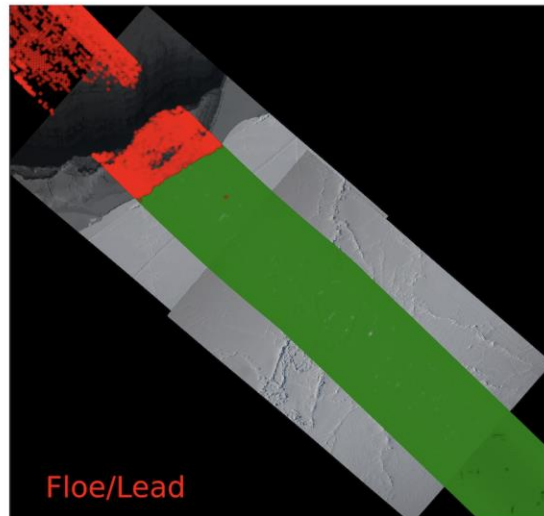
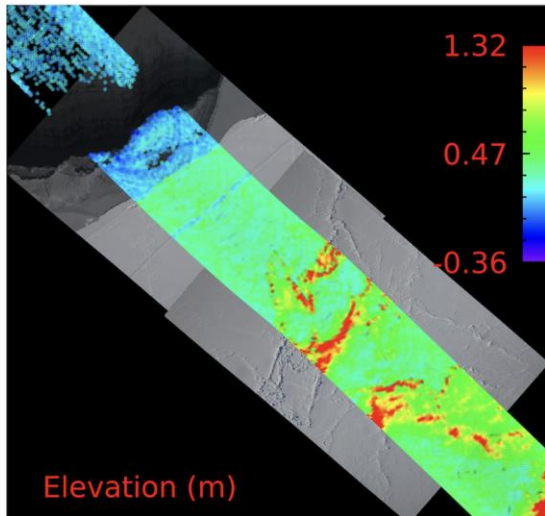
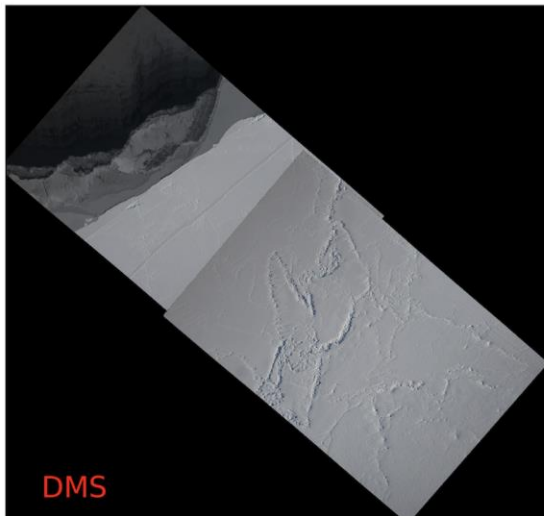
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## Comparing Coincident Elevation and Freeboard From IceBridge and Five Different CryoSat-2 Retracker

Donghui Yi , Nathan Kurtz, Jeremy Harbeck, Ron Kwok, Stefan Hendricks, and Robert Ricker



# ATM Cluster Analysis – Separate floe and lead

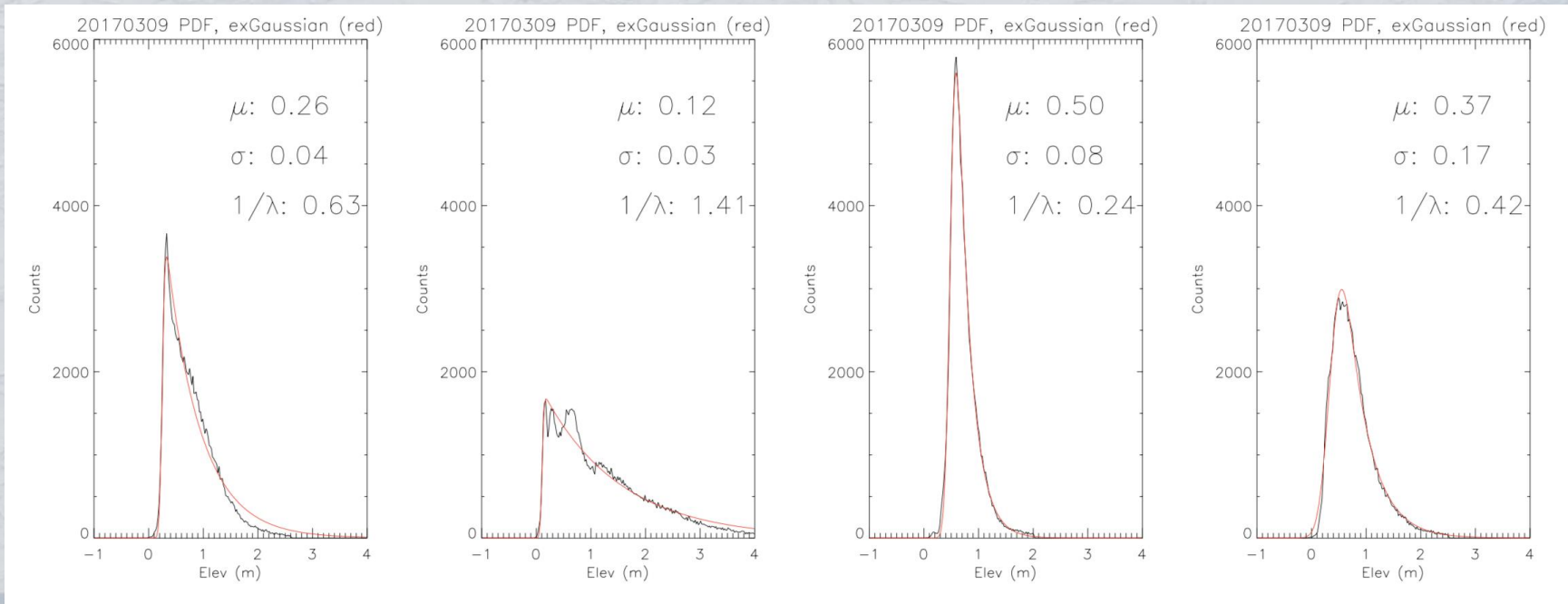




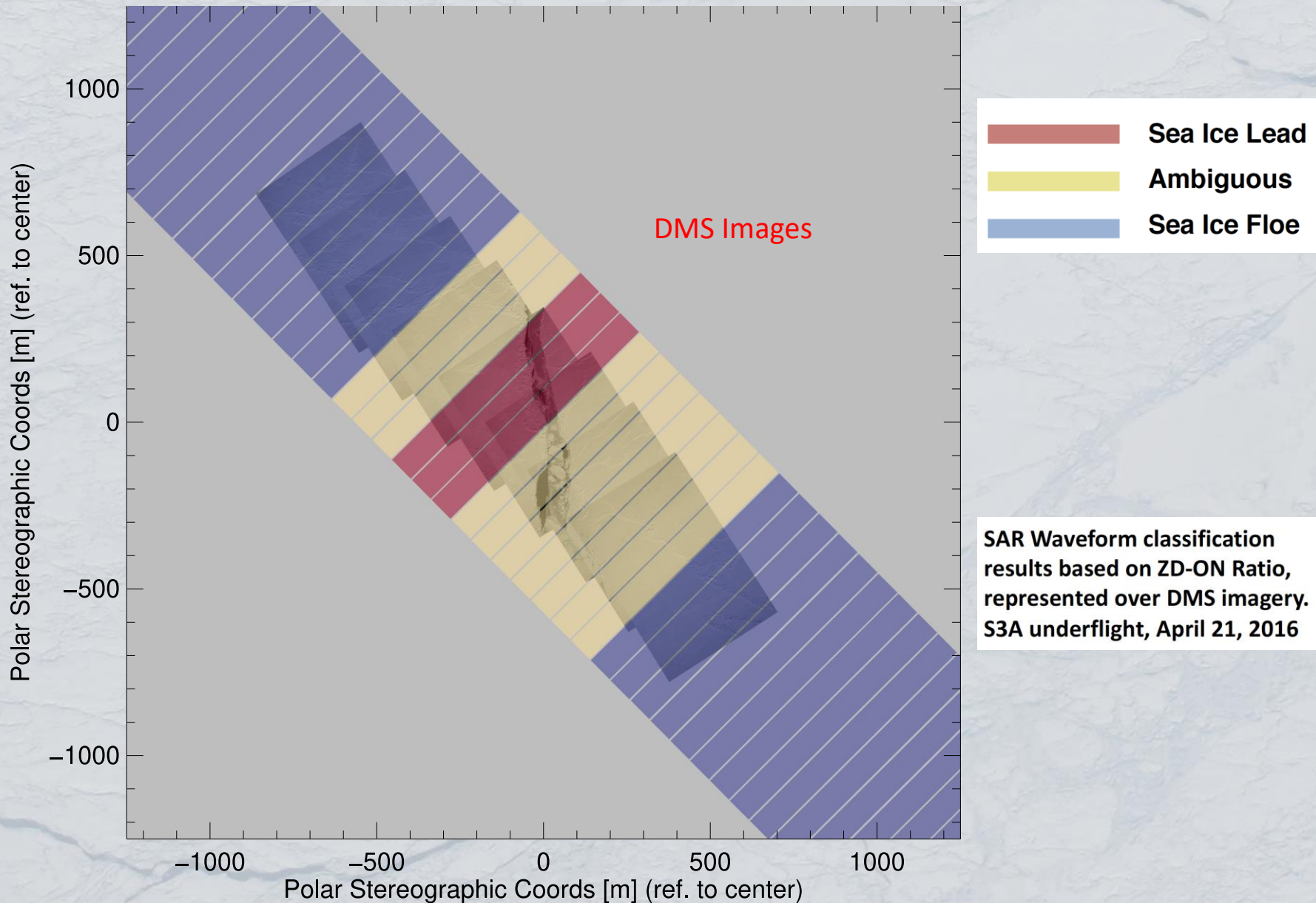
# ATM elevation PDF and exGaussian fitting

The probability density function (PDF) of the surface height is calculated from ATM elevation and modeled using the probability density function of the exponentially modified normal distribution (exGaussian),

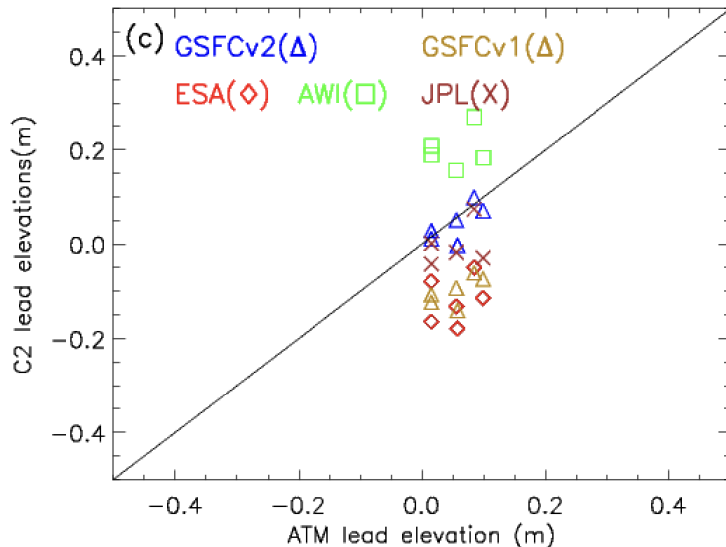
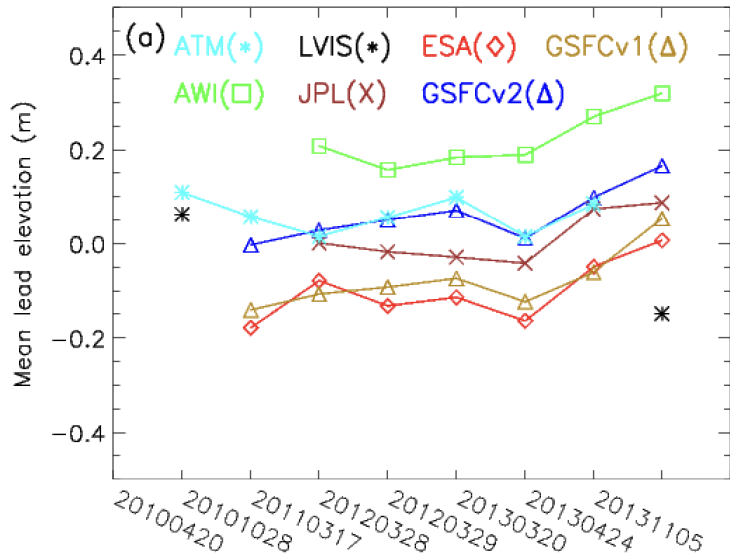
$$f(x; \mu, \sigma, \lambda) = \frac{\lambda}{2} e^{\frac{\lambda}{2}(2\mu + \lambda\sigma^2 - 2x)} \operatorname{erfc}\left(\frac{\mu + \lambda\sigma^2 - x}{\sqrt{2}\sigma}\right)$$



# SAR Waveform Classification



# ATM VS Cryosat-2 retrackerers (Yi et al, 2019)



## Mean lead elevation

The five Cryosat-2 retrackerers used are:

ESA (Laxon et al, 2013)

GSFCv1 (Kurtz et al, 2014)

AWI (Ricker et al, 2014)

**(there is an new version)**

JPL (Kwok and Cunningham, 2016)

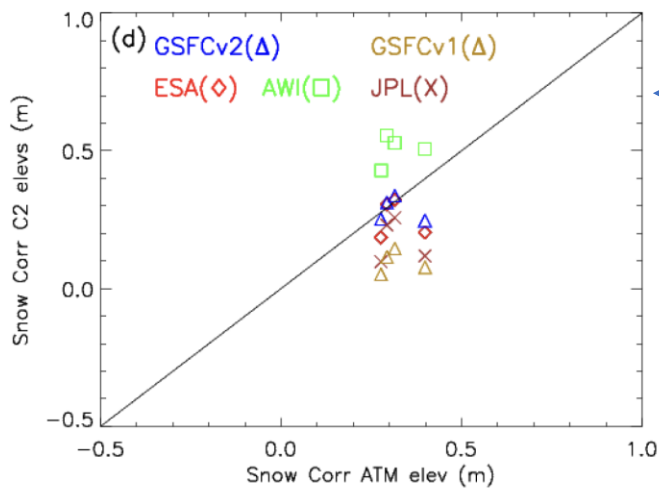
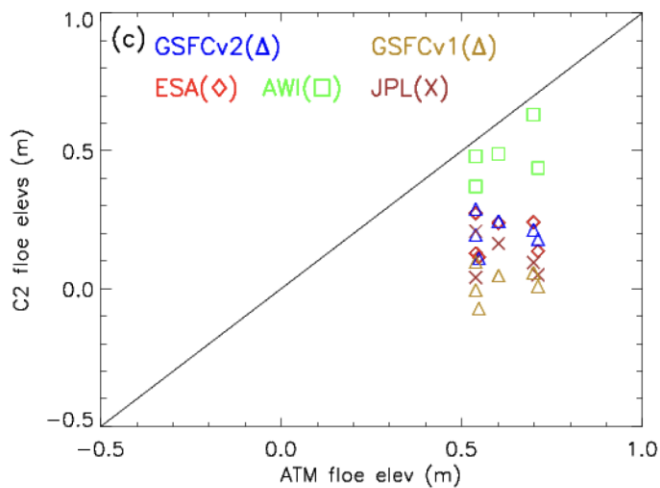
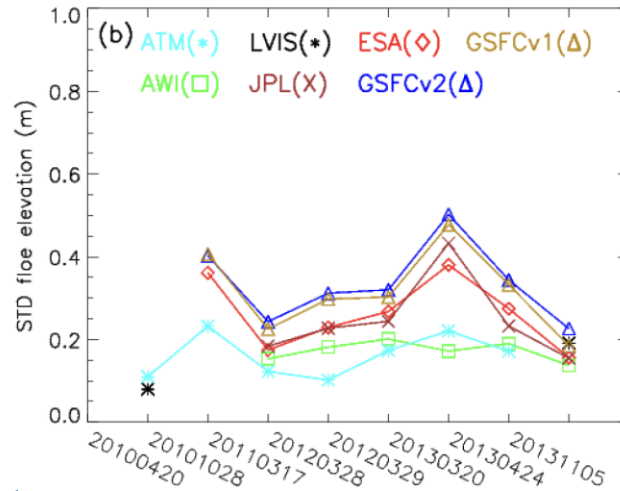
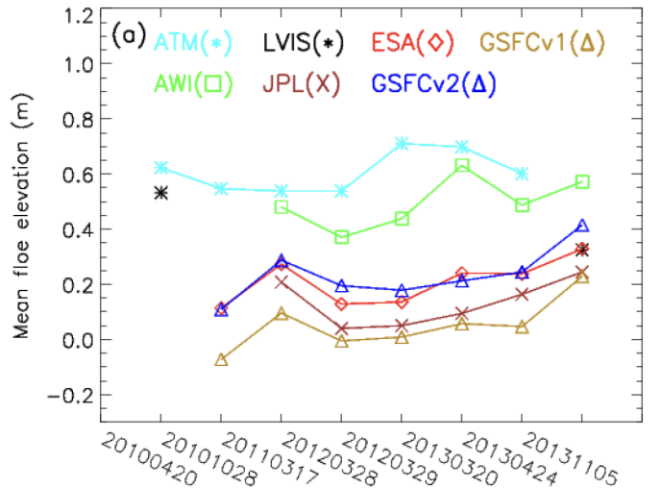
GSFCv2 (an improved version of GSFCv1)

These retrackerers show distinct differences in mean elevation up to 0.45 meters over leads.

**Elevation is retrackerer dependent!**



# Mean floe elevation (Yi et al, 2019 )



(a), (c)  
Original elevation;

These retrackerers  
show distinct  
differences in  
mean elevation  
up to 0.75 meters  
over floes.

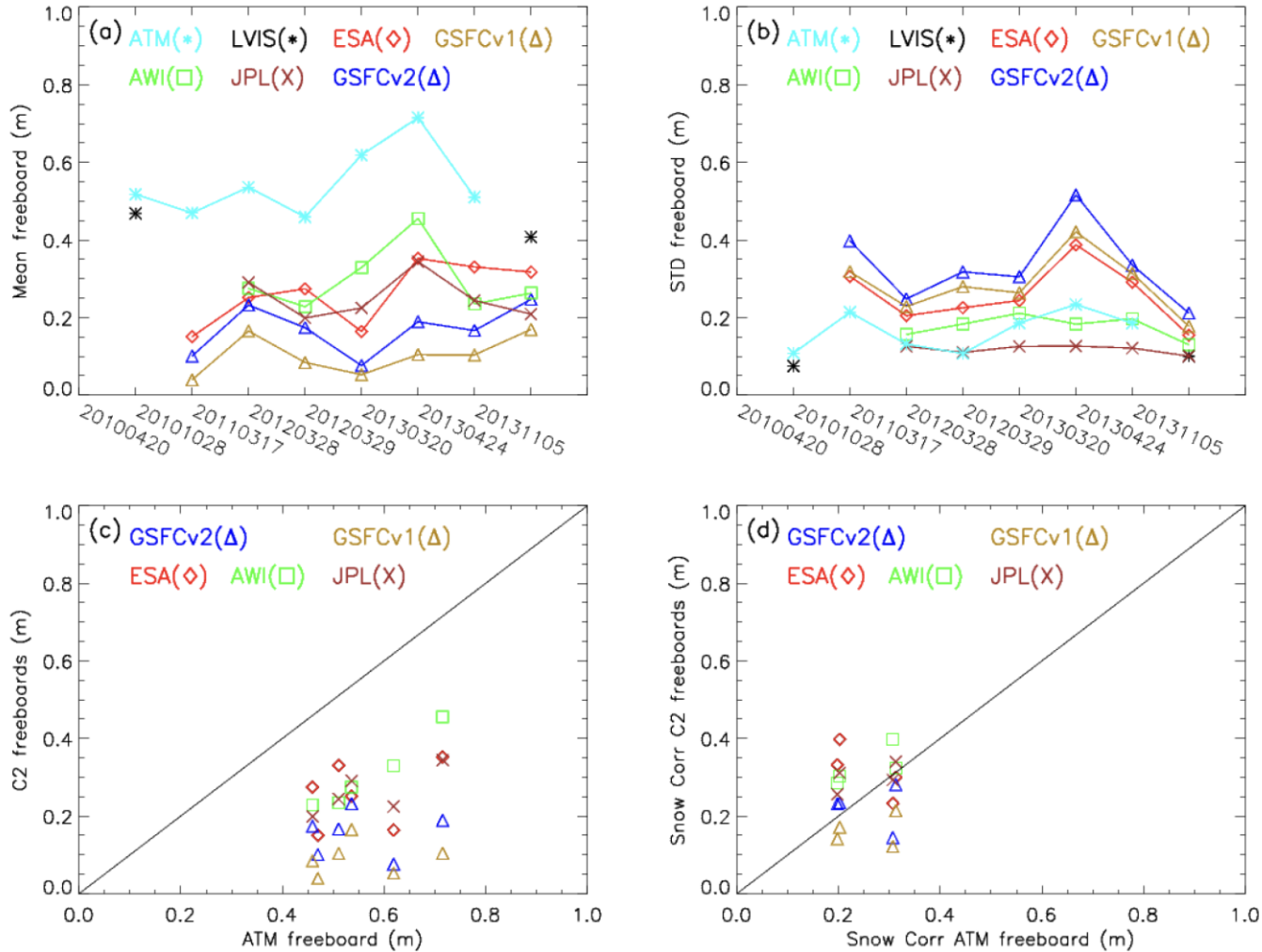
(d) Snow/ice  
interface

ATM - Snow depth

CryoSat-2 +  
 $0.2191 \times$  snow  
depth (speed of  
light Correction)

Fig. 6. (a) Mean floe elevation, (b) STD of floe elevation, (c) CryoSat-2 floe elevation versus ATM floe elevation, and CryoSat-2 versus ATM elevation at the snow/ice interface (d).

# Mean freeboard (Yi et al, 2019)



Snow/ice interface

ATM – Snow depth

Cryosat-2 +  
0.2191 × snow  
depth  
(speed of light  
Correction)

Mean Cryosat-2 -  
ATM:  
-0.03, 0.04, 0.06,  
0.07, and -0.09  
meters.

Fig. 7. (a) Mean freeboard, (b) STD of freeboard, (c) CryoSat-2 freeboard versus ATM freeboard (c), and (d) CryoSat-2 versus ATM freeboard at the snow/ice interface (d).



# Summary

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**Radar altimeter sea ice elevation and freeboard are retracker dependent. Since sea ice freeboard retrieval methods use relative elevations, the freeboard biases are less than floe elevation biases between the retrackers.**

**Snow depth can be estimated by Laser – Radar freeboard and it is also retracker dependent.**

**We believe Fully Focused SAR technique will improve Cryosat-2/Sentinel-3 waveform retracking and will compare ATM elevation and freeboard with FFSAR results for calibration/validation.**

**Similar technique can be used for Cryosat-2/ICESat-2 data comparison and maybe for future CRISTAL data analysis.**